

**LECTURE NOTES**  
**ON**  
**COMPUTER ORGANIZATION AND ARCHITECTURE**

**III semester (IARE - R16)**

**Dr. Y. MOHANA ROOPA**  
Professor

**Dr. P. L. SRINIVASA MURTHY**  
Professor

**MR. N.V.KRISHNA RAO**  
Assistant Professor

**MS. A.SWAPNA**  
Assistant Professor



**COMPUTER SCIENCE AND ENGINEERING**  
**INSTITUTE OF AERONAUTICAL ENGINEERING**  
(AUTONOMOUS)  
DUNDIGAL, HYDERABAD - 500 043

## UNIT-I

### INTRODUCTION TO COMPUTER ORGANIZATION

Basic Computer Organization – CPU Organization – Memory Subsystem Organization and Interfacing – I/O Subsystem Organization and Interfacing – A Simple Computer- Levels of Programming Languages, Assembly Language Instructions, Instruction Set Architecture Design, A simple Instruction Set Architecture.

#### 1.1 BASIC COMPUTER ORGANIZATION:

Most of the computer systems found in automobiles and consumer appliances to personal computers and main frames have some basic organization. The basic computer organization has three main components:

- CPU
- Memory subsystem
- I/O subsystem.

The generic organization of these components is shown in the figure below.

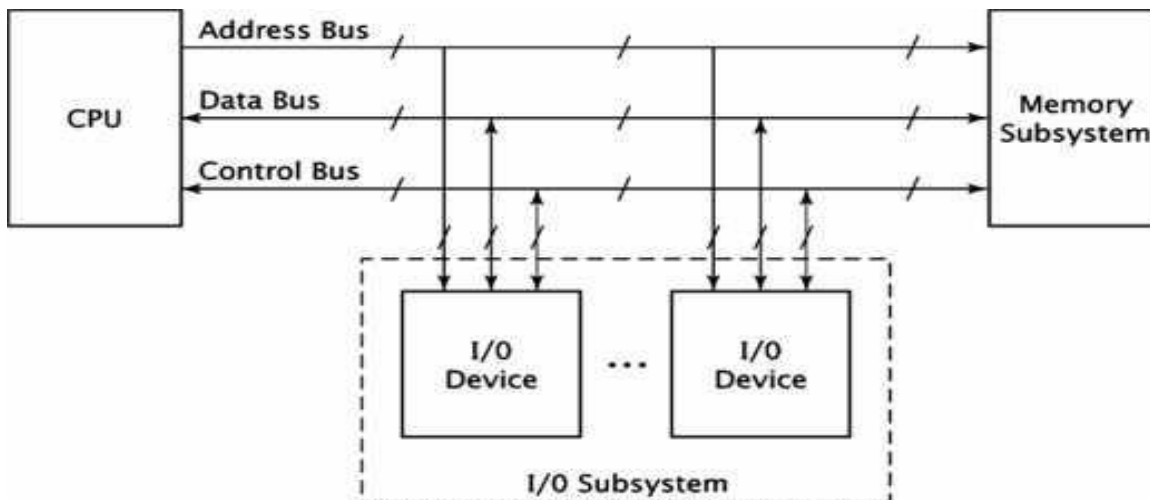


Fig 1.1 Generic computer Organization

##### 1.1.1 System bus:

Physically the bus is a set of wires. The components of a computer are connected to the buses. To send information from one component to another the source component outputs data on to the bus. The destination component then inputs the data from bus.

The system has three buses

- Address bus
- Data bus
- Control bus

- The uppermost bus in this figure is the **address bus**. When the CPU reads data or instructions from or writes data to memory, it must specify the address of the memory location it wishes to access.
- Data is transferred via the **data bus**. When CPU fetches data from memory it first outputs the memory address on to its address bus. Then memory outputs the data onto the data bus. Memory then reads and stores the data at the proper locations.
- **Control bus** carries the control signal. Control signal is the collection of individual control signals. These signals indicate whether data is to be read into or written out of the CPU.

### 1.1.2 Instruction cycles:

- The instruction cycle is the procedure a microprocessor goes through to process an instruction.
- First the processor **fetches** or reads the instruction from memory. Then it decodes the instruction determining which instruction it has fetched. Finally, it performs the operations necessary to execute the instruction.
- After fetching it **decodes** the instruction and controls the execution procedure. It performs some Operation internally, and supplies the address, data & control signals needed by memory & I/O devices to **execute** the instruction.
- The READ signal is a signal on the control bus which the microprocessor asserts when it is ready to read data from memory or I/O device.
- When READ signal is asserted the memory subsystem places the instruction code be fetched on to the computer system's data bus. The microprocessor then inputs the data from the bus and stores its internal register.
- READ signal causes the memory to read the data, the WRITE operation causes the memory to store the data.

Below figure shows the memory read and memory write operations.

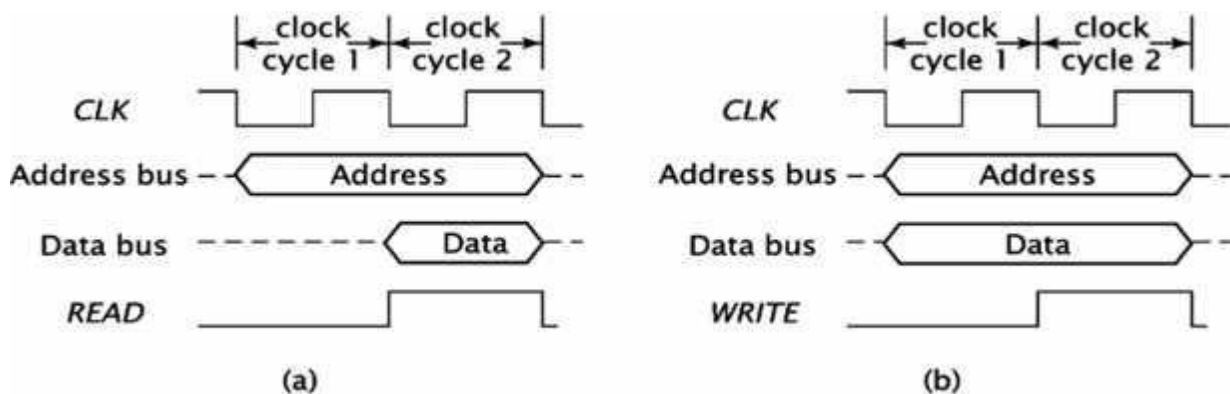


Fig 1.2: Timing diagram for memory read and memory write operations

- In the above figure the top symbol is CLK. This is the computer system clock. The processor uses the system clock to synchronize its operations.
- In fig (a) the microprocessor places the address on to the bus at the beginning of a clock cycle, a 0/1 sequence of clock. One clock cycle later, to allow for memory to decode the address and access its data, the microprocessor asserts the READ control signal. This causes the memory to place its data onto the system data bus. During this clock cycle, the microprocessor reads the data off the system bus and stores it in one of the registers. At the end of the clock cycle it removes the address from the address bus and deasserts the READ signal. Memory then removes the data from the data bus completing the memory read operation.
- In fig(b) the processor places the address and data onto the system bus during the first clock pulse. The microprocessor then asserts the WRITE control signal at the end of the second clock cycle. At the end of the second clock cycle the processor completes the memory write operation by removing the address and data from the system bus and deasserting the WRITE signal.
- I/O read and write operations are similar to the memory read and write operations. Basically the processor may use memory mapped I/O and isolated I/O.
- In memory mapped I/O it follows the same sequence of operations to input data as to read from or write data into memory.

In isolated I/O follow same process but have a second control signal to distinguish between I/O and memory accesses. For example in 8085 microprocessor has a control signal called  $\overline{IO}/\overline{MEM}$ . The processor set  $\overline{IO}/\overline{MEM}$  to 1 for I/O read and write operations and 0 for memory read and write operations.

## 1.2 CPU ORGANIZATION:

**Central processing unit (CPU)** is the electronic circuitry within a computer that carries out the instructions of a computer program by performing the basic arithmetic, logical, control and input/output (I/O) operations specified by the instructions.

In the computer all the major components are connected with the help of the **system bus**. **Data bus** is used to shuffle data between the various components in a computer system.

To differentiate memory locations and I/O devices the system designer assigns a unique memory address to each memory element and I/O device. When the software wants to access some particular memory location or I/O device it places the corresponding address on the **address bus**. Circuitry associated with the memory or I/O device recognizes this address and instructs the memory or I/O device to read the data from or place data on the data bus. Only the device whose address matches the value on the address bus responds.

The **control bus** is an eclectic collection of signals that control how the processor communicates with the rest of the system. The **read** and **write** control lines control the direction of data on the data bus.

When both contain logic one the CPU and memory-I/O are not communicating with one another. If the read line is low (logic zero) the CPU is reading data from memory (that is the system is transferring data from memory to the CPU). If the write line is low the system transfers data from the CPU to memory.

The CPU controls the computer. It **fetches** instructions from memory, supply the address and control signals needed by the memory to access its data.

Internally, CPU has three sections as shown in the fig below

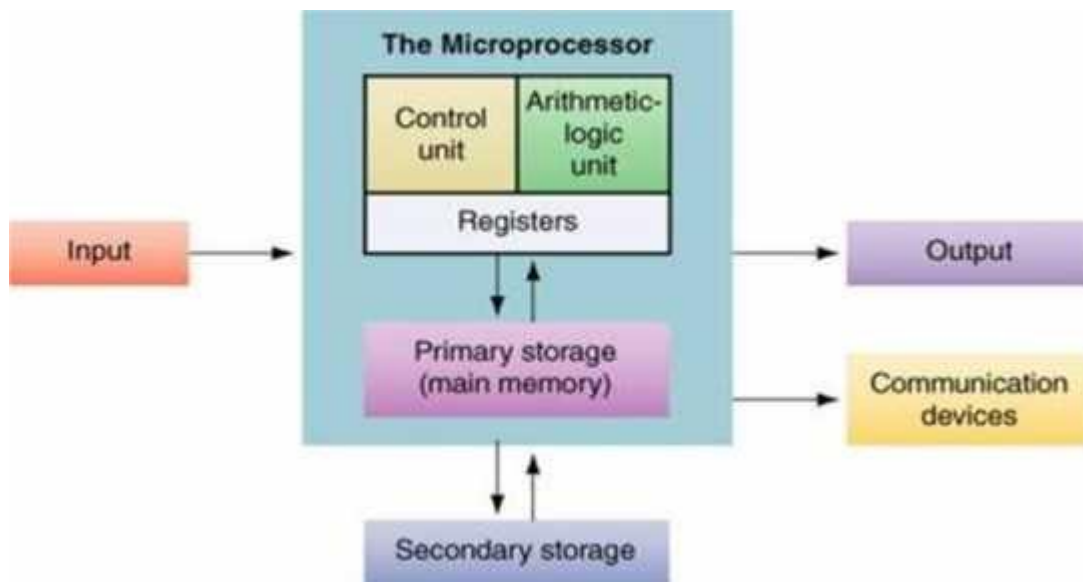


Fig 1.3: CPU Organization

- The register section, as its name implies, includes a set of registers and a bus or other communication mechanism.
- The register in a processor's instruction set architecture are found in the section of the CPU.
- The system address and data buses interact with this section of CPU. The register section also contains other registers that are not directly accessible by the programmer.
- The fetch portion of the instruction cycle, the processor first outputs the address of the instruction onto the address bus. The processor has a register called the "**program counter**".
- The CPU keeps the address of the next instruction to be fetched in this register. Before the CPU outputs the address on to the system bus, it retrieves the address from the program counter register.
- At the end of the instruction fetch, the CPU reads the instruction code from the system data bus.
- It stores this value in an internal register, usually called the "**instruction register**".
- The arithmetic / logic unit (or) ALU performs most arithmetic and logic operations such as adding and ANDing values. It receives its operands from the register section of the CPU and stores its result

back in the register section.

- Just as CPU controls the computer, the control unit controls the CPU. The control unit receives some data values from the register unit, which it used to generate the control signals. This code generates the instruction codes & the values of some flag registers.
- The control unit also generates the signals for the system control bus such as READ, WRITE, IO/M signals.

### **1.3 MEMORY SUBSYSTEM ORGANIZATION AND INTERFACING:**

Memory is the group of circuits used to store data. Memory components have some number of memory locations, each word of which stores a binary value of some fixed length. The number of locations and the size of each location vary from memory chip to memory chip, but they are fixed within individual chip.

The size of the memory chip is denoted as the number of locations times the number of bits in each location. For example, a memory chip of size  $512 \times 8$  has 512 memory locations, each of which has eight bits. The address inputs of a memory chip choose one of its locations. A memory chip with  $2^n$  locations requires n address inputs.

- View the memory unit as a black box. Data transfer between the memory and the processor takes place through the use of two registers called MAR (Memory Address Register) and MDR (Memory data register).
- MAR is n-bits long and MDR is m-bits long, and data is transferred between the memory and the processor. This transfer takes place over the processor bus.

#### **Internal organization of the memory chips:**

- Memory is usually organized in the form of arrays, in which each cell is capable of storing one bit information.
- A possible organization is stored in the fig below...
- Each row of cell constitutes a memory word, and all cells of a row are connected to a common column called word line, which is driven by the address decoder on the chip.
- The cells in each column are connected to sense/write circuit by two bit lines.
- The sense /write circuits are connected to the data input/output lines of the chip.
- During read operation these circuits sense or read the information stored in cells selected by a word line and transmit the information to the output lines.
- During write operation the sense/write circuit receives the input information and store in the cell of selected word.

## Types of Memory:

There are two types of memory chips

1. Read Only Memory (ROM)
2. Random Access Memory (RAM)

### a) ROM Chips:

ROM chips are designed for applications in which data is read. These chips are programmed with data by an external programming unit before they are added to the computer system. Once it is done the data does not change. A ROM chip always retains its data, even when

Power to chip is turned off so ROM is called **nonvolatile** because of its property. There are several types of ROM chips which are differentiated by how often they are programmed.

- Masked ROM(or) simply ROM
- PROM(Programmed Read Only Memory)
- EPROM(Electrically Programmed Read Only Memory)
- EEPROM(Electrically Erasable PROM)
- Flash Memory
  - A masked ROM or simply ROM is programmed with data as chip is fabricated.
  - The mask is used to create the chip and chip is designed with the required data hardwired in it.

Once chip is designed the data will not change. Figure below shows the possible configuration of the ROM cell.

- Logic 0 is stored in the cell if the transistor is connected to ground at point P, other wise 1 stored.
- A sense circuit at the end of the bit line generates at the high voltage indicating a 1. Data are written into the ROM when it is manufactured.

### PROM

- Some ROM designs allow the data to be loaded by the user, thus providing programmable ROM (PROM).
- Programmability is achieved by inserting a fuse at point P in the above fig. Before it is programmed, the memory contains all 0's.
- The user insert 1's at the required locations by burning out the fuse at these locations using high current pulse.
- The fuses in PROM cannot restore once they are blown, PROM's can only be programmed once.

### 2) EPROM

- EPROM is the another ROM chip allows the stored data to be erased and new data to be loaded. Such an erasable reprogrammable ROM is usually called an EPROM.

- Programming in EPROM is done by charging of capacitors. The charged and uncharged capacitors cause each word of memory to store the correct value.
- The chip is erased by being placed under UV light, which causes the capacitor to leak their charge.

### 3) EEPROM

- A significant disadvantage of the EPROM is the chip is physically removed from the circuit for reprogramming and that entire contents are erased by the UV light.
- Another version of EPROM is EEPROM that can be both programmed and erased electrically, such chips called EEPROM, do not have to remove for erasure.
- The only disadvantage of EEPROM is that different voltages are need for erasing, writing, reading and stored data.

### 4) Flash Memory

- A special type of EEPROM is called a flash memory is electrically erase data in blocks rather than individual locations.
- It is well suited for the applications that writes blocks of data and can be used as a solid state hard disk. It is also used for data storage in digital computers.

### RAM Chips:

- RAM stands for Random access memory. This often referred to as read/write memory. Unlike the ROM it initially contains no data.
- The digital circuit in which it is used stores data at various locations in the RAM are retrieves data from these locations.
- The data pins are bidirectional unlike in ROM.
- A ROM chip loses its data once power is removed so it is a volatile memory.
- RAM chips are differentiated based on the data they maintain.
  - Dynamic RAM (DRAM)
  - Static RAM (SRAM)

#### 1. Dynamic RAM:

- DRAM chips are like leaky capacitors. Initially data is stored in the DRAM chip, charging its memory cells to their maximum values.
- The charging slowly leaks out and would eventually go too low to represent valid data.
- Before this a refresher circuit reads the content of the DRAM and rewrites data to its original locations.
- DRAM is used to construct the RAM in personal computers.
- DRAM memory cell is shown in the figure below.



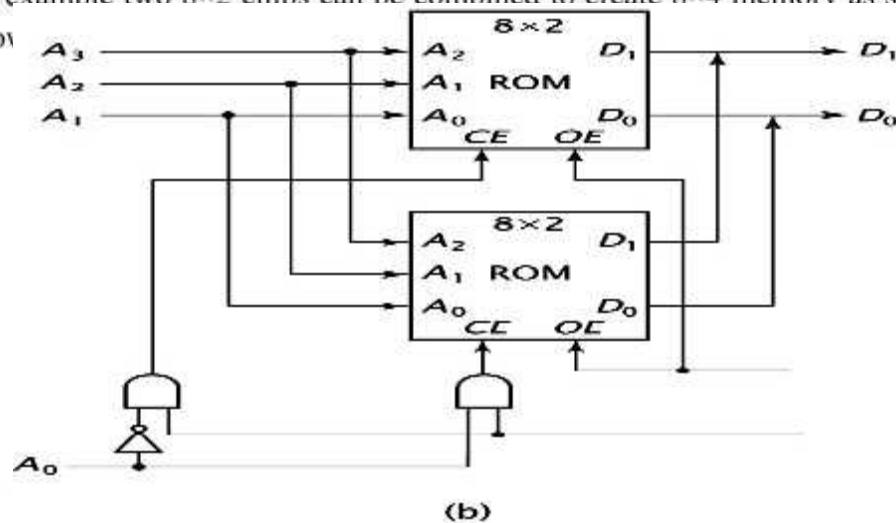
## 2. Static RAM:

- Static RAM are more likely the register .Once the data is written to SRAM, its contents stay valid it does not have to be refreshed.
- Static RAM is faster than DRAM but it is also much more expensive. Cache memory in the personal computer is constructed from SRAM.
- Various factors such as cost, speed, power consumption and size of the chip determine how a RAM is chosen for a given application
  - Static RAMs:
    - Chosen when speed is the primary concern.
    - Circuit implementing the basic cell is highly complex, so cost and size are affected.
    - Used mostly in cache memories.
  - Dynamic RAMs:
    - Predominantly used for implementing computer main memories.
    - High densities available in these chips.
    - Economically viable for implementing large memories

### Memory subsystem configuration:

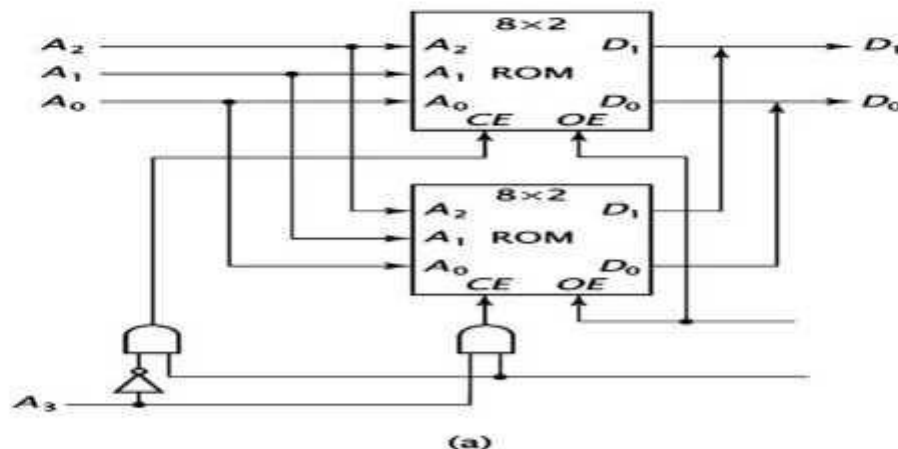
- Two or more chips are combined to create memory with more bits per location. This is done by connecting the corresponding address and control signals of chips and connecting their data pins to different bits of the data bus.
- The following figure fallowed the higher order interleaving where the higher order bit A3 is 0 and lower chip has A3 1. This difference is used to select one of the two chips.
- In the lower order interleaving we consider lower bit for selecting the two chips. So the upper chip is enabled when A0=0 or by address 0×××(or 0,2,4,6,8,10,12) and lower chip is enabled when A0=1 which is true for the address 1,3,5,7,9,11,13 and 15. Figure for lower order interleaving is shown in the figure below.

- For example two  $8 \times 2$  chips can be combined to create  $8 \times 4$  memory as shown the figure below



An  $8 \times 4$  memory subsystem constructed from two  $8 \times 2$  ROM chips

- Both receive the same address inputs from the bus as well as the same chips enable and output enable signals. The data pins of the first two connected to bits 3 and 2 of the data bus and other chip are connected to bits 1 and 0.
- When the CPU read the data it places the address on the address bus. Both the chips read the address and perform their internal decoding.
- If CE (Chip Enable) and OE (Output Enable) signals are activated. The chips place the data on the data bus because OE and CE are same for both chips. The same  $8 \times 2$  configured as a  $16 \times 2$  shown in the figure below.



A  $16 \times 4$  memory subsystem constructed from two  $8 \times 2$  ROM chips with higher order interleaving

- The upper chip is configured as memory locations 0-7(0000 to 0111). The lower chip is configured as 8 to 15(1000 to 1111).
- The configurations can be done by using two methods **higher order interleaving** and **lower order interleaving**.

### Multi byte organization:

- Many data formats use more than one 8-bit byte to represent a value whether it is an integer , floating point, or character string.
- Most CPU assign addresses to 8-bit memory locations so these values must be stored in more than one location. It is necessary for every CPU to define the order it expects for the data in these locations.
- There are two commonly used organizations for multi byte data.
  - Big endian
  - Little endian
- In BIG-ENDIAN systems the most significant byte of a multi-byte data item always has the lowest address, while the least significant byte has the highest address.
- In LITTLE-ENDIAN systems, the least significant byte of a multi-byte data item always has the lowest address, while the most significant byte has the highest address.

### 1.4 I/O SUBSYSTEM ORGANIZATION AND INTERFACING

The I/O subsystem is treated as an independent unit in the computer The CPU initiates I/O commands generically

- Read, write, scan, etc.
- This simplifies the CPU

Below figure shows the basic connection between the CPU, memory to the I/O device .The I/O device is connected to the computer system address, data and control buses. Each I/O device includes I/O circuitry that interacts with the buses.

#### INPUT DEVICE:

- The generic interface circuitry for an input device such as keyboard and also enable logic for tri state buffer is shown in the figure below.

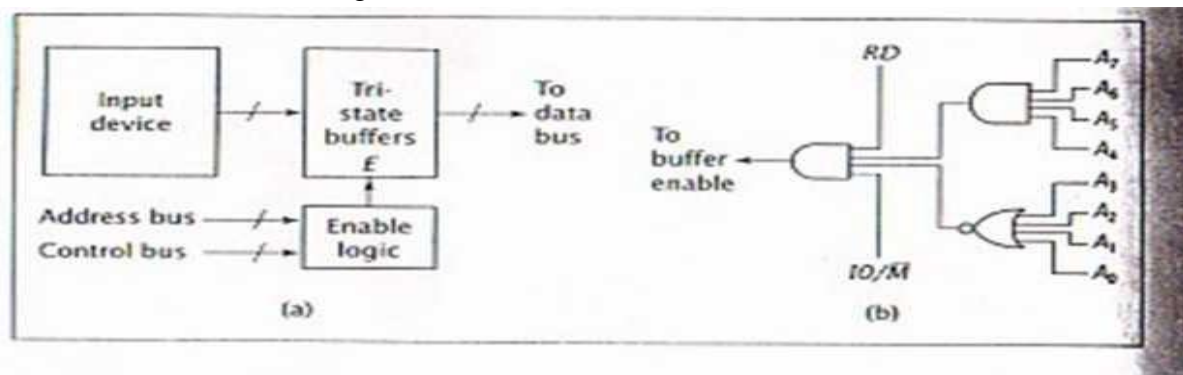
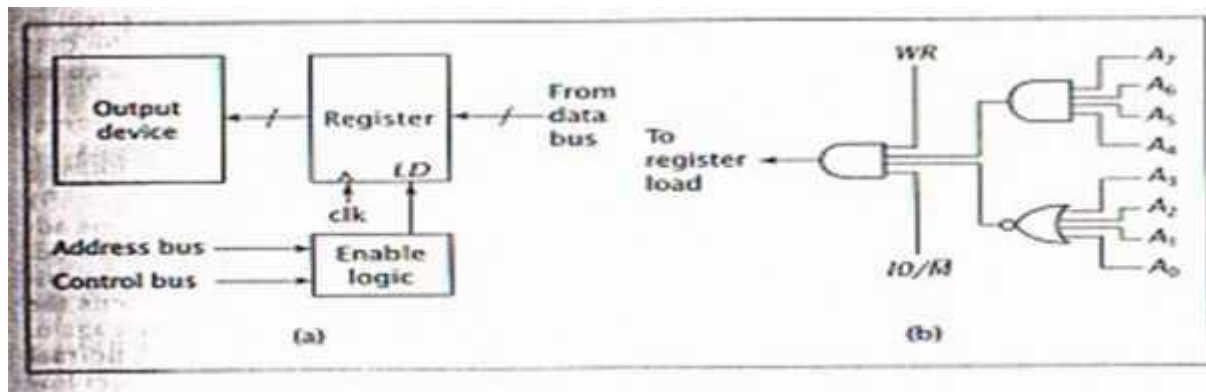


Fig 1.5: (a) with its interface and (b) the enable logic for the tri-state buffers

- The data from the input device goes to the tri-state buffers. When the value in the address and control buses are correct, the buffers are enabled and data passes on the data bus.
- The CPU can then read this data. If the conditions are not right the logic block does not enable the buffers and do not place on the bus.
- The enable logic contains 8-bit address and also generates two control signals RD and IO/.

## OUTPUT DEVICE

- The design of the interface circuitry for an output device such as a computer monitor is somewhat different than for the input device.
- The design of the interface circuitry for an output device, such as a computer monitor, is somewhat different than that for the input device. Tri-state buffers are replaced by a register.
- The tri-state buffers are used in input device interfaces to make sure that one device writes data to the bus at any time.
- Since the output devices read from the bus, rather than write data to it, they don't need the buffers.
  - The data can be made available to all output devices but the devices only contains the correct address will read it in.
    - When the load logic receives the correct address and control signals, it asserts data bus. The output device can read the data from the register at its leisure while the CPU performs the other tasks.



An output device: (a) with its interface and (b) the enable logic for the registers

Some devices are used for both input and output. Personal computer and hard disk devices are falls into this category. Such a devices requires a combined interface that is essential two interfaces. A bidirectional I/O device with its interface and enable/ load logic is shown in the figure below.

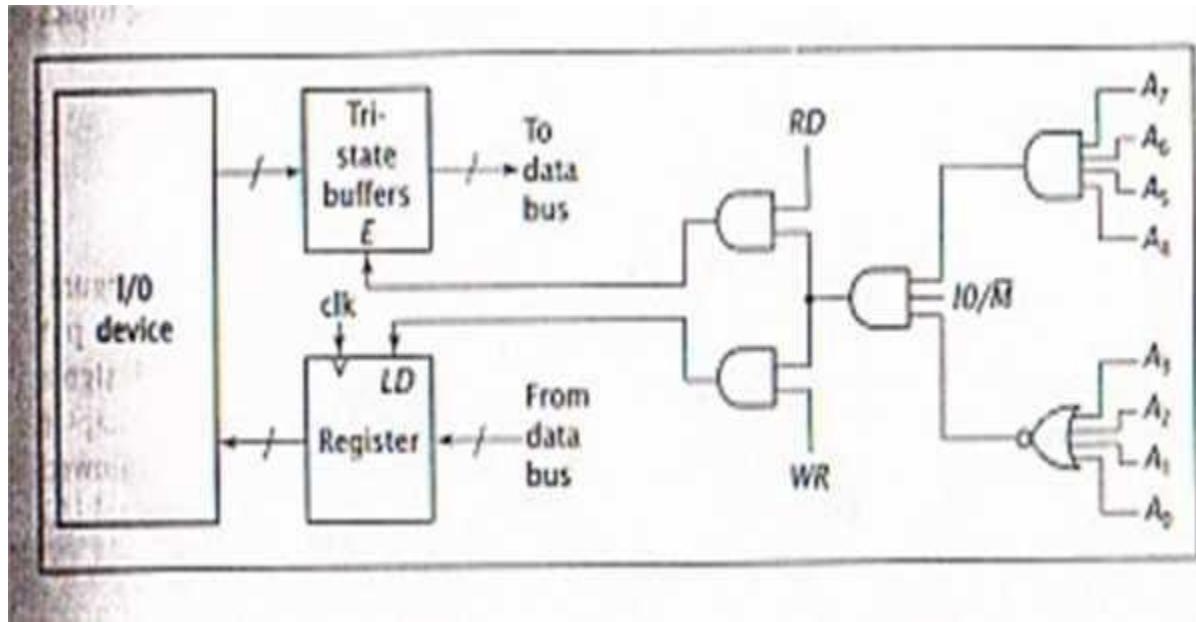
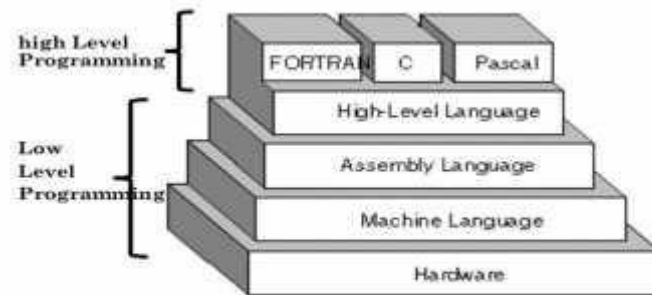


Fig: A bidirectional I/O device with its interface and enable/load logic

## 1.5 LEVELS OF PROGRAMMING LANGUAGES

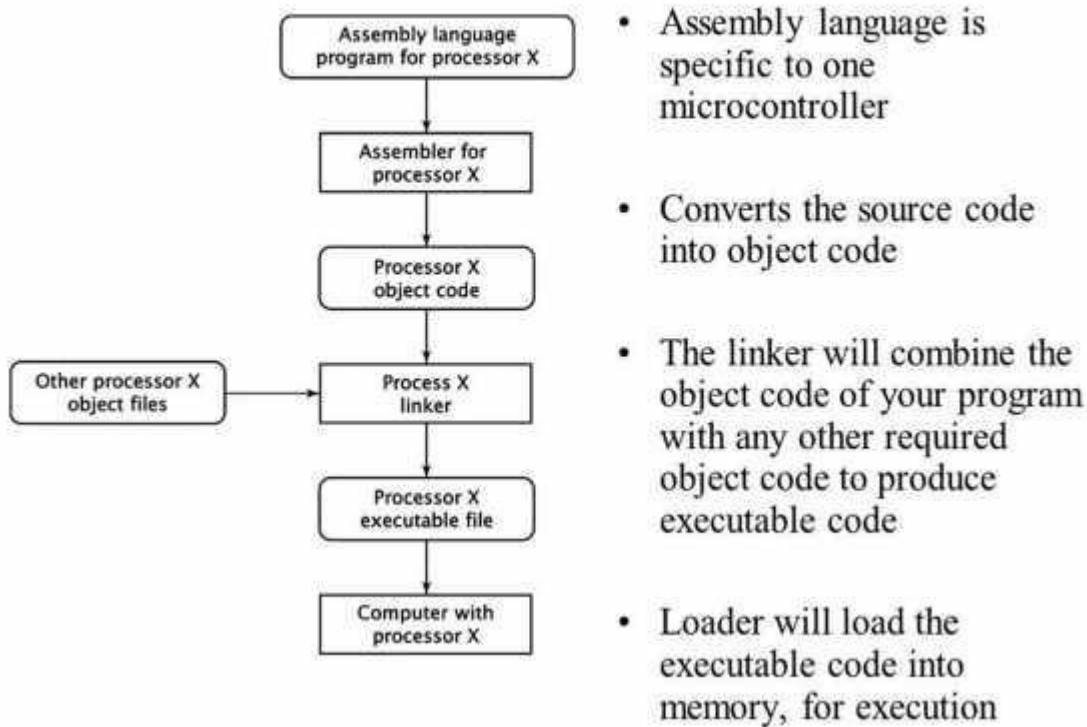
- Computer programming languages are divided into 3 categories.
  - High level language
  - Assembly level language
  - Machine level language
- **High level languages** are platform independent that is these programs can run on computers with different microprocessor and operating systems without modifications. Languages such as C++, Java and FORTRAN are high level languages.
- **Assembly languages** are at much lower level of abstraction. Each processor has its own assembly language.
- A program written in the assembly language of one processor cannot be run on a computer that has different processor so assembly languages are platform dependent.
- Unlike high level languages, instructions in assembly languages can directly manipulate the data stored in microprocessor internal components. Assembly language instructions can load the data from memory into microprocessor registers, add values, and perform many other operations.
- The lowest level of programming language is **machine level languages**. These languages contain the binary values that cause the microprocessor to perform certain operations. When microprocessor reads and executes an instruction it's a machine language instruction.

- Levels of programming languages is shown in the figure below



- Programmers don't write the programs in machine language, rather programs written in assembly or high level are converted into machine level and then executed by the microprocessor.
- High level language programs are **compiled** and assembly level language programs are assembled.
- A program written in the high level language is input to the compiler. The compiler checks to make sure every statement in the program is valid. When the program has no syntax errors the compiler finishes the compiling the program that is **source code** and generates an **object code file**.
- An object code is the machine language equivalent of source code.
- A **linker** combines the object code to any other object code. This combined code stores in the **executable file**.
- The process of converting the assembly language program to an executable form is shown the figure below.

# Assembling programs



**Fig: Assembly process for assembly language programs**

## 1.6 ASSEMBLY LANGUAGE INSTRUCTIONS:

- The simplest way to organize a computer is to have one processor register and instruction code format with two parts. The first part specifies the operation to be performed and the second specifies an address. The memory address tells the control where to find an operand in memory. This operand is read from memory and used as the data to be operated on together with the data stored in the processor register.
- Below Figure depicts this type of organization. Instructions are stored in one section of memory and data in another.
- For a memory unit with 4096 words we need 12 bits to specify an address since  $2^{12} = 4096$ . If we store each instruction code in one 16-bit memory word, we have available four bits for the operation code (abbreviated op code) to specify one out of 16 possible operations, and 12 bits to specify the address of an operand.
- The control reads a 16-bit instruction from the program portion of memory. It uses the 12-bit

address part of the instruction to read a 16-bit operand from the data portion of memory. It then executes the operation specified by the operation code.

**a) Instruction formats:**

- The basic computer has three instruction code formats, as shown in Fig below. Each format has 16 bits. The operation code (opcode) part of the instruction contains three bits and the meaning of the remaining 13 bits depends on the operation code encountered.
- A memory reference instruction uses 12 bits to specify an address and one bit to specify the addressing mode I. I is equal to 0 for direct address and to 1 for indirect address.
- The register-reference instructions are recognized by the operation code 111 with a 0 in the leftmost bit (bit 15) of the instruction. A register-reference instruction specifies an

Operation on or a test of the AC register. An operand from memory is not needed therefore the other 12 bits are used to specify the operation or test to be executed.

- Similarly, an input-output instruction does not need a reference to memory and is recognized by the operation code 111 with a 1 in the leftmost bit of the instruction. The remaining 12 bits are used to specify the type of input-output operation or test performed. The type of instruction is recognized by the computer control from the four bits in positions 12 through 15 of the instruction. If the three op code bits in positions 12 through 14 are not equal to 111, the instruction is a memory-reference type and the bit in position 15 is taken as the addressing mode I. If the 3-bit op code is equal to 111, control then inspects the bit in position 15. If this bit is 0, the instruction is a register-reference type. If the bit is 1, the instruction is an I/O type.
- The instruction for the computer is shown the table below. The symbol designation is a three letter word and represents an abbreviation intended for programmers and users. The hexadecimal code is equal to the equivalent hexadecimal number of the binary code used for the instruction. By using the hexadecimal equivalent we reduced the 16 bits of an instruction code to four digits with each hexadecimal digit being equivalent to four bits.
- A memory-reference instruction has an address part of 12 bits. The address part is denoted by three x's and stand for the three hexadecimal digits corresponding to the 12-bit address. The last bit of the instruction is designated by the symbol I. When I = 0, the last four bits of an instruction have a hexadecimal digit equivalent from 0 to 6 since the last bit is 0. When I = 1, the hexadecimal digit equivalent of the last four bits of the instruction ranges from 8 to E since the last bit is 1.
- Register-reference instructions use 16 bits to specify an operation. The leftmost four bits are always 0111, which is equivalent to hexadecimal 7. The other three hexadecimal digits give the binary equivalent of the remaining 12 bits.
- The input-output instructions also use all 16 bits to specify an operation. The last four bits are always 1111, equivalent to hexadecimal F.



Sym	Hexadecimal code		Description
AND	0xx	8xx	AND memory word to AC
ADD	1xx	9xx	ADD memory word to AC
LDA	2xx	Axx	Load memory word to AC
STA	3xx	Bxx	Store content of AC in
BUN	4xx	Cxx	Branch Unconditionally
BSA	5xx	Dxx	Branch and save return
ISZ	6xx	Exx	Increment & skip if skip
CLA	7800		Clear AC
CLE	7400		Clear E
CMA	7200		Complement AC
CME	7100		Complement E
CIR	7080		Circulate right AC & E
CIL	7040		Circulate left AC & E
INC	7020		Increment AC
SPA	7010		Skip next address if AC is
SNA	7008		Skip next address if AC is -
SZA	7004		Skip next address if AC is
SZE	7002		Skip next address if E is zero
HLT	7001		Halt computer
INP	F800		Input character to AC
OUT	F400		output character from AC
SKI	F200		Skip on input flag
SKO	F100		Skip on output flag
ION	F080		Interrupt on
IOF	F040		Interrupt off

Fig: Basic computer instructions

#### Instruction types:

- Assembly languages instructions are grouped together based on the operation they performed.
  - Data transfer instructions
  - Data operational instructions
  - Program control instructions

#### 1) Data transfer instructions:

- **Load the data from memory into the microprocessor:** These instructions copy data from memory into a microprocessor register

- **Store the data from the microprocessor into the memory:** This is similar to the load data expect data is copied in the opposite direction from a microprocessor register to memory.
- **Move data within the microprocessor:** These operations copies data from one microprocessor register to another.
- **Input the data to the microprocessor:** The microprocessor inputs the data from the input devices ex: keyboard in to one of its registers.
- **Output the data from the microprocessor:** The microprocessor copies the data from one of the registers to an input device such as digital display of a microwave oven.

## 2) Data operational instructions:

- Data operational instructions do modify their data values. They typically perform some operations using one or two data values (operands) and store result.
- Arithmetic instructions make up a large part of data operations instructions. Instructions that add, subtract, multiply, or divide values fall into this category. An instruction that increment or decrement also falls in to this category.
- Logical instructions perform basic logical operations on data. They AND, OR, or XOR two data values or complement a single value.
- Shift operations as their name implies shift the bits of a data values also comes under this category.

## 3) Program control instructions:

- Program control instructions are used to control the flow of a program. Assembly language instructions may include subroutines like in high level language program may have subroutines, procedures, and functions.
- A jump or branch instructions are generally used to go to another part of the program or subroutine.
- A microprocessor can be designed to accept interrupts. An interrupt causes the processor to stop what is doing and start other instructions. Interrupts may be software or hardware.
- One final type of control instructions is halt instruction. This instruction causes a processor to stop executing instructions such as end of a program.

## 1.7 Instruction set architecture(ISA) design:

- Designing of the instruction set is the most important in designing the microprocessor. A poor designed ISA even it is implemented well leads to bad microprocessor.
- A well designed instruction set architecture on the other hand can result in a powerful processor that can meet variety of needs.
- In designing ISA the designer must evaluate the tradeoffs in performance and such constrains issues as size and cost when designing ISA specifications.
- If the processor is to be used for general purpose computing such as personal computer it will probably require a rich set of ISA. It will need a relatively large instruction set to

perform the wide variety of tasks it must accomplish. It may also need many registers for some of these tasks.

- In contrast consider a microwave oven it require only simple ISA those need to control the oven. This issue of **completeness** of the ISA is one of the criteria in designing the processor that means the processor must have complete set of instructions to perform the task of the given application.
- Another criterion is instruction **orthogonality**. Instructions are orthogonal if they do not overlap, or perform the same function. A good instruction set minimizes the overlap between instructions.
- Another area that the designer can optimize the ISA is the **register set**. Registers have a large effect on the performance of a CPU. The CPU Can store data in its internal registers instead of memory. The CPU can retrieve data from its registers much more likely than form the memory.
- Having too few registers causes a program to make more reference to the memory thus reducing performance.

General purposes CPU have many registers since they have to process different types of programs. Intel processor has 128 general purpose registers for integer data and another 128 for floating point data. For dedicated CPU such as microwave oven having too many registers adds unnecessary hardware to the CPU without providing any benefits.

### 1.7 A RELATIVELY SIMPLE INSTRUCTION SET ARCHITECTURE:

- A relatively simple instruction set architecture describes the ISA of the simple processor or CPU.
- A simple microprocessor can access 64K ( $=2^{16}$ ) bytes of memory with each byte having 8 bits or 64K $\times$ 8 of memory. This does not mean that every computer constructed using this relatively simple CPU must have full 64K of memory. A system based on this processor can have less than memory if doesn't need the maximum 64K of memory.
- This processor inputting the data from and outputting the data to external devices such as microwave ovens keypad and display are treated as memory accesses. There are two types of input/output interactions that can design a CPU to perform.
  - Isolated I/O
  - Memory mapped I/O
- An **isolated I/O** input and output devices are treated as being separated from memory. Different instructions are used for memory and I/O.
- **Memory mapped I/O** treats input and output devices as memory locations the CPU access these I/O devices using the same instructions that it uses to access memory. For relatively simple CPU memory mapped I/O is used.
- There are three registers in ISA of this processor.
  - Accumulator (AC)

- Register R
- Zero flag (Z)

- The first accumulator is an 8bit register. Accumulator of this CPU receives the result of any arithmetic and logical operations. It also provides one of the operands for ALU instructions that use two operands. Data is loaded from memory it is loaded into the accumulator and also data stored to memory also comes from AC.
- Register R is an 8-bit general purpose register. It supplies the second operand of all two operand arithmetic and logical instructions. It also stores the final data.
- Finally, there is a 1-bit zero flag Z. Whenever an arithmetic and logical instruction is executed. If the result of the instruction is 0 then Z is set to 1 that a zero result was generated. Otherwise it is set to 0.
- The final component is the instruction set architecture for this relatively simple CPU is shown in the table below.

Instruction	Instruction Code	Operation
NOP	0000 0000	No operation
LDAC	0000 0001 $\Gamma$	$AC = M[\Gamma]$
STAC	0000 0010 $\Gamma$	$M[\Gamma] = AC$
MVAC	0000 0011	$R = AC$
MOVR	0000 0100	$AC = R$
JUMP	0000 0101 $\Gamma$	GOTO $\Gamma$
JMPZ	0000 0110 $\Gamma$	IF (Z=1) THEN GOTO $\Gamma$
JPNZ	0000 0111 $\Gamma$	IF (Z=0) THEN GOTO $\Gamma$
ADD	0000 1000	$AC = AC + R$ , If $(AC + R = 0)$ Then $Z = 1$ Else $Z = 0$
SUB	0000 1001	$AC = AC - R$ , If $(AC - R = 0)$ Then $Z = 1$ Else $Z = 0$
INAC	0000 1010	$AC = AC + 1$ , If $(AC + 1 = 0)$ Then $Z = 1$ Else $Z = 0$
CLAC	0000 1011	$AC = 0$ , $Z = 1$
AND	0000 1100	$AC = AC \wedge R$ , If $(AC \wedge R = 0)$ Then $Z = 1$ Else $Z = 0$
OR	0000 1101	$AC = AC \vee R$ , If $(AC \vee R = 0)$ Then $Z = 1$ Else $Z = 0$
XOR	0000 1110	$AC = AC \oplus R$ , If $(AC \oplus R = 0)$ Then $Z = 1$ Else $Z = 0$
NOT	0000 1111	$AC = AC'$ , If $(AC' = 0)$ Then $Z = 1$ Else $Z = 0$

- The LDAC, STAC, JUMP, JMPZ AND JPNZ instructions all require a 16-bit memory address represented by the symbol  $\Gamma$ .
- Since each byte of memory is 8-bit wide these instructions requires 3 bytes in memory. The first byte contains the opcode for the instruction and the remaining 2 bytes for the address.

- The instructions of this instruction set architecture can be grouped in to 3 categories
  - Data transfer instructions
  - Program control instructions
  - Data operational instructions
- The NOP, LDAC, STAC, MVAC or MOVR instructions are **data transfer instructions**. The NOP operation performs no operation. The LDAC operation loads the data from the memory it reads the data from the memory location  $M[\Gamma]$ . The STAC performs opposite, copying data from AC to the memory location  $\Gamma$ .
- The MOVAC instruction copies data from R to AC and MOVR instruction copies the data from R to AC.
- There are three **program control instructions** in the instruction set: JUMP, JUPZ and JPNZ. The JUMP is the unconditional it always jumps to the memory location  $\Gamma$ . For example JUMP 1234H instruction always jump to the memory location 1234H. The JUMP instruction uses the immediate addressing mode since the jump address is specified in the instruction. The other two program control instructions JUPZ and JPNZ are conditional. If their conditions are met  $Z=0$  for JUPZ and  $Z=1$  for JPNZ these instructions jump to the memory location  $\Gamma$ .
- Finally data operations instructions are ADD, SUB, INAC and CLAC instructions are arithmetic instructions. The ADD instructions add the content of AC and R and store the result again in AC. The instruction also set the zero flag  $Z=1$  if sum is zero or  $Z=0$  if the sum is non zero value. The SUB operation performs the same but it subtracts the AC and R.
- INAC instruction adds 1 to the AC and sets Z to its proper value. The CLAC instruction always makes  $Z=1$  because it clears the AC value that is AC to 0.
- The last four data operation instructions are logical instructions as the name imply the AND, OR, and XOR instructions logically AND, OR and XOR the values AC and R and store the result in AC. The NOT instruction sets AC to its bitwise complement.

## 1.8 RELATIVELY SIMPLE COMPUTER:

- In this relatively simple computer we put all the hard ware components of the computer together in one system. This computer will have 8K ROM starting at address 0 followed by 8K RAM. It also has a memory mapped bidirectional I/O port at address 8000H.
- First let us look at the CPU since it uses 16 bit address labeled A15 through A0. System bus via pins through D7 to D0. The CPU also has the two control lines READ and WRITE.
- Since it uses the memory mapped I/O it does not need a control signal such as  $\overline{M}$ . The relatively simple computer is shown in the figure below. It only contains the CPU details. Each part will be developed in the design.

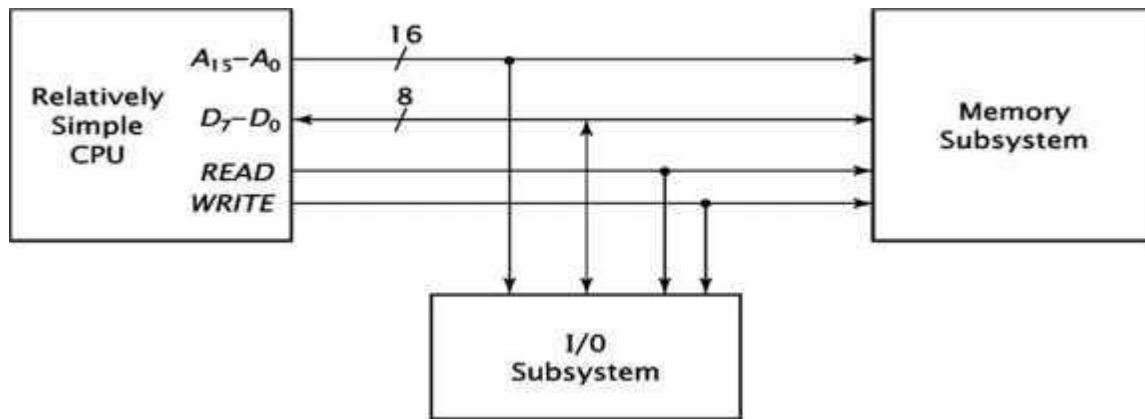


Fig: A relatively simple computer: CPU details only

- To access a memory chip the processor must supply an address used by the chip. An 8K memory chip has  $2^{13}$  internal memory locations it has 13bit address input to select one of these locations. The address input of each chip receives CPU address bits  $A_{12}$  to  $A_0$  from system address bus. The remaining three bits  $A_{15}$ ,  $A_{14}$ , and  $A_{13}$  will be used to select one of the memory chips.
- The address range of ROM and RAM is

## UNIT- II

### ORGANIZATION OF A COMPUTER

Register transfer: Register transfer language, register transfer, bus and memory transfers, arithmetic micro operations, logic micro operations, And shift micro operations; Control unit: Control memory, address sequencing, micro program example, and design of control unit.

#### Register Transfer and Microoperations

##### 2.1 Register Transfer Language

- A digital system is an interconnection of digital hardware module. Digital systems varies in size and complexity from a few integrated circuits to a complex of interconnected and interacting digital computers.
- Digital system design invariably uses a modular approach. The modules are constructed from such digital components as registers, decoders, arithmetic elements, and control logic.
- The various modules are interconnected with common data and control paths to form a digital computer system.
- Digital modules are best defined by the registers they contain and the operations that are performed on the data stored in them. The operations executed on data stored in registers are called microoperations.
- A microoperation is an elementary operation performed on the information stored in one or more registers.
- The result of the operation may replace the previous binary information of a register or may be transferred to another register. Examples of microoperations are shift, count, clear, and load.

The internal hardware organization of a digital computer is best defined by specifying:

1. The set of registers it contains and their function.
2. The sequence of microoperations performed on the binary information stored in the registers.
3. The control that initiates the sequence of microoperations.

- The symbolic notation used to describe the microoperation transfers among registers is called a **register transfer language**.
- The term "register transfer" implies the availability of hardware logic circuits that can perform a stated microoperation and transfer the result of the operation to the same or another register.
- The word "language" is borrowed from programmers, who apply this term to programming languages. A programming language is a procedure for writing symbols to specify a given computational process.
- A register transfer language is a system for expressing in symbolic form the microoperation sequences among the registers of a digital module.
- It is a convenient tool for describing the internal organization of digital computers in

concise and precise manner. It can also be used to facilitate the design process of digital systems.

- The register transfer language adopted here is believed to be as simple as possible, so it should not take very long to memorize.
- To define symbols for various types of microoperations, and at the same time, describe associated hardware that can implement the stated microoperations.
- Other symbology in use can easily be learned once this language has become familiar, for most of the differences between register transfer languages consist of variations in detail rather than in overall purpose.

## 2.2 Register Transfer

- Computer registers are designated by capital letters (sometimes followed by numerals) to denote the function of the register. For example, MAR, PC, IR. The individual flip-flops
- Figure 1 shows the representation of registers in block diagram form. The most common way to represent a register is by a rectangular box with the name of the register inside, as in Fig. 1(a) the individual bits can be distinguished as in (b). The numbering of bits in a 16-bit register can be marked on top of the box as shown in (c). A 16-bit register is partitioned into two parts in (d). Bits 0 through 7 are assigned the symbol L (for low byte) and bits 8 through 15 are assigned the symbol H (for high byte). The name of the 16-bit register is PC. The symbol PC(0-7) or PC(L) refers to the low-order byte and PC(8-15) or PC(H) to the high-order byte.
- Information transfer from one register to another is designated in symbolic form by means of a replacement operator.
- The statement  $R2 \leftarrow R1$  denotes a transfer of the content of register R1 into register R2.
- It designates a replacement of the content of R2 by the content of R1. By definition, the content of the source register R1 does not change after the transfer.
- A statement that specifies a register transfer implies that circuits are available from the outputs of the source register to the inputs of the destination register and that the destination register has a parallel load capability.
- The transfer to occur only under a predetermined control condition. This can be shown by means of an if-then statement.

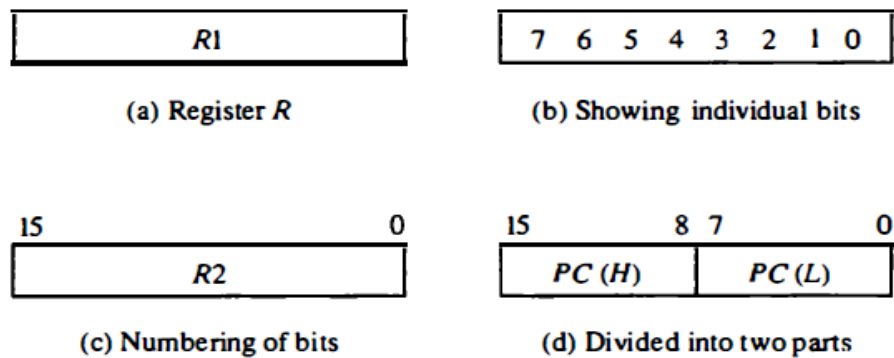
If ( $P = 1$ ) then ( $R2 \leftarrow R1$ )

Where P is a control signal generated in the control section. It is sometimes convenient to separate the control variables from the register transfer operation by specifying a control function. A control function is a Boolean variable that is equal to 1 or 0. The control function is included in the statement as follows:

P:  $R2 \leftarrow R1$



Figure 1 Block diagram of register.



The control condition is terminated with a colon. It symbolizes the requirement that the transfer operation be executed by the hardware only if  $P = 1$ .

Every statement written in a register transfer notation implies a hardware construction for implementing the transfer.

- Above figure shows the block diagram that depicts the transfer from *R1* to *R2*. The *n* outputs of register *R1* are connected to the *n* inputs of register *R2*.
- The basic symbols of the register transfer notation are listed in Table 4-1. Registers are denoted by capital letters, and numerals may follow the letters.

$T: R2 \leftarrow R1, R1 \leftarrow R2$

The statement denotes an operation that exchanges the contents of two registers during one common clock pulse provided that  $T = 1$ . This simultaneous operation is possible with registers that have edge-triggered flip-flops.

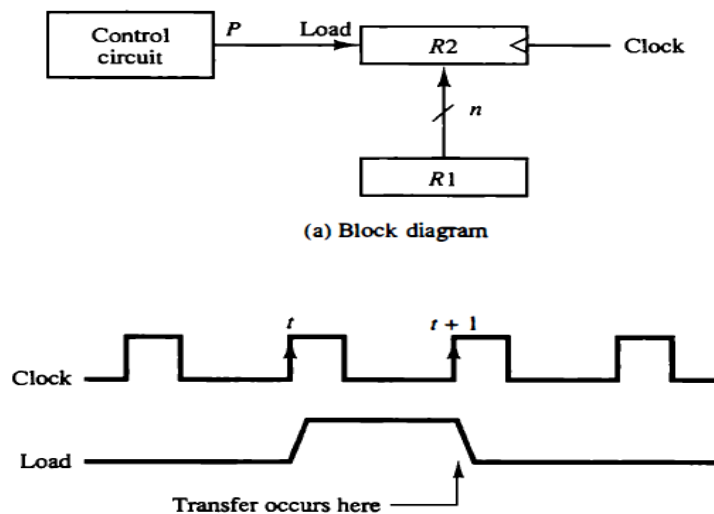


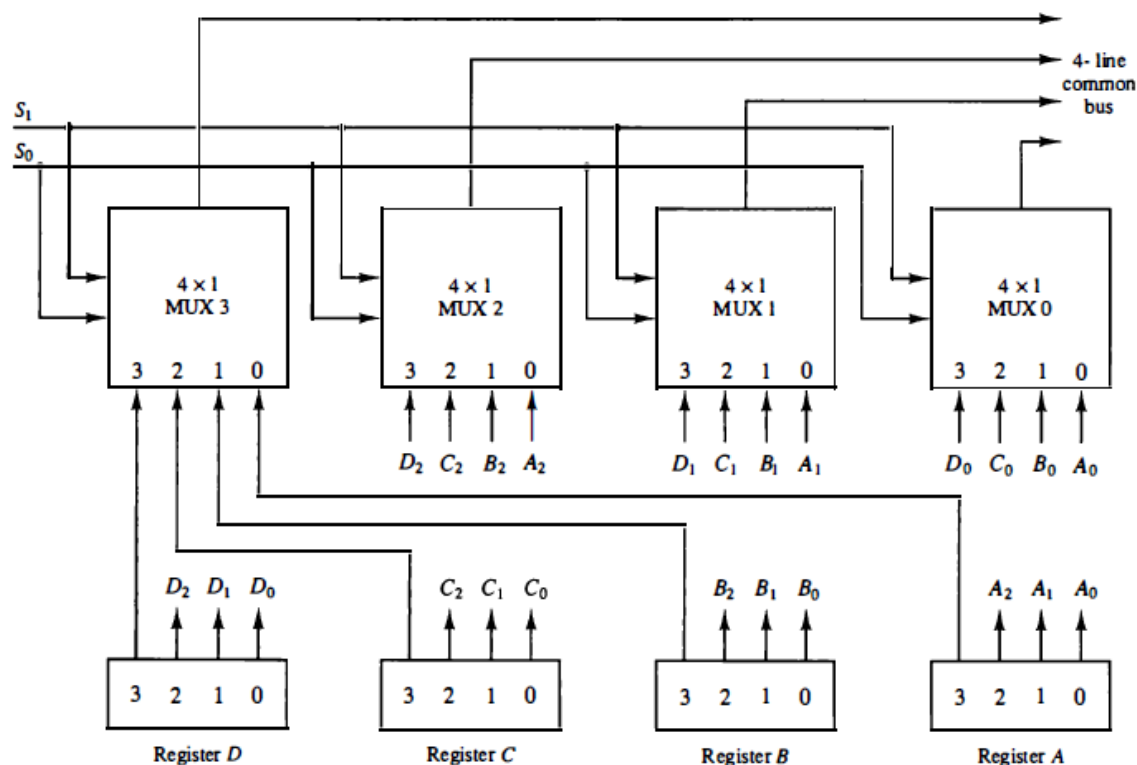
TABLE 1 Basic symbols for register Transfers

Symbol	Description	Examples
Letters and numerals	Denotes a register	MAR,R2
Parenthesis( )	Denotes a part of registers	R290-70,R2(L)
Arrow $\leftarrow$	Denotes transfer of information	$R2 \leftarrow R1$
Comma ,	Separates two microoperations	$R2 \leftarrow R1, R1 \leftarrow R2$

### 2.3 Bus and Memory Transfers

- A typical digital computer has many registers, and paths must be provided to transfer information from one register to another. The number of wires will be excessive if separate lines are used between each register and all other registers in the system.
- A more efficient scheme for transferring information between registers in a multiple-register configuration is a common bus system.
- A bus structure consists of a set of common lines, one for each bit of a register, through which binary information is transferred one at a time. Control signals determine which register is selected by the bus during each particular register transfer.
- The diagram shows that the bits in the same significant position in each register are connected to the data inputs of one multiplexer to form one line of the bus.
- MUX 0 multiplexes the four 0 bits of the registers, MUX 1 multiplexes the four 1 bits of the registers, and similarly for the other two bits.

Figure 3: Bus systems for four registers



- The two selection lines  $S_1$  and  $S_0$  are connected to the selection inputs of all four multiplexers. The selection lines choose the four bits of one register and transfer them into the four-line common bus.
- When  $S_1S_0 = 00$ , the 0 data inputs of all four multiplexers are selected and applied to the outputs that form the bus.
- This causes the bus lines to receive the content of register A since the outputs of this register are connected to the 0 data inputs of the multiplexers. Similarly, register B is selected if  $S_1S_0 = 01$ , and so on.

Table 2 shows the register that is selected by the bus for each of the four possible binary value of the selection lines.

Table 2 function table for Bus of fig 3

$S_1$	$S_0$	Registers selected
0	0	A
0	1	B
1	0	C
1	1	D

- In general, a bus system will multiplex  $k$  registers of  $n$  bits each to produce an  $n$ -line common bus.
- The number of multiplexers needed to construct the bus is equal to  $n$ , the number of bits in each register. The size of each multiplexer must be  $k \times 1$  since it multiplexes  $k$  data lines. For example, a common bus for eight registers of 16 bits each requires 16 multiplexers, one for each line in the bus.
- Each multiplexer must have eight data input lines and three selection lines to multiplex one significant bit in the eight registers.
- The transfer of information from a bus into one of many destination registers can be accomplished by connecting the bus lines to the inputs of all destination registers and activating the load control of the particular destination register selected.
- The symbolic statement for a bus transfer may mention the bus or its presence may be implied in the statement. When the bus is included in the statement, the register transfer is symbolized as follows:

$BUS \leftarrow C,$

$R1 \leftarrow BUS$

The content of register C is placed on the bus, and the content of the bus is loaded into register R1 by activating its load control input.

If the bus is known to exist in the system, it may be convenient just to show the direct transfer.

$R1 \leftarrow C$

From this statement the designer knows which control signals must be activated to produce the transfer through the bus.

## Three state bus buffers

- A bus system can be constructed with three-state gates instead of multiplexers. A three-state gate is a digital circuit that exhibits three states. Two of the states are signals equivalent to logic 1 and 0 as in a conventional gate. The third state is a high-impedance state.
- The high-impedance state behaves like an open circuit, which means that the output is disconnected and does not have logic significance. Three-state gates may perform any conventional logic, such as AND or NAND.
- However, the one most commonly used in the design of a bus system is the buffer gate.
- The graphic symbol of a three-state buffer gate is shown in Fig 4. It is distinguished from a normal buffer by having both a normal input and a control input. The control input determines the output state.
- The construction of a bus system with three-state buffers is demonstrated in Fig. 5. To construct a common bus for four registers of  $n$  bits each using three-state buffers, we need  $n$  circuits with four buffers in each as shown in Fig. 5. Each group of four buffers receives one significant bit from the four registers. Each common output produces one of the lines for the common bus for a total of  $n$  lines. Only one decoder is necessary to select between the four registers.

Fig 4: Graphic symbol for 3 state buffers

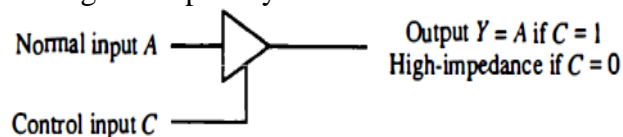
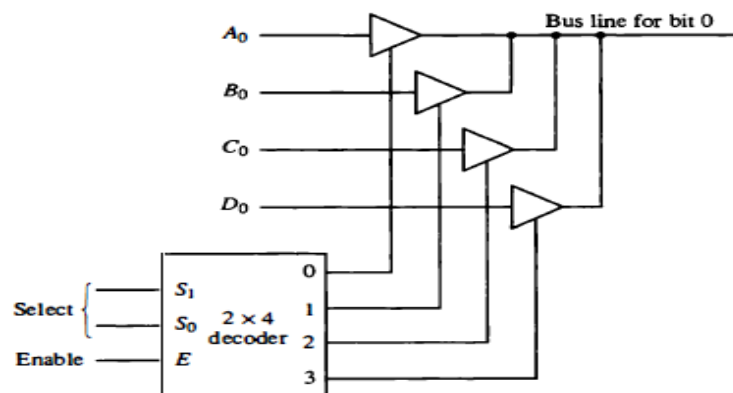


Fig 5: Bus line with 3 state buffer



## Memory Transfer

- The operation of a memory unit was described in Sec. 2-7. The transfer of information from a memory word to the outside environment is called a read operation. The transfer of new information to be stored into the memory is called a write operation.
- A memory word will be symbolized by the letter  $M$ . The particular memory word among the many available is selected by the memory address during the transfer. It is necessary

to specify the address of M when writing memory transfer operations. This will be done by enclosing the address in square brackets following the letter M. Consider a memory unit that receives the address from a register, called the address register, symbolized by AR. The data are transferred to another register, called the data register, symbolized by DR. The read operation can be stated as follows:

Read:  $DR \leftarrow [AR]$

This causes a transfer of information into DR from the memory word M selected by the address in AR. The write operation transfers the content of a data register to a memory word M selected by the address. Assume that the input data are in register R1

$R3 \leftarrow R1 + \bar{R2} + 1$

R2 is the symbol for the 1's complement of R2. Adding 1 to the 1's complement produces the 2's complement. Adding the contents of R1 to the 2's complement of R2 is equivalent to  $R1 - R2$ .

**TABLE 3 Arithmetic Microoperations**

Symbolic designation	Description
$R3 \leftarrow R1 + R2$	Contents of R1 plus R2 transferred to R3
$R3 \leftarrow R1 - R2$	Contents of R1 minus R2 transferred to R3
$R2 \leftarrow \bar{R2}$	Complement the contents of R2 (1's complement)
$R2 \leftarrow \bar{R2} + 1$	2's complement the contents of R2 (negate)
$R3 \leftarrow R1 + \bar{R2} + 1$	R1 plus the 2's complement of R2 (subtraction)
$R1 \leftarrow R1 + 1$	Increment the contents of R1 by one
$R1 \leftarrow R1 - 1$	Decrement the contents of R1 by one

- The increment and decrement microoperations are symbolized by plus one and minus-one operations, respectively. These microoperations are implemented with a combinational circuit or with a binary up-down counter.
- The arithmetic operations of multiply and divide are not listed in Table 3. These two operations are valid arithmetic operations but are not included in the basic set of microoperations.
- The only place where these operations can be considered as microoperations is in a digital system, where they are implemented by means of a combinational circuit.

## 2.4 Arithmetic micro operations

### Binary Adder

- To implement the add microoperation with hardware, we need the registers that hold the data and the digital component that performs the arithmetic addition. The digital circuit that forms the arithmetic sum of two bits and a previous carry is called a full-adder.

- The digital circuit that generates the arithmetic sum of two binary numbers of any length is called a binary adder.
- The binary adder is constructed with full-adder circuits connected in cascade, with the output carry from one full-adder connected to the input carry of the next full-adder. Figure 4-6 shows the interconnections of four full-adders (FA) to provide a 4-bit binary adder.

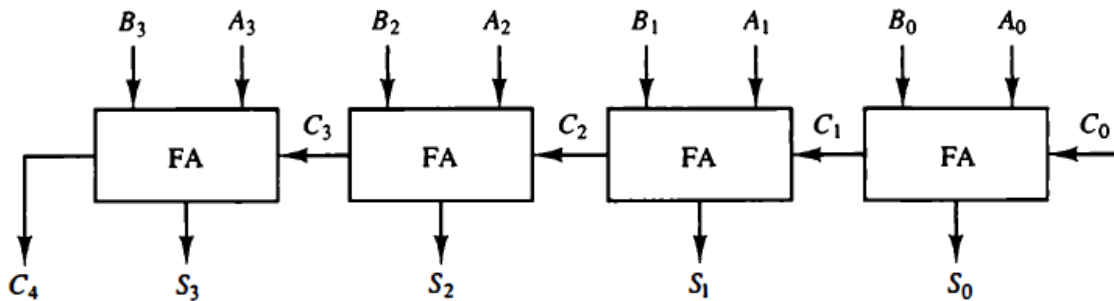


Fig 6: binary adder

### Binary Adder-Subtractor

- The subtraction of binary numbers can be done most conveniently by means of complements as discussed in Sec. 3-2. Remember that the subtraction  $A - B$  can be done by taking the 2's complement of  $B$  and adding it to  $A$ .
- The 2's complement can be obtained by taking the 1's complement and adding one to the least significant pair of bits. The 1's complement can be implemented with inverters and a one can be added to the sum through the input carry.
- The addition and subtraction operations can be combined into one common circuit by including an exclusive-OR gate with each full-adder. A 4-bit adder-subtractor circuit is shown in Fig. 4-7.

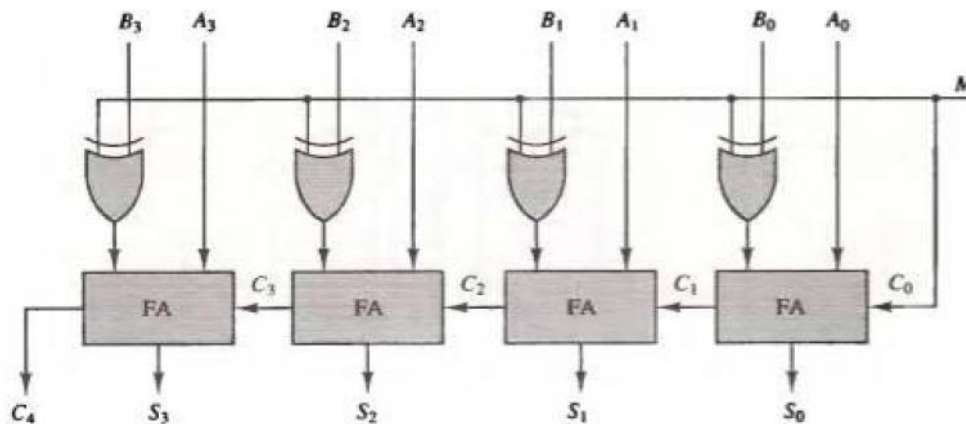


Fig7: 4 bit adder- subtractor

### Binary Incrementer

- The increment microoperation adds one to a number in a register. For example, if a 4-bit register has a binary value 0110, it will go to 0111 after it is incremented.

- This microoperation is easily implemented with a binary counter every time the count enable is active, the clock pulse transition increments the content of the register by one.
- There may be occasions when the increment microoperation must be done with a combinational circuit independent of a particular register. Binary incrementer.
- The increment microoperation adds one to a number in a register. For example, if a 4-bit register has a binary value 0110, it will go to 0111 after it is incremented. This microoperation is easily implemented with a binary counter.
- The diagram of a 4-bit combinational circuit incrementer is shown in Fig. 8.

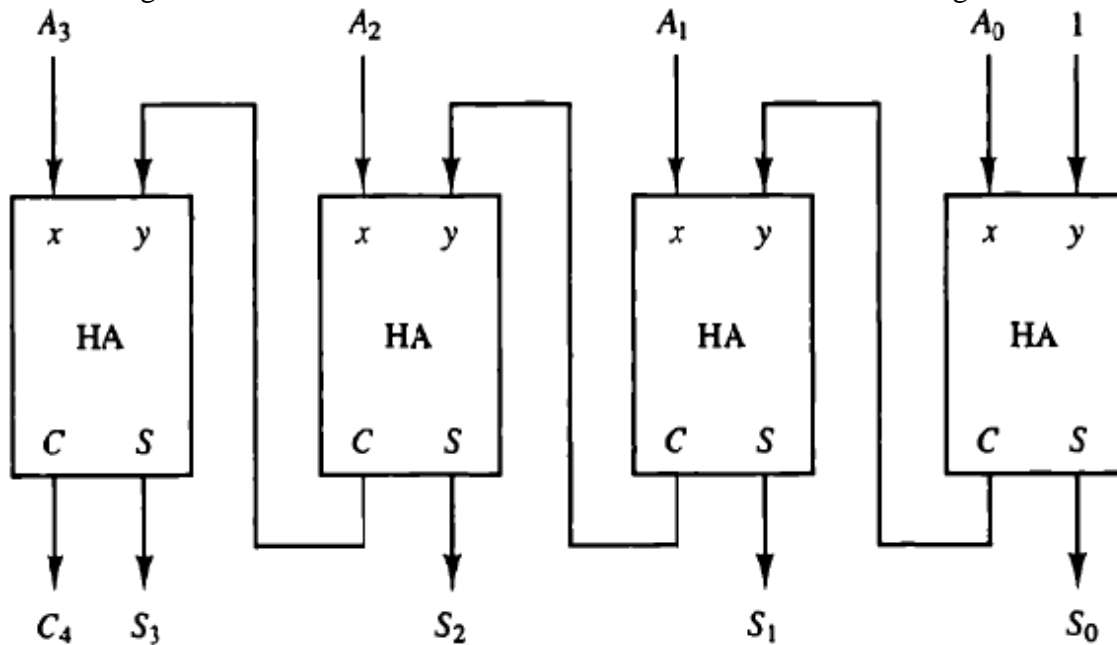


Fig 8: 4- bit binary incrementer

### Arithmetic Circuit

- The arithmetic microoperations listed in Table 4-3 can be implemented in one composite arithmetic circuit. The basic component of an arithmetic circuit is the parallel adder.
- By controlling the data inputs to the adder, it is possible to obtain different types of arithmetic operations. The diagram of a 4-bit arithmetic circuit is shown in Fig. 9. The output of the binary adder is calculated from the following arithmetic sum:

$$D = A + Y + C_{in}$$

Where A is the 4-bit binary number at the X inputs and Y is the 4-bit binary number at the Y inputs of the binary adder.  $C_{in}$  is the input carry, which can be equal to 0 or 1. Note that the symbol + in the equation above denotes an arithmetic plus. By controlling the value of Y with the two selection inputs S1 and S0 and making  $C_{in}$  equal to 0 or 1, it is possible to generate the eight arithmetic microoperations listed in Table 4.

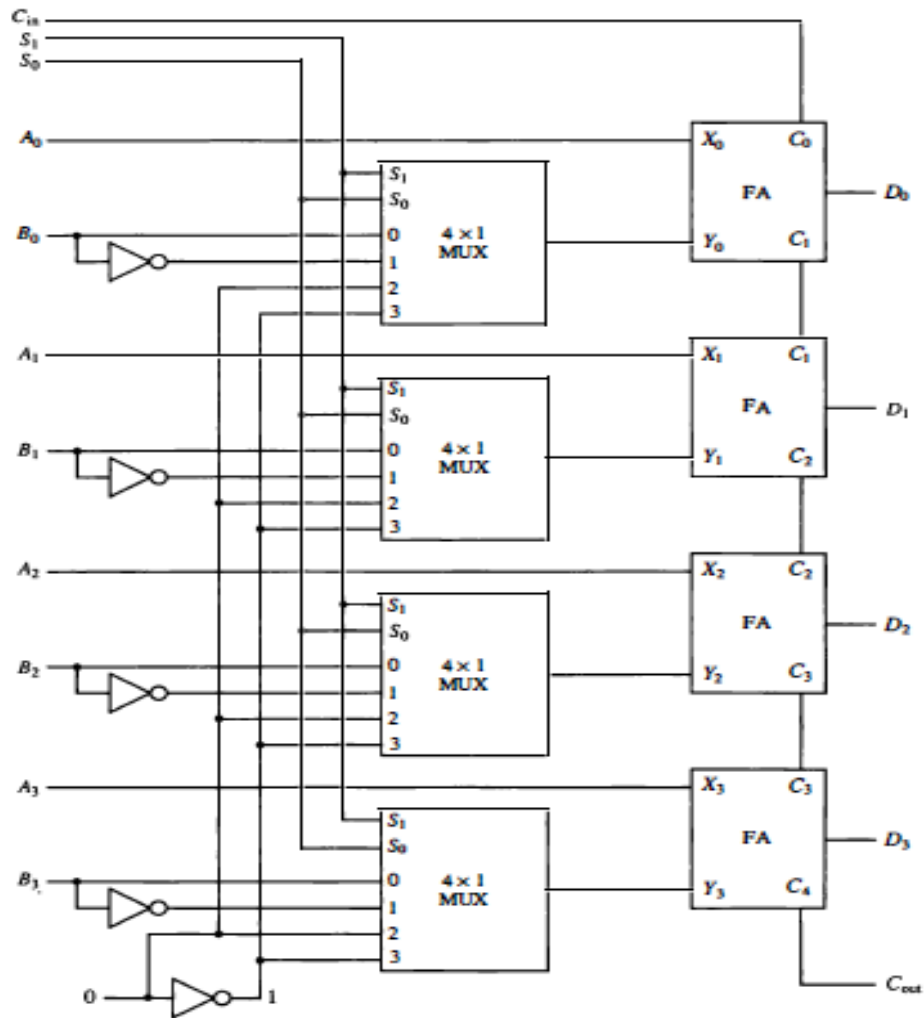


Fig 9: 4- bit arithmetic circuit

**TABLE 4** Arithmetic Circuit Function Table

Select			Input $Y$	Output $D = A + Y + C_{in}$	Microoperation
$S_1$	$S_0$	$C_{in}$			
0	0	0	$B$	$D = A + B$	Add
0	0	1	$B$	$D = A + B + 1$	Add with carry
0	1	0	$\bar{B}$	$D = A + \bar{B}$	Subtract with borrow
0	1	1	$\bar{B}$	$D = A + \bar{B} + 1$	Subtract
1	0	0	0	$D = A$	Transfer $A$
1	0	1	0	$D = A + 1$	Increment $A$
1	1	0	1	$D = A - 1$	Decrement $A$
1	1	1	1	$D = A$	Transfer $A$

### 3 Logic Microoperations



Logic microoperations specify binary operations for strings of bits stored in registers. These operations consider each bit of the register separately and treat them as binary variables. For example, the exclusive-OR microoperation with the contents of two registers R 1 and R2 is symbolized by the statement

$$P: R1 \leftarrow R1 \oplus R2$$

It specifies a logic microoperation to be executed on the individual bits of the registers provided that the control variable  $P = 1$ . As a numerical example, assume that each register has four bits. Let the content of R1 be 1010 and the content of R2 be 1 100. The exclusive-OR microoperation stated above symbolizes the following logic computation:

1010 Content of R 1

1 100 Content of R2

0110 Content of R 1 after  $P = 1$

The content of R 1 , after the execution of the microoperation, is equal to the bit-by-bit exclusive-OR operation on pairs of bits in R2 and previous values of R 1 . The logic microoperations are seldom used in scientific computations, but they are very useful for bit manipulation of binary data and for making logical decisions.

- Special symbols will be adopted for the logic microoperations OR, AND, and complement, to distinguish them from the corresponding symbols used to express Boolean functions.
- The symbol  $\vee$  will be used to denote an OR microoperation and the symbol  $\wedge$  to denote an AND microoperation. The complement microoperation is the same as the 1's complement and uses a bar on top of the symbol that denotes the register name.
  - By using different symbols, it will be possible to differentiate between a logic microoperation and a control (or Boolean) function. Another reason for adopting two sets of symbols is to be able to distinguish the symbol  $+$  , when used to symbolize an arithmetic plus, from a logic OR operation. Although the  $+$  symbol has two meanings, it will be possible to distinguish between them by noting where the symbol occurs.

$$P + Q: R1 \quad R2 + R3, R4 \quad R5 \vee R6$$

### List of Logic Microoperations

- There are 16 different logic operations that can be performed with two binary variables.
- They can be determined from all possible truth tables obtained with two binary variables as shown in Table 5.
- In this table, each of the 16 columns F0 through F15 represents a truth table of one possible Boolean function for the two variables  $x$  and  $y$ . Note that the functions are determined from the 16 binary combinations that can be assigned to  $F$  .
- The 16 Boolean functions o f two variables  $x$  and  $y$  are expressed in algebraic form in the first column of Table 6. The 16 logic microoperations are derived from these functions by replacing variable  $x$  by the binary content of register A and variable  $y$  by the binary content of register B

**TABLE 5** Truth Tables for 16 Functions of Two Variables

$x$	$y$	$F_0$	$F_1$	$F_2$	$F_3$	$F_4$	$F_5$	$F_6$	$F_7$	$F_8$	$F_9$	$F_{10}$	$F_{11}$	$F_{12}$	$F_{13}$	$F_{14}$	$F_{15}$
0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
0	1	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1
1	0	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1
1	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1

**TABLE 6** Sixteen Logic Microoperations

Boolean function	Microoperation	Name
$F_0 = 0$	$F \leftarrow 0$	Clear
$F_1 = xy$	$F \leftarrow A \wedge B$	AND
$F_2 = xy'$	$F \leftarrow A \wedge \overline{B}$	
$F_3 = x$	$F \leftarrow A$	Transfer $A$
$F_4 = x'y$	$F \leftarrow \overline{A} \wedge B$	
$F_5 = y$	$F \leftarrow B$	Transfer $B$
$F_6 = x \oplus y$	$F \leftarrow A \oplus B$	Exclusive-OR
$F_7 = x + y$	$F \leftarrow A \vee B$	OR
$F_8 = (x + y)'$	$F \leftarrow \overline{A \vee B}$	NOR
$F_9 = (x \oplus y)'$	$F \leftarrow \overline{A \oplus B}$	Exclusive-NOR
$F_{10} = y'$	$F \leftarrow \overline{B}$	Complement $B$
$F_{11} = x + y'$	$F \leftarrow A \vee \overline{B}$	
$F_{12} = x'$	$F \leftarrow \overline{A}$	Complement $A$
$F_{13} = x' + y$	$F \leftarrow \overline{A} \vee B$	
$F_{14} = (xy)'$	$F \leftarrow \overline{A \wedge B}$	NAND
$F_{15} = 1$	$F \leftarrow \text{all 1's}$	Set to all 1's

## Hardware Implementation

- The hardware implementation of logic microoperations requires that logic gates be inserted for each bit or pair of bits in the registers to perform the required logic function.
- Although there are 16 logic microoperations, most computers use only four-AND, OR, XOR (exclusive-OR), and complement from which all others can be derived.
- Figure 10 shows one stage of a circuit that generates the four basic logic microoperations.
- It consists of four gates and a multiplexer. Each of the four logic operations is generated through a gate that performs the required logic. The outputs of the gates are applied to the data inputs of the multiplexer.

## Some Applications

Logic microoperations are very useful for manipulating individual bits or a portion of a word stored in a register. They can be used to change bit values, delete a group of bits, or insert new bit values into a register.

The following examples show how the bits of one register (designated by  $A$ ) are manipulated by logic microoperations as a function of the bits of another register (designated by  $B$ ). In a typical

application, register A is a processor register and the bits of register B constitute a logic operand extracted from memory and placed in register B .

The selective-set operation sets to 1 the bits in register A where there are corresponding 1's in register B. It does not affect bit positions that have 0's in B. The following numerical example clarifies this operation:

1010 A before  
1100 B (logic operand)  
1110 A after

The two leftmost bits of B are 1's, so the corresponding bits of A are set to 1. One of these two bits was already set and the other has been changed from 0 to 1. The two bits of A with corresponding 0's in B remain unchanged. The example above serves as a truth table since it has all four possible combinations of two binary variables. From the truth table we note that the bits of A after the operation are obtained from the logic-OR operation of bits in B and previous values of A. Therefore, the OR microoperation can be used to selectively set bits of a register.

The selective-complement operation complements bits in A where there are selective-clear corresponding 1's in B. It does not affect bit positions that have 0's in B. For example:

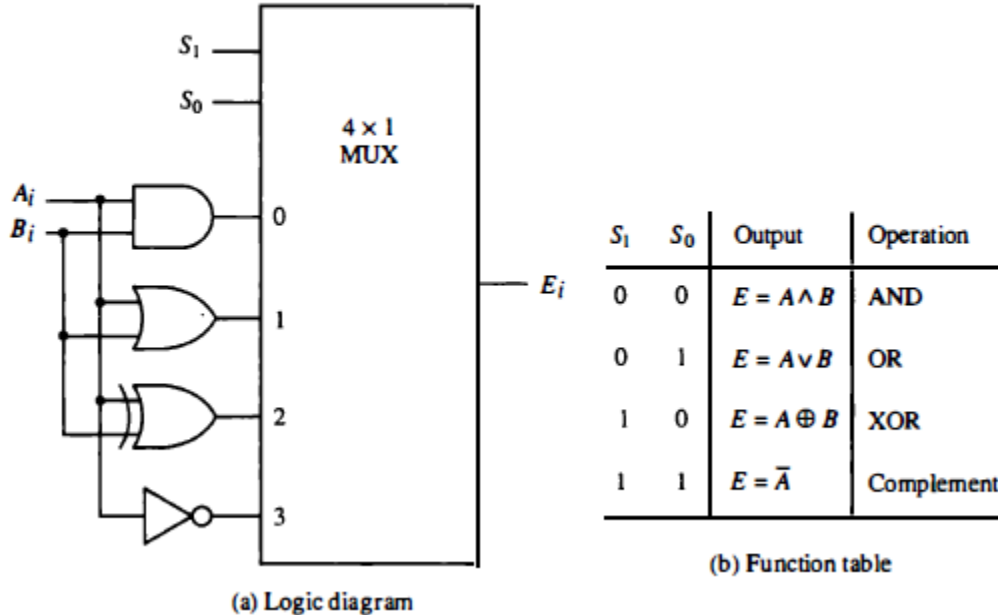
1010 A before  
1100 B (logic operand)  
0110 A after

Again the two leftmost bits of B are 1's, so the corresponding bits of A are complemented. This example again can serve as a truth table from which one can deduce that the selective-complement operation is just an exclusive-OR microoperation. Therefore, the exclusive-OR microoperation can be used to selectively complement bits of a register. The selective-clear operation clears to 0 the bits in A only where there are corresponding 1's in B. For example:

1010 A before  
1100 B (logic operand)  
0010 A after

Again the two leftmost bits of B are 1's, so the corresponding bits of A are cleared to 0. One can deduce that the Boolean operation performed on the individual bits is  $A \wedge B'$ . The corresponding logic microoperation is  $A \wedge B'$ .

Figure 10 One stage of logic circuit.



The mask operation is similar to the selective-clear operation except that the bits of A are cleared only where there are corresponding 0's in B. The mask operation is an AND micro operation as seen from the following numerical example:

1010 A before

1 100 B (logic operand)

1000 A after masking

The two rightmost bits of A are cleared because the corresponding bits of B are 0's. The two leftmost bits are left unchanged because the corresponding bits of B are 1's. The mask operation is more convenient to use than the selective clear operation because most computers provide an AND instruction, and few provide an instruction that executes the microoperation for selective-clear. The insert operation inserts a new value into a group of bits. This is done by first masking the bits and then ORing them with the required value. For example, suppose that an A register contains eight bits, 0110 1010.

To replace the four leftmost bits by the value 1001 we first mask the four unwanted bits:

0110 1010 A Before

0000 1 1 1 1 B(mask)

0000 1010 A after masking

and then insert the new value:

0000 1010 A before

1001 0000 B (insert)

1001 1010 A after insertion

The mask operation is an AND microoperation and the insert operation is an OR microoperation.

The clear operation compares the words in A and B and produces an all 0's result if the two numbers are equal. This operation is achieved by an exclusive-OR microoperation as shown by the following example:

1010 A

1010 B

0000 A  $\leftarrow$  A + B

When A and B are equal, the two corresponding bits are either both 0 or both

1. In either case the exclusive-OR operation produces a 0. The all-0's result is then checked to determine if the two numbers were equal.

## 2.5 Shift Microoperations

- Shift microoperations are used for serial transfer of data. They are also used in conjunction with arithmetic, logic, and other data-processing operations.
- The contents of a register can be shifted to the left or the right. At the same time that the bits are shifted, the first flip-flop receives its binary information from the serial input. During a shift-left operation the serial input transfers a bit into the rightmost position. During a shift-right operation the serial input transfers a bit into the leftmost position.
- The information transferred through the serial input determines the type of shift. There are three types of shifts: logical, circular, and arithmetic.
- A logical shift is one that transfers 0 through the serial input. We will adopt the symbols shl and shr for logical shift-left and shift-right microoperations. For example:

$R1 \leftarrow \text{shl } R1$

$R2 \leftarrow \text{shr } R2$

are two microoperations that specify a 1-bit shift to the left of the content of register R 1 and a 1-bit shift to the right of the content of register R2. The symbolic notation for the shift microoperations is shown in table 7.

**TABLE 7** Shift Microoperations

Symbolic designation	Description
$R \leftarrow \text{shl } R$	Shift-left register <i>R</i>
$R \leftarrow \text{shr } R$	Shift-right register <i>R</i>
$R \leftarrow \text{cil } R$	Circular shift-left register <i>R</i>
$R \leftarrow \text{cir } R$	Circular shift-right register <i>R</i>
$R \leftarrow \text{ashl } R$	Arithmetic shift-left <i>R</i>
$R \leftarrow \text{ashr } R$	Arithmetic shift-right <i>R</i>

- An arithmetic shift is a microoperation that shifts a signed binary number to the left or right. An arithmetic shift-left multiplies a signed binary number by 2.
- An arithmetic shift-right divides the number by 2. Arithmetic shifts must leave the sign bit unchanged because the sign of the number remains the same when it is multiplied or divided by 2. The leftmost bit in a register holds the sign bit, and the remaining bits hold the number.



Figure 11 Arithmetic shift right.

If  $V_s = 0$ , there is no overflow, but if  $V_s = 1$ , there is an overflow and a sign reversal after the shift.  $V_s$  must be transferred into the overflow flip-flop with the same clock pulse that shifts the register.

$$V_s = K_{n-1} \oplus K_{n-2}$$

### Hardware Implementation

A possible choice for a shift unit would be a bidirectional shift register with parallel load. Information can be transferred to the register in parallel and then shifted to the right or left. In this type of configuration, a clock pulse is needed for loading the data into the register, and another pulse is needed to initiate the shift. In a processor unit with many registers it is more efficient to implement the shift operation with a combinational circuit. In this way the content of a register that has to be shifted is first placed onto a common bus whose output is connected to the combinational shifter, and the shifted number is then loaded back into the register. This requires only one clock pulse for loading the shifted value into the register. A combinational circuit shifter can be constructed with multiplexers as shown in Fig.12. The 4-bit shifter has four data inputs,  $A_0$  through  $A_3$ , and four data outputs,  $H_0$  through  $H_3$ . There are two serial inputs, one for shift left ( $IL$ ) and the other for shift right ( $IR$ ). When the selection input  $S = 0$ , the input data are shifted right (down in the diagram). When  $S = 1$ , the input data are shifted left (up in the diagram). The function table in Fig. 12 shows which input goes to each output after the shift. A shifter with  $n$  data inputs and outputs requires  $n$  multiplexers. The two serial inputs can be controlled by another multiplexer to provide the three possible types of shifts.

## 2.6 Arithmetic Logic Shift Unit

- The arithmetic, logic, and shift circuits introduced in previous sections can be combined into one ALU with common selection variables. One stage of an arithmetic logic shift unit is shown in Fig. 13.
- Fig. 13 provides eight arithmetic operations, four logic operations, and two shift operations. Each operation is selected with the five variables  $S_3, S_2, S_1, S_0$ , and  $C$ . The input carry  $C$ , is used for selecting an arithmetic operation only.

Table 8 lists the 14 operations of the ALU. The first eight are arithmetic operations and are selected with  $S_3S_2 = 00$ . The next four are logic operations and are selected with  $S_3S_2 = 01$ .

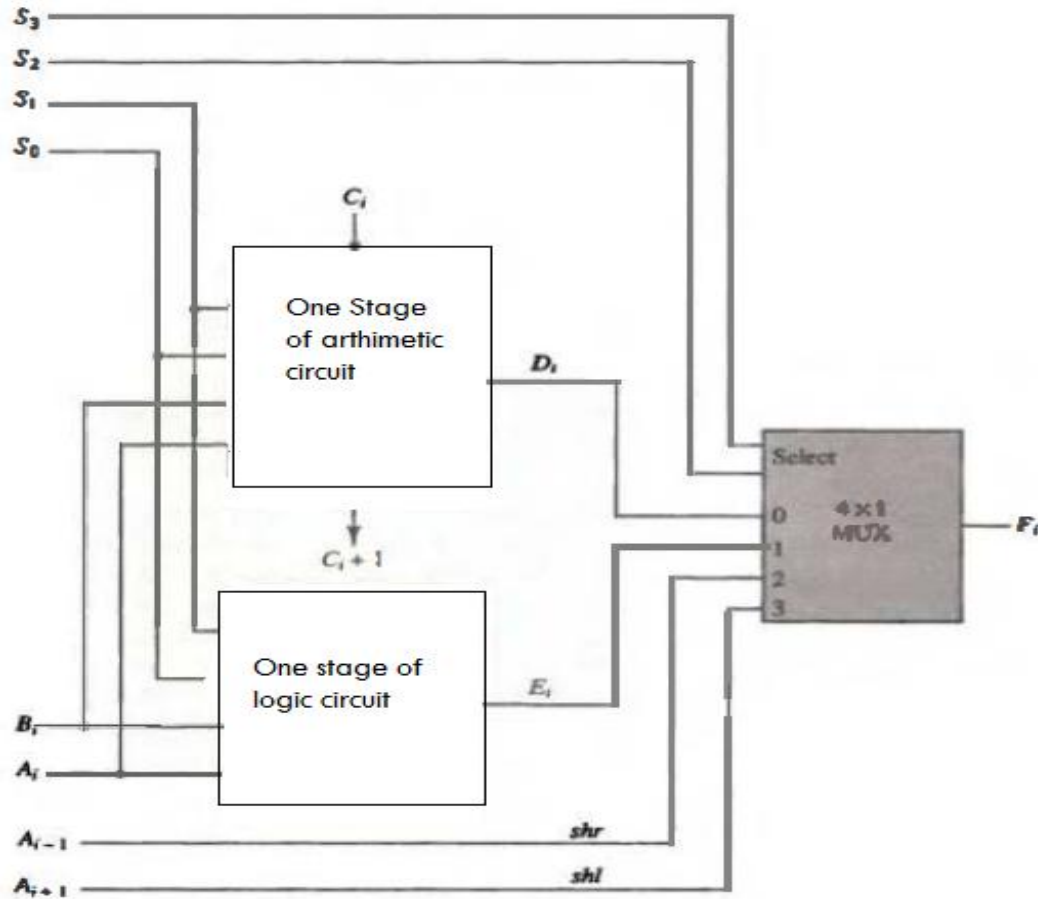


Fig 13: One stage of arithmetic and logic unit

TABLE 8 Function Table for Arithmetic Logic Shift Unit

Operation select					Operation	Function
$S_3$	$S_2$	$S_1$	$S_0$	$C_{in}$		
0	0	0	0	0	$F = A$	Transfer A
0	0	0	0	1	$F = A + 1$	Increment A
0	0	0	1	0	$F = A + B$	Addition
0	0	0	1	1	$F = A + B + 1$	Add with carry
0	0	1	0	0	$F = A + \bar{B}$	Subtract with borrow
0	0	1	0	1	$F = A + \bar{B} + 1$	Subtraction
0	0	1	1	0	$F = A - 1$	Decrement A
0	0	1	1	1	$F = A$	Transfer A
0	1	0	0	x	$F = A \wedge B$	AND
0	1	0	1	x	$F = A \vee B$	OR
0	1	1	0	x	$F = A \oplus B$	XOR
0	1	1	1	x	$F = \bar{A}$	Complement A
1	0	x	x	x	$F = shr A$	Shift right A into F
1	1	x	x	x	$F = shl A$	Shift left A into F

## 2.7 Control memory

- the control memory can be a read-only memory (ROM). The content of the words in ROM are fixed and cannot be altered by simple programming since no writing capability is available in the ROM.
  - ROM words are made permanent during the hardware production of the unit. The use of a microprogram involves placing all control variables in words of ROM for use by the control unit through successive read operations.
  - The content of the word in ROM at a given address specifies a microinstruction. A more advanced development known as dynamic microprogramming
  - permits a microprogram to be loaded initially from an auxiliary memory such as a magnetic disk. Control units that use dynamic microprogramming employ a writable control memory.
  - This type of memory can be used for writing (to change the microprogram) but is used mostly for reading. A memory that is part of a control unit is referred to as a control memory.
- 
- The general configuration of a microprogrammed control unit is demonstrated in the block diagram of Fig. 14 .
  - The control memory is assumed to be a ROM, within which all control information is permanently stored.
  - The control memory address register specifies the address of the microinstruction, and the control data register holds the microinstruction read from memory.
  - The microinstruction contains a control word that specifies one or more microoperations for the data processor. Once these operations are executed, the control must determine the next address.

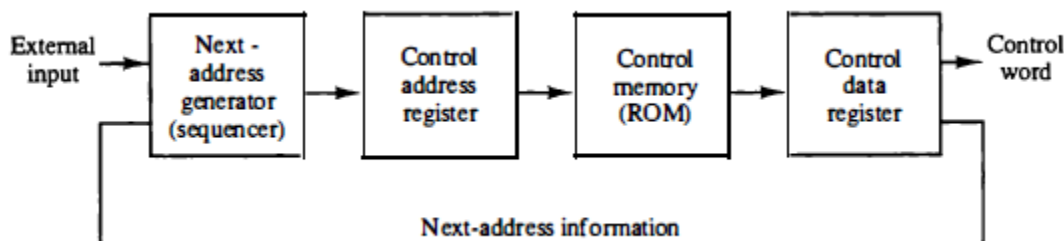


Fig 14: Microprogrammed control organization

- The hardware configuration should not be changed for different operations; the only thing that must be changed is the microprogram residing in control memory.

## 2.8 Address Sequencing

- Microinstructions are stored in control memory in groups, with each group specifying a routine. Each computer instruction has its own microprogram routine in control memory to generate the microoperations that execute the instruction.
- The hardware that controls the address sequencing of the control memory must be capable of sequencing the microinstructions within a routine and be able to branch from one routine to another.



- To appreciate the address sequencing in a microprogram control unit, let us enumerate the steps that the control must undergo during the execution of a single computer instruction. An initial address is loaded into the control address register when power is turned on in the computer.
- This address is usually the address of the first microinstruction that activates the instruction fetch routine.
- The fetch routine may be sequenced by incrementing the control address register through the rest of its microinstructions. At the end of the fetch routine, the instruction is in the instruction register of the computer.

The next step is to generate the microoperations that execute the instruction fetched from memory.

- The microoperation steps to be generated in processor registers depend on the operation code part of the instruction. Each instruction has its own microprogram routine stored in a given location of control memory.
- The transformation from the instruction code bits to an address in control memory where the routine is located is referred to as a mapping process. A mapping procedure is a rule that transforms the instruction code into a control memory address.
- Once the required routine is reached, the microinstructions that execute the instruction may be sequenced by incrementing the control address register, but sometimes the sequence of microoperations will depend on values of certain status bits in processor registers.
- Microprograms that employ subroutines will require an external register for storing the return address.
- Return addresses cannot be stored in ROM because the unit has no writing capability.
- When the execution of the instruction is completed, control must return to the fetch routine.
- This is accomplished by executing an unconditional branch microinstruction to the first address of the fetch routine.

In summary, the address sequencing capabilities required in a control memory are:

1. Incrementing of the control address register.
  2. Unconditional branch or conditional branch, depending on status bit conditions.
  3. A mapping process from the bits of the instruction to an address for control memory.
2. A facility for subroutine call and return.

Figure 7-2 shows a block diagram of a control memory and the associated hardware needed for selecting the next microinstruction address.

### **Conditional Branching**

The branch logic of Fig. 15 provides decision-making capabilities in the control unit.

The status conditions are special bits in the system that provide parameter information such as the carry-out of an adder, the sign bit of a number, the mode bits of an instruction, and input or output status conditions..

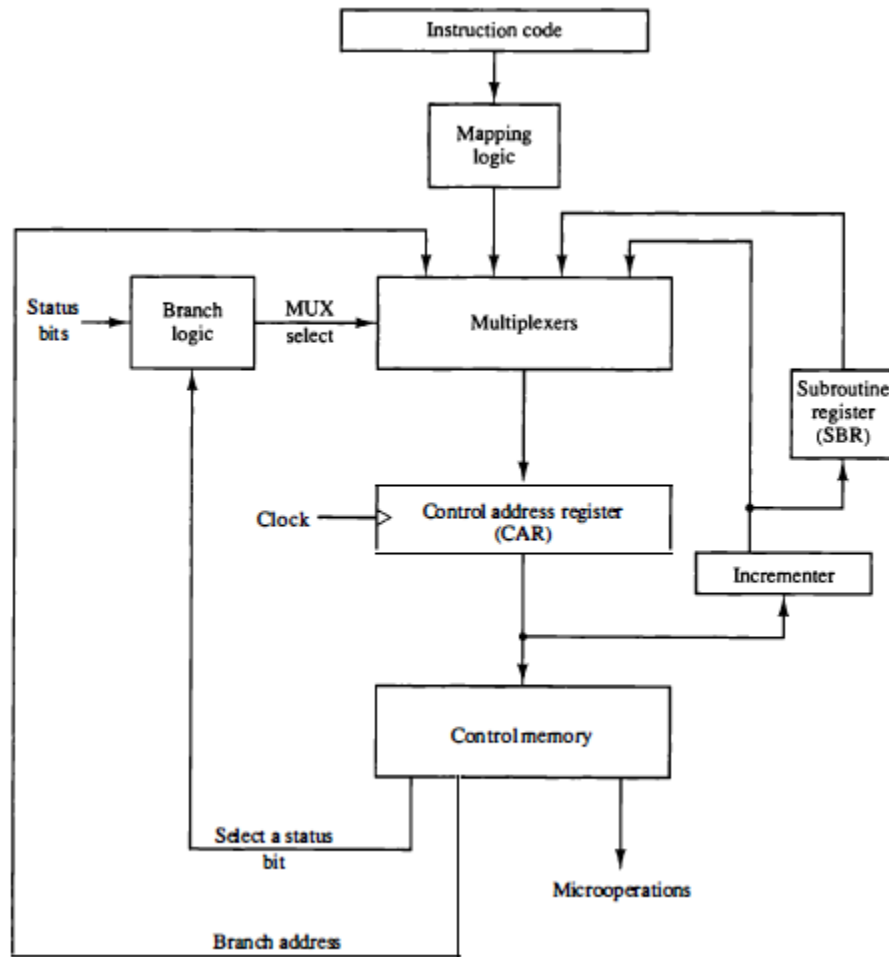


Fig 15: Selection for address for control memory

### Mapping of Instruction

- A special type of branch exists when a microinstruction specifies a branch to the first word in control memory where a microprogram routine for an instruction is located.
- The status bits for this type of branch are the bits in the operation code part of the instruction. For example, a computer with a simple instruction format as shown in Fig. 16 has an operation code of four bits which can specify up to 16 distinct instructions.
- Assume further that the control memory has 128 words, requiring an address of seven bits. For each operation code there exists a microprogram routine in control memory that executes the instruction. One simple mapping process that converts the 4-bit operation code to a 7-bit address for control memory is shown in Fig. 16.
- This mapping consists of placing a 0 in the most significant bit of the address, transferring the four operation code bits, and clearing the two least significant bits of the control address register. This provides for each computer instruction a microprogram routine with a capacity of four microinstructions. If the routine needs more than four microinstructions, it can use addresses 1000000 through 1 1 1 1 1 1 1 .

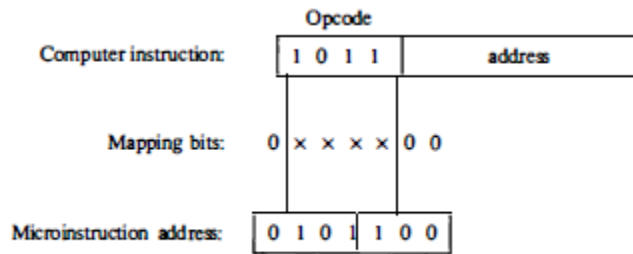


Fig 16: mapping of instructions

### Subroutines

- Subroutines are programs that are used by other routines to accomplish a particular task. A subroutine can be called from any point within the main body of the microprogram.
- Frequently, many microprograms contain identical sections of code. Microinstructions can be saved by employing subroutines that use common sections of microcode. For example, the sequence of microoperations needed to generate the effective address of the operand for an instruction is common to all memory reference instructions. This sequence could be a subroutine that is called from within many other routines to execute the effective address computation.
- Microprograms that use subroutines must have a provision for storing the return address during a subroutine call and restoring the address during a subroutine return.

### Microprogram Example

Once the configuration of a computer and its microprogrammed control unit is established, the designer's task is to generate the microcode for the control memory. This code generation is called microprogramming and is a process similar to conventional machine language programming.

### Computer Configuration

The block diagram of the computer is shown in Fig. 17 It consists of two memory units: a main memory for storing instructions and data, and a control memory for storing the microprogram. Four registers are associated with the processor unit and two with the control unit. The processor registers are

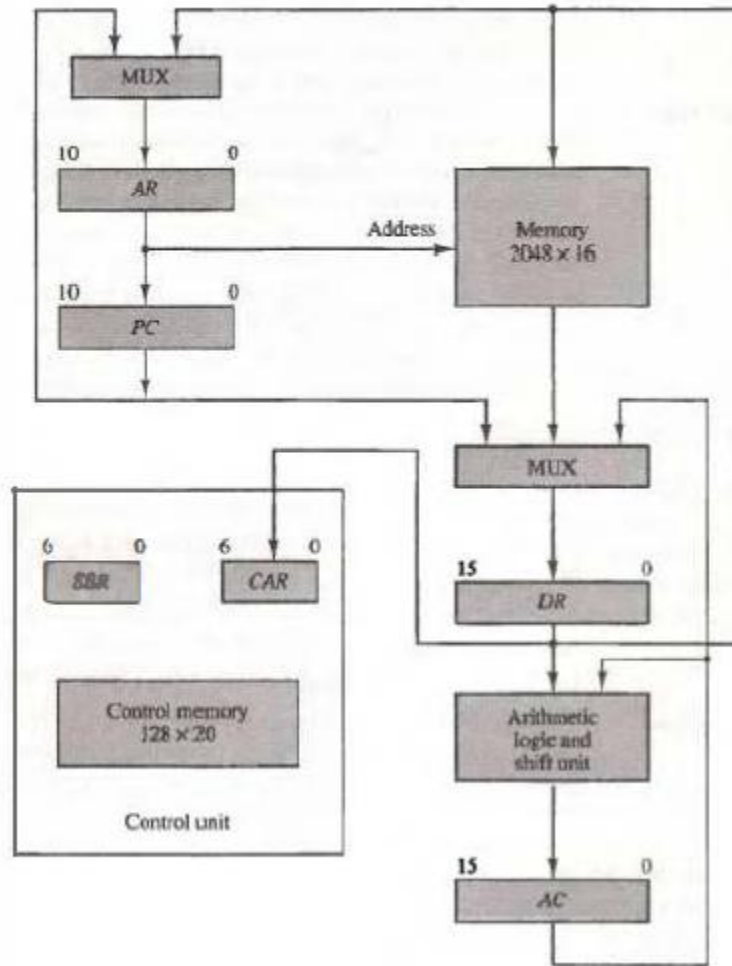


Fig 17 computer hard ware configuration

program counter PC, address register AR, data register DR, and accumulator register AC. The function of these registers is similar to the basic computer

## 2.8 Design of Control Unit

- The bits of the microinstruction are usually divided into fields, with each field defining a distinct, separate function. The various fields encountered in instruction formats provide control bits to initiate microoperations in the system, special bits to specify the way that the next address is to be evaluated, and an address field for branching.
- The number of control bits that initiate microoperations can be reduced by grouping mutually exclusive variables into fields and encoding the  $k$  bits in each field to provide  $2^k$  microoperations. Each field requires a decoder to produce the corresponding control signals.
- This method reduces the size of the microinstruction bits but requires additional hardware external to the control memory. It also increases the delay time of the control signals because they must propagate through the decoding circuits.

Figure 18 shows the three decoders and some of the connections that must be made from their outputs. Each of the three fields of the microinstruction presently available in the output of control memory are decoded with a 3 x 8 decoder to provide eight outputs.

As shown in Fig. 18 outputs 5 and 6 of decoder f1 are connected to the load input of AR so that when either one of these outputs is active, information from the multiplexers is transferred to AR. The multiplexers select the information from DR when output 5 is active and from PC when output 6 is inactive.

TABLE 7-4 Input Logic Truth Table for Microprogram Sequencer

BR Fiel	Input $I_1 I_0 T$	MUX 1 $S_1 S_0$	Load SBR $L$
0 0	0 0 0	0 0	0
0 0	0 0 1	0 1	0
0 1	0 1 0	0 0	0
0 1	0 1 1	0 1	1
1 0	1 0 $\times$	1 0	0
1 1	1 1 $\times$	1 1	0

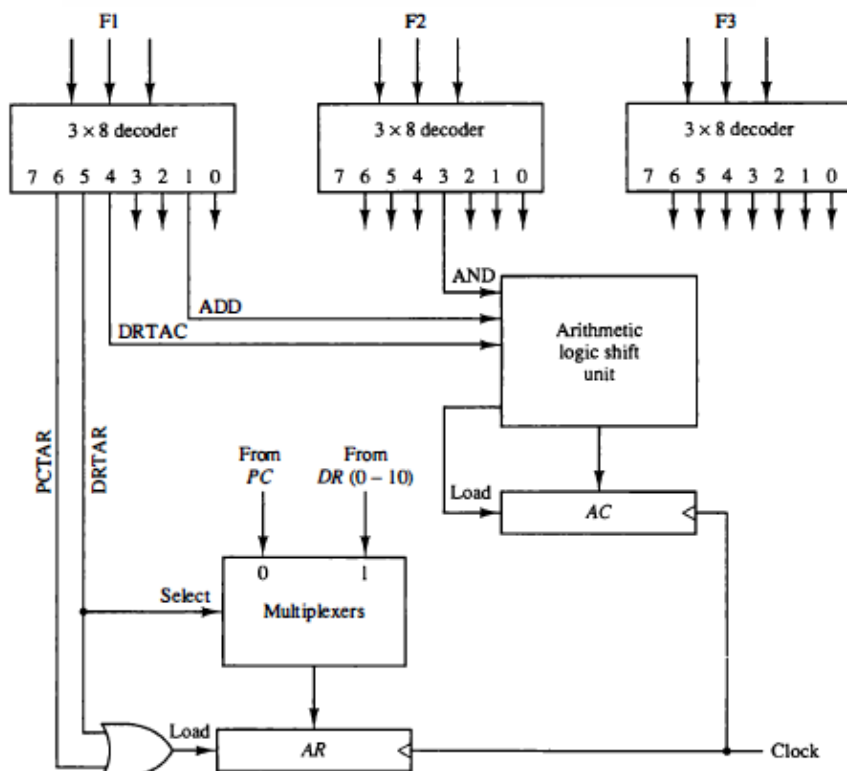


Fig 18: Decoding of micro coding operations

tively, as shown in Fig. 18. The other outputs of the decoders that are associated with an AC operation must also be connected to the arithmetic logic shift unit in a similar fashion.

## 2.10 Microprogram Sequencer

- A microprogram sequencer can be constructed with digital functions to suit a particular application. However, just as there are large ROM units available in integrated circuit packages, so are general-purpose sequencers suited for the construction of microprogram control units.
- To guarantee a wide range of acceptability, an integrated circuit sequencer must provide an internal organization that can be adapted to a wide range of applications.
- The block diagram of the microprogram sequencer is shown in Fig. 19.
- The control memory is included in the diagram to show the interaction between the sequencer and the memory attached to it.
- There are two multiplexers in the circuit. The first multiplexer selects an address from one of four sources and routes it into a control address register CAR .
- The second multiplexer tests the value of a selected status bit and the result of the test is applied to an input logic circuit. The output from CAR provides the address for the control memory. The content of CAR is incremented and applied to one of the multiplexer inputs and to the subroutine register SBR .

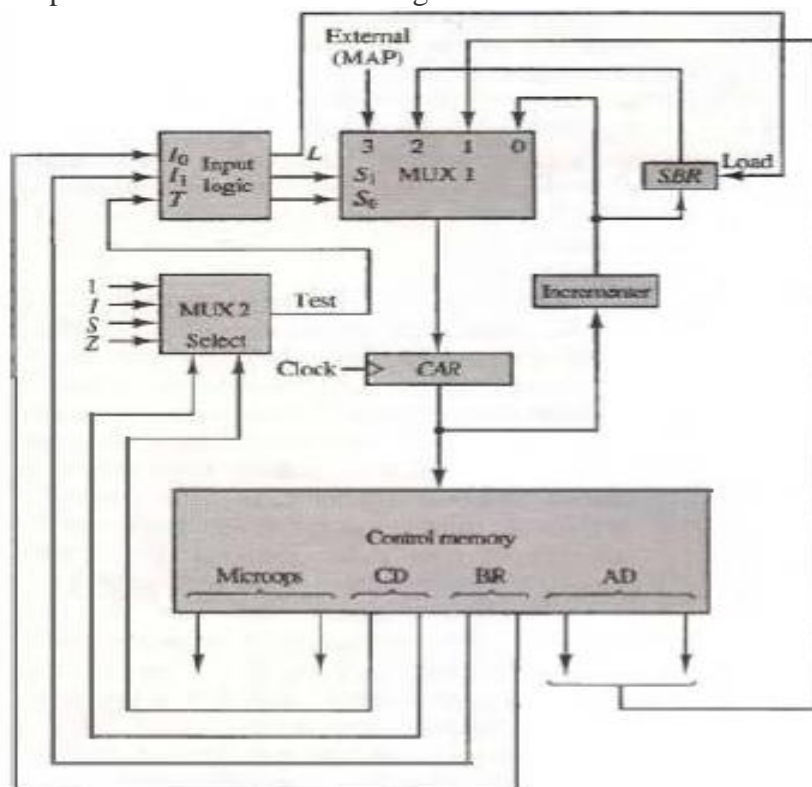


Fig19: Micro program sequencer for control memory

The input logic circuit in Fig. 19 has three inputs,  $I_0$ ,  $I_1$ , and  $T$ , and three outputs,  $S_0$ ,  $S_1$ , and  $L$ . Variables  $S_0$  and  $S_1$  select one of the source addresses for CAR. Variable  $L$  enables the load input in SBR. The binary values of the two selection variables determine the path in the multiplexer. For example, with  $S_1 S_0 = 10$ , multiplexer input number 2 is selected and

establishes a transfer path from SBR to CAR. Note that each of the four inputs as well as the output of MUX 1 contains a 7-bit address.

## UNIT-III

### CPU AND COMPUTER ARITHMETIC

CPU design: Instruction cycle, data representation, memory reference instructions, input-output, and interrupt, addressing modes, data transfer and manipulation, program control. Computer arithmetic: Addition and subtraction, floating point arithmetic operations, decimal arithmetic unit.

#### 3.1 INSTRUCTION CYCLE

- An **instruction cycle** (sometimes called a **fetch–decode–execute cycle**) is the basic operational process of a computer.
- It is the process by which a computer retrieves a program instruction from its memory, determines what actions the instruction dictates, and carries out those actions.
- This cycle is repeated continuously by a computer's central processing unit (CPU), from boot-up to when the computer is shut down.
- In simpler CPUs the instruction cycle is executed sequentially, each instruction being processed before the next one is started.
- In most modern CPUs the instruction cycles are instead executed concurrently, and often in parallel, through an instruction pipeline: the next instruction starts being processed before the previous instruction has finished, which is possible because the cycle is broken up into separate steps.

#### COMPONENTS

##### **Program counter (PC)**

An incrementing counter that keeps track of the memory address of the instruction that is to be executed next or in other words, holds the address of the instruction to be executed next.

##### **Memory address registers (MAR)**

Holds the address of a block of memory for reading from or writing to.

##### **Memory data register (MDR)**

A two-way register that holds data fetched from memory (and ready for the CPU to process) or data waiting to be stored in memory. (This is also known as the memory buffer register (MBR)).

##### **Instruction register (IR)**



A temporary holding ground for the instruction that has just been fetched from memory.

### **Control unit (CU)**

Decodes the program instruction in the IR, selecting machine resources, such as a data source register and a particular arithmetic operation, and coordinates activation of those resources.

### **Arithmetic logic unit (ALU)**

Performs mathematical and logical operations.

### **Floating-point unit (FPU)**

Performs floating-point operations.

Each computer's CPU can have different cycles based on different instruction sets, but will be similar to the following cycle:

1. **Fetch the instruction:** The next instruction is fetched from the memory address that is currently stored in the program counter (PC), and stored in the instruction register (IR). At the end of the fetch operation, the PC points to the next instruction that will be read at the next cycle.
2. **Decode the instruction:** During this cycle the encoded instruction present in the IR (instruction register) is interpreted by the decoder.
3. **Read the effective address:** In case of a memory instruction (direct or indirect) the execution phase will be in the next clock pulse. If the instruction has an indirect address, the effective address is read from main memory, and any required data is fetched from main memory to be processed and then placed into data registers (Clock Pulse:  $T_3$ ). If the instruction is direct, nothing is done at this clock pulses. If this is an I/O instruction or a Register instruction, the operation is performed (executed) at clock Pulse.
4. **Execute the instruction:** The control unit of the CPU passes the decoded information as a sequence of control signals to the relevant function units of the CPU to perform the actions required by the instruction such as reading values from registers, passing them to the ALU to perform mathematical or logic functions on them, and writing the result back to a register. If the ALU is involved, it sends a condition signal back to the CU. The result generated by the operation is stored in the main memory, or sent to an output device. Based on the condition of any feedback from the ALU, Program Counter may be updated to a different address from which the next instruction will be fetched.

The cycle is then repeated.

### **Initiating the cycle**

The cycle begins as soon as power is applied to the system, with an initial PC value that is predefined by the system's architecture (for instance, in Intel IA-32 CPUs, the predefined PC value is ). Typically this address points to a set of instructions in read-only memory (ROM), which begins the process of loading (or *booting*) the operating system.

## Fetching the instruction

Step 1 of the instruction cycle is fetch cycle, which is the same for each instruction:

1. The CPU sends the PC to the MAR and sends a read command on the address bus
2. In response to the read command (with address equal to PC), the memory returns the data stored at the memory location indicated by PC on the data bus
3. The CPU copies the data from the data bus into its MDR (also known as MBR, see section Components above)
4. A fraction of a second later, the CPU copies the data from the MDR to the instruction register (IR)
5. The PC is incremented so that it points to the following instruction in memory. This step prepares the CPU for the next cycle.

The control unit fetches the instruction's address from the memory unit.

## Decoding the instruction

Step 2 of the instruction Cycle is called the Decode Cycle. The decoding process allows the CPU to determine what instruction is to be performed, so that the CPU can tell how many operands it needs to fetch in order to perform the instruction. The opcode fetched from the memory is decoded for the next steps and moved to the appropriate registers. The decoding is done by the CPU's Control Unit.

## Reading the effective address

Step 3 is evaluating which operation it is. If this is a Memory operation - in this step the computer checks if it's a direct or indirect memory operation:

- **Direct memory instruction** - Nothing is being done.
- **Indirect memory instruction** - The effective address is being read from the memory.

If this is an I/O or Register instruction - the computer checks its kind and executes the instruction.

## Executing the instruction

Step 4 of the Instruction Cycle is the Execute Cycle. Here, the function of the instruction is performed. If the instruction involves arithmetic or logic, the Arithmetic Logic Unit is utilized. This is the only stage of the instruction cycle that is useful from the perspective of the end user. Everything else is overhead required to make the execute phase happen.

## 3.2 DATA REPRESENTATION

### 3.1.2 DATA TYPES

The data types found in the registers of digital computers may be classified as being one of the following categories:

- numbers used in arithmetic computations,
- letters of the alphabet used in data processing.

- Other discrete symbols used for specific purposes.

All types of data, except binary numbers, are represented in computer registers in binary form. This is because registers are made up of flip-flops and flip-flops are two-state devices that can store only 1's and 0's.

The binary number system is the most natural system to use in a digital computer. But sometimes it is convenient to employ different number systems.

### Number systems

- A number system of base, or radix,  $r$  is a system that uses distinct symbols for  $r$  digits. Numbers are represented by a string of digit symbols.
- To determine the quantity that the number represents, it is necessary to multiply each digit by an integer power of  $r$  and then form the sum of all weighted digits. For example, the decimal number system in everyday use employs the radix 10 system.
- The 10 symbols are 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9. The string of digits
- 724.5 is interpreted to represent the quantity
- $7 \times 10^2 + 2 \times 10^1 + 4 \times 10^0 + 5 \times 10^{-1}$

The binary number system uses the radix 2. The two digit symbols used are 0 and 1. The string of digits 101101 is interpreted to represent the quantity

$$1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 = 45$$

To distinguish between different radix numbers, the digits will be enclosed in parentheses and the radix of the number inserted as a subscript. For example, to show the equality between decimal and binary forty-five we will write  $(101101)_2 = (45)_{10}$ .

The octal (radix 8) and hexadecimal (radix 16) are important in digital computer work. The eight symbols of the octal system are 0, 1, 2, 3, 4, 5, 6, and 7. The 16 symbols of the hexadecimal system are 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, and F. When used to represent hexadecimal digits, the symbols A, B, C, D, E, F correspond to the decimal numbers 10, 11, 12, 13, 14, 15, respectively.

Octal 736.4 is converted to decimal as follows:

$$\begin{aligned}(736.4)_8 &= 7 \times 8^2 + 3 \times 8^1 + 6 \times 8^0 + 4 \times 8^{-1} \\ &= 7 \times 64 + 3 \times 8 + 6 \times 1 + 4/8 = (478.5)_{10}\end{aligned}$$

The equivalent decimal number of hexadecimal F3 is obtained from the following calculation:

$$(F3)_{16} = F \times 16 + 3 = 15 \times 16 + 3 = (243)_{10}$$

Binary Numeral System - Base-2

Binary numbers uses only 0 and 1 digits.

B denotes binary prefix.

Examples:

$$101012 = 10101B = 1 \times 24 + 0 \times 23 + 1 \times 22 + 0 \times 21 + 1 \times 20 = 16 + 4 + 1 = 21$$

$$101112 = 10111B = 1 \times 24 + 0 \times 23 + 1 \times 22 + 1 \times 21 + 1 \times 20 = 16 + 4 + 2 + 1 = 23$$

$$1000112 = 100011B = 1 \times 25 + 0 \times 24 + 0 \times 23 + 0 \times 22 + 1 \times 21 + 1 \times 20 = 32 + 2 + 1 = 35$$

Octal Numeral System - Base-8

Octal numbers uses digits from 0..7.

Examples:

$$278 = 2 \times 81 + 7 \times 80 = 16 + 7 = 23$$

$$308 = 3 \times 81 + 0 \times 80 = 24$$

$$43078 = 4 \times 83 + 3 \times 82 + 0 \times 81 + 7 \times 80 = 2247$$

Decimal Numeral System - Base-10

Decimal numbers uses digits from 0..9.

These are the regular numbers that we use.

Example:

$$253810 = 2 \times 103 + 5 \times 102 + 3 \times 101 + 8 \times 100$$

Hexadecimal Numeral System - Base-16

Hex numbers uses digits from 0..9 and A..F.

H denotes hex prefix.

Examples:

$$2816 = 28H = 2 \times 161 + 8 \times 160 = 40$$

$$2F16 = 2FH = 2 \times 161 + 15 \times 160 = 47$$

$$BC1216 = BC12H = 11 \times 163 + 12 \times 162 + 1 \times 161 + 2 \times 160 = 48146$$

### TYPES OF INSTRUCTIONS

The basic computer has three 16-bit instruction code formats:

1. Memory Reference Instructions
2. Register Reference Instructions
3. Input/Output Instructions

### MEMORY REFERENCE INSTRUCTIONS

In Memory reference instruction: First 12 bits(0-11) specify an address.

- ☐ Next 3 bits specify operation code (opcode).
- ☐ Left most bit specify the addressing mode I
- ☐ I = 0 for direct address I = 1 for indirect address

#### Memory Reference Instructions

In Memory reference instruction: first 12 bits (0-11) specify an address.

- ☐ The address field is denoted by three x's (in hexadecimal notation) and is equivalent to 12-bit address. The last mode bit of the instruction represents by symbol I.
- ☐ When I = 0, the last four bits of an instruction have a hexadecimal digit equivalent from 0 to 6 since the last bit is zero (0). When I = 1 the last four bits of an instruction have a hexadecimal digit equivalent from 8 to E since the last bit is one (1).

#### Memory Reference Instructions

	Hexadecimal code		
Symbol	I = 0	I = 1	Description
AND	0xxx	8xxx	AND memory word to AC
ADD	1xxx	9xxx	ADD memory word to AC
LDA	2xxx	Axxx	LOAD Memory word to AC
STA	3xxx	Bxxx	Store content of AC in memory
BUN	4xxx	Cxxx	Branch unconditionally
BSA	5xxx	Dxxx	Branch and save return address

ISZ	6xxx	Exxx	Increment and Skip if zero
-----	------	------	----------------------------

## Register Reference Instructions

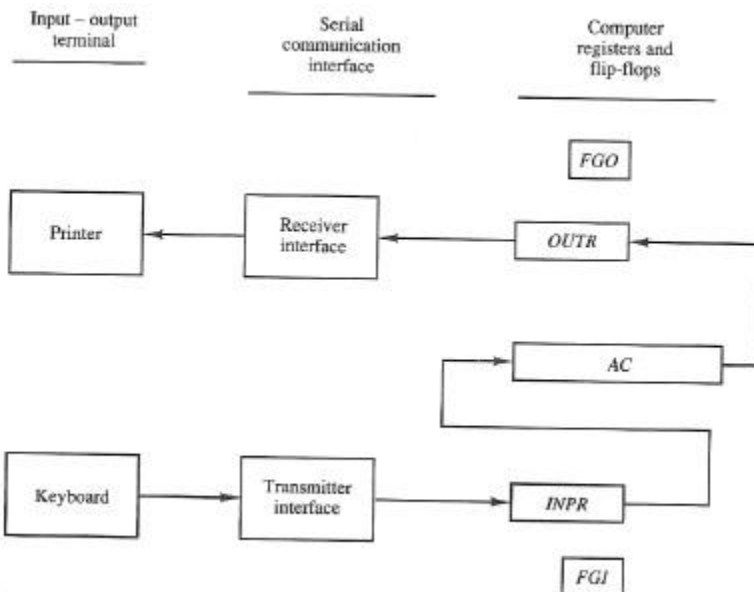
In Register Reference Instruction: First 12 bits (0-11) specify the register operation.

- ☐ The next three bits equals to 111 specify opcode.
- ☐ The last mode bit of the instruction is 0.
- ☐ Therefore, left most 4 bits are always 0111 which is equal to hexadecimal 7.

## I/O Reference Instructions

In I/O Reference Instruction: First 12 bits (0-11) specify the I/O operation.

- ☐ The next three bits equals to 111 specify opcode.
  - ☐ The last mode bit of the instruction is 1.
  - ☐ Therefore, left most 4 bits are always 1111 which is equal to hexadecimal F.
- A computer is useless unless the information is communication between I/O terminals and the processor. In a computer, instructions and data stored in memory come from some input device and computational results must be transmitted to the user through some output device.
  - The terminal sends and receives serial information. Each quantity of information has 8 bits of an alphanumeric code. Two basic computer registers INPR and OUTR communicate with a communication interface.



Input-Output Configuration

- The terminals send and receive serial information the 8-bits information is shifted from the keyboard into the input register(INPR). The serial
- information for the printer is stored in OUTR. These two registers communicate in the communication interface serially and with the
- accumulator in parallel. The transmitter interface receives the information and transfer to INPR. The receiver interface receives from OUTR and transmits to the printer.
- The input register INPR consists of 8-bits and stores alphanumeric information. FGI is 1-bit controlled flip-flop or flag. A flag bit is set to 1.
- When new information is available in input device and cleared to zero and the information is accepted by the computer. Initially, the input flag
- FGI clear to zero. When a key in a keyboard is pressed , 8-bits alphanumeric code is shifted into INPR is transferred into accumulator and FGI is cleared to zero. The output flag FGO is initially set to one the computer checks FGO and if it is one(1) then the content of accumulator(AC) is transferred into OUTR and FGO is cleared to zero. Once the content of OUTR is transmitted to the printer FGO is again set to 1. Therefore, if FGO=1, then the data from input device can't be transferred into INPR and similarly, if FGO=0, then the content of AC can't be transferred into OUTR.

### Input-Output Instruction

I/O instructions are needed to transferring information to and from AC register, for checking the flag bits and for controlling the interrupt facility.

$D_7IT_3 = p$  (common to all input-output instructions)

$IR(i) = B_i$  [bit in  $IR(6-11)$  that specifies the instruction]

	$p:$	$SC \leftarrow 0$	Clear $SC$
INP	$pB_{11}:$	$AC(0-7) \leftarrow INPR, FGI \leftarrow 0$	Input character
OUT	$pB_{10}:$	$OUTR \leftarrow AC(0-7), FGO \leftarrow 0$	Output character
SKI	$pB_9:$	If $(FGI = 1)$ then $(PC \leftarrow PC + 1)$	Skip on input flag
SKO	$pB_8:$	If $(FGO = 1)$ then $(PC \leftarrow PC + 1)$	Skip on output flag
ION	$pB_7:$	$IEN \leftarrow 1$	Interrupt enable on
IOF	$pB_6:$	$IEN \leftarrow 0$	Interrupt enable off

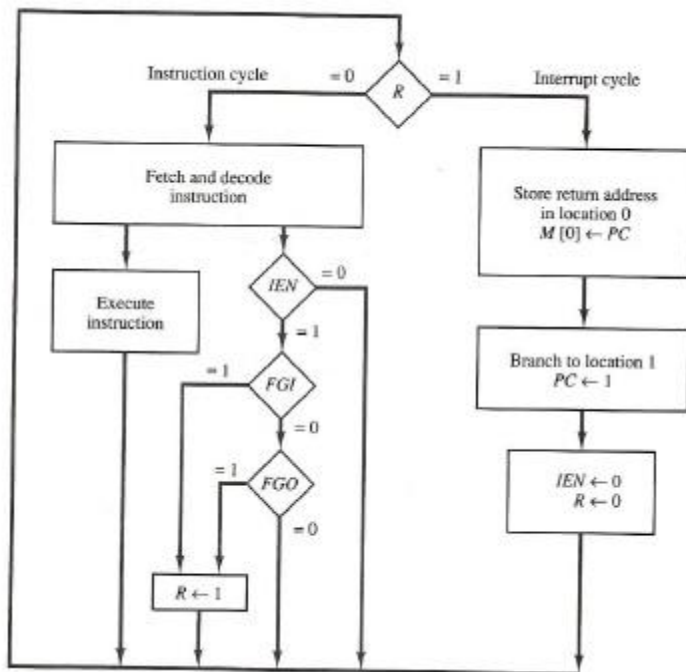
I/O instruction

### Program Interrupt

- Input and Output interactions with electromechanical peripheral devices require huge processing times compared with CPU processing times. – I/O (milliseconds) versus CPU (nano/microseconds)
- Interrupts permit other CPU instructions to execute while waiting for I/O to complete.
- The I/O interface, instead of the CPU, monitors the I/O device.
- When the interface found that the I/O device is ready for data transfer, it generates an interrupt request to the CPU
- Upon detecting an interrupt, the CPU stops momentarily the task it is doing, branches to the service routine to process the data transfer, and then returns to the task it was performing.

### Interrupt Cycle

This is a hardware implementation of a branch and save return address operation.



Flowchart of interrupt cycle

- An alternative to the program controlled procedure is to let the internal device inform the computer when it is ready for data transfer. At The same time, the processor can execute other tasks. This method uses the interrupt facility when the computer is w=executing a program, itdoesn't check the flags.But, when the flag is set , the computer is momentarily interrupted from executing the current program and is informed that the flag has been set.
- In this case, the computer momentarily deviates from what it is executing currently and starts the I/Otransfer . Once the I/O transfer is complete, the computer returns back to its original job.
- The interrupt enables flip-flop IEN can be set and cleared with two instruction. When IEN is cleared to zero with IOF instruction. Then, the flag can't interrupt the computer , when IEN is set to 1 with ION instruction the computer can be interrupted.

#### Register transfer operation in interrupt cycle

##### Register Transfer Statements for Interrupt Cycle

-RF/F←1 if IEN(FGI+FGO)T0'T1'T2'↔T0'T1'T2'(IEN)(FGI+FGO):R←1

The fetch and decode phases of the instruction cycle must be modified: Replace T0,T1,T2 with R'T0,R'T1,R'T2

The interrupt cycle: RT0:AR←0,TR←PC

RT1:M[AR]←TR,PC←0

RT2:PC←PC+1,IEN←0,R←0,SC← 0



## Complete Computer Description Flowchart

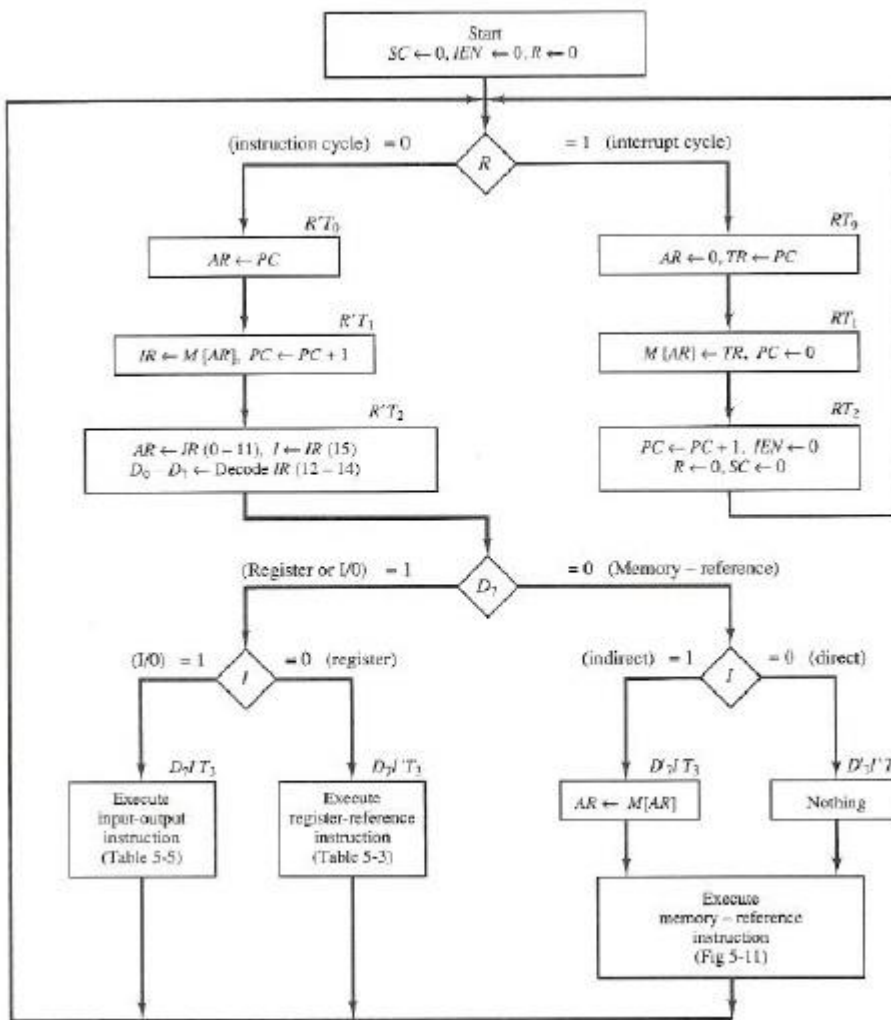


fig. Instruction cycle including Interrupt cycle

## ADDRESSING MODES

Addressing mode is the way of addressing a memory location in instruction. Microcontroller needs data or operands on which the operation is to be performed. The method of specifying source of operand and output of result in an instruction is known as addressing mode.

There are various methods of giving source and destination address in instruction, thus there are various types of Addressing Modes. Here you will find the different types of Addressing Modes that are supported in Micro Controller 8051. Types of Addressing Modes are explained below:

Also Read: Introduction to Microcontroller 8051

## Types Of Addressing Modes:

Following are the types of Addressing Modes:

- Register Addressing Mode
- Direct Addressing Mode
- Register Indirect Addressing Mode
- Immediate Addressing Mode
- Index Addressing Mode
- Also Read: How Microcontroller Works

Explanation:

- **Register Addressing Mode:** In this addressing mode, the source of data or destination of result is Register. In this type of addressing mode the name of the register is given in the instruction where the data to be read or result is to be stored.

Example: ADD A, R5 (The instruction will do the addition of data in Accumulator with data in register R5)

For example,

MOV DX, TAX\_RATE ; Register in first operand

MOV COUNT, CX ; Register in second operand

MOV EAX, EBX ; Both the operands are in registers

- **Direct Addressing Mode:** In this type of Addressing Mode, the address of data to be read is directly given in the instruction. In case, for storing result the address given in instruction is used to store the result.

Example: MOV A, 46H (This instruction will move the contents of memory location 46H to Accumulator)

For example,

BYTE\_VALUE DB 150 ; A byte value is defined

WORD\_VALUE DW 300 ; A word value is defined

ADD BYTE\_VALUE, 65 ; An immediate operand 65 is added

MOV AX, 45H ; Immediate constant 45H is transferred to AX

- **Mode Register Indirect Addressing:** In Register Indirect Addressing Mode, as its name suggests the data is read or stored in register indirectly. That is, we provide the register in the instruction, in which the address of the other register is stored or which points to other register where data is stored or to be stored.

Example: MOV A, @R0 (This instruction will move the data to accumulator from the register whose address is stored in register R0 ).

Also Read: Architecture of 8051

- **Immediate Addressing Mode:** In Immediate Addressing Mode, the data immediately follows the instruction. This means that data to be used is already given in the instruction itself.

Example: MOV A, #25H (This instruction will move the data 25H to Accumulator. The #sign show that preceding term is data, not the address.)

- **Index Addressing Mode:** Offset is added to the base index register to form the effective address if the memory location. This Addressing Mode is used for reading lookup tables in Program Memory. The Address of the exact location of the table is formed by adding the Accumulator Data to the base pointer.

Example: MOVC, @A+DPTR (This instruction will move the data from the memory to Accumulator; the address is made by adding the contents of Accumulator and Data Pointer.

## Reading Assignments and Exercises

This section is organized as follows:

- 3.1. Arithmetic and Logic Operations
- 3.2. Arithmetic Logic Units and the MIPS ALU
- 3.3. Boolean Multiplication and Division
- 3.4. Floating Point Arithmetic
- 3.5. Floating Point in MIPS

Information contained herein was compiled from a variety of text- and Web-based sources, is intended as a teaching aid only (to be used in conjunction with the required text, and is not to be used for any commercial purpose. A particular thank is given to Dr. Enrique Mafla for his permission to use selected illustrations from his course notes in these Web pages.

In order to secure your understanding of the topics in this section, students should review the discussion of number representation in Section 2.4, especially twos complement.

### 3.1. ARITHMETIC AND LOGIC OPERATIONS

#### Reading Assignments and Exercises

The ALU is the core of the computer - it performs arithmetic and logic operations on data that not only realize the goals of various applications (e.g., scientific and engineering programs), but also manipulate addresses (e.g., pointer arithmetic). In this section, we will overview algorithms used for the basic arithmetic and logical operations. A key assumption is that twos complement representation will be employed, unless otherwise noted.

#### 3.1.1. Boolean Addition

When adding two numbers, if the sum of the digits in a given position equals or exceeds the modulus, then a *carry* is propagated. For example, in Boolean addition, if two ones are added, the sum is obviously two (base 10), which exceeds the modulus of 2 for Boolean numbers ( $\mathbf{B} = \mathbf{Z}_2 = \{0,1\}$ , the integers modulo 2). Thus, we record a zero for the sum and propagate a carry valued at one into the next more significant digit, as shown in Figure 3.1.

$$\begin{array}{r}
 \bullet 5_{\text{ten}} + 6_{\text{ten}} \\
 \begin{array}{r}
 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0101\ (5_{\text{ten}}) \\
 +\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0110\ (6_{\text{ten}}) \\
 \hline
 =\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 1011\ (11_{\text{ten}})
 \end{array}
 \end{array}$$

**Carries**

$$\begin{array}{r}
 \dots (0) \quad (1) \quad (0) \quad (0) \quad (0) \\
 \dots 0 \quad 0 \quad 1 \quad 0 \quad 1 \\
 + \dots 0 \quad 0 \quad 1 \quad 1 \quad 0 \\
 \hline
 \dots 0 \quad (0)1 \quad (1)0 \quad (0)1 \quad (0)1
 \end{array}$$

**Figure 3.1.** Example of Boolean addition with carry propagation, adapted from [Maf01].

#### 3.1.2. Boolean Subtraction

When subtracting two numbers, two alternatives present themselves. First, one can formulate a subtraction algorithm, which is distinct from addition. Second, one can negate the subtrahend (i.e., in  $a - b$ , the subtrahend is  $b$ ) then perform addition. Since we already know how to perform addition as well as twos complement negation, the second alternative is more practical. Figure 3.2 illustrates both processes, using the decimal subtraction  $12 - 5 = 7$  as an example.

$$\begin{aligned}
 & \bullet 12_{\text{ten}} - 5_{\text{ten}} \\
 & \quad 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 1100 \quad (12_{\text{ten}}) \\
 & - \quad 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0101 \quad (5_{\text{ten}}) \\
 & \hline
 & = 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0111 \quad (7_{\text{ten}})
 \end{aligned}$$
  

$$\begin{aligned}
 & \bullet 12_{\text{ten}} - 5_{\text{ten}} = 12_{\text{ten}} + (-5_{\text{ten}}) \\
 & \quad 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 1100 \quad (12_{\text{ten}}) \\
 & + \quad 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1011 \quad (-5_{\text{ten}}) \\
 & \hline
 & = 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0111 \quad (7_{\text{ten}})
 \end{aligned}$$

**Figure 3.2.** Example of Boolean subtraction using (a) unsigned binary representation, and (b) addition with twos complement negation - adapted from [Maf01].

Just as we have a carry in addition, the subtraction of Boolean numbers uses a *borrow*. For example, in Figure 3.2a, in the first (least significant) digit position, the difference  $0 - 1$  in the one's place is realized by borrowing a one from the two's place (next more significant digit). The borrow is propagated upward (toward the most significant digit) until it is zeroed (i.e., until we encounter a difference of  $1 - 0$ ).

### 3.1.3. Overflow

Overflow occurs when there are insufficient bits in a binary number representation to portray the result of an arithmetic operation. Overflow occurs because computer arithmetic is not closed with respect to addition, subtraction, multiplication, or division. Overflow *cannot* occur in addition (subtraction), if the operands have different (resp. identical) signs.

To detect and compensate for overflow, one needs  $n+1$  bits if an  $n$ -bit number representation is employed. For example, in 32-bit arithmetic, 33 bits are required to detect or compensate for overflow. This can be implemented in addition (subtraction) by letting a carry (borrow) occur into (from) the sign bit. To make a pictorial example of convenient size, Figure 3.3 illustrates the four possible sign combinations of differencing 7 and 6 using a number representation that is four bits long (i.e., can represent integers in the interval  $[-8,7]$ ).

$  \begin{array}{r}  7 + 6 \\  \begin{array}{cccc}  0 & 1 & 1 & 1 \\  + 0 & 1 & 1 & 0 \\  \hline  1 & 1 & 0 & 1  \end{array}  \end{array}  \begin{array}{l}  (7_{\text{ten}}) \\  (6_{\text{ten}}) \\  (13_{\text{ten}})  \end{array}  $	$  \begin{array}{r}  -7 + -6 \\  \begin{array}{cccc}  1 & 0 & 0 & 1 \\  + 1 & 0 & 1 & 0 \\  \hline  0 & 0 & 1 & 1  \end{array}  \end{array}  \begin{array}{l}  (-7_{\text{ten}}) \\  (-6_{\text{ten}}) \\  (-13_{\text{ten}})  \end{array}  $
$  \begin{array}{r}  -7 - 6 \\  \begin{array}{cccc}  1 & 0 & 0 & 1 \\  - 0 & 1 & 1 & 0 \\  \hline  0 & 0 & 1 & 1  \end{array}  \end{array}  \begin{array}{l}  (-7_{\text{ten}}) \\  (6_{\text{ten}}) \\  (-13_{\text{ten}})  \end{array}  $	$  \begin{array}{r}  -7 - 6 = -7 + -6 \\  \begin{array}{cccc}  1 & 0 & 0 & 1 \\  + 1 & 0 & 1 & 0 \\  \hline  0 & 0 & 1 & 1  \end{array}  \end{array}  \begin{array}{l}  (-7_{\text{ten}}) \\  (-6_{\text{ten}}) \\  (-13_{\text{ten}})  \end{array}  $

**Figure 3.3.** Example of overflow in Boolean arithmetic, adapted from [Maf01].

### 3.1.4. MIPS Overflow Handling

MIPS raises an *exception* when overflow occurs. Exceptions (or interrupts) act like procedure calls. The register \$sepc stores the address of the instruction that *caused* the interrupt, and the instruction

**mfc register, \$sepc**

moves the contents of \$sepc to *register*. For example, *register* could be \$t1. This is an efficient approach, since no conditional branch is needed to test for overflow.

Two's complement arithmetic operations (add, addi, and sub instructions) raise exceptions on overflow. In contrast, unsigned arithmetic (addu and addiu) instructions do not raise an exception on overflow, since they are used for arithmetic operations on addresses (recall our discussion of pointer arithmetic in Section 2.6). In terms of high-level languages, C ignores overflows (always uses addu, addiu, and subu), while FORTRAN uses the appropriate instruction to detect overflow. Figure 3.4 illustrates the use of conditional branch on overflow for signed and unsigned addition operations.

#### Signed addition

addu	\$t0, \$t1, \$t2	# add but do not trap
xor	\$t3, \$t1, \$t2	# check if sign differ
slt	\$t3, \$t3, \$0	# \$t3 = 1 if signs differ
bne	\$t3, \$0, NO_OVFL	# signs of t1, t2 different
xor	\$t3, \$t0, \$t1	# sign of sum (t0) different?
slt	\$t3, \$t3, \$0	# \$t3 = 1 if sum has different sign
bne	\$t3, \$0, OVFL	# go to overflow

#### Unsigned addition (range = $[0 : 2^{32} - 1] \Rightarrow \$t1 + \$t2 \leq 2^{32} - 1$ )

addu	\$t0, \$t1, \$t2	# \$t0 contains the sum
nor	\$t3, \$t1, \$0	# negate \$t1 (\$t3 = NOT \$t1)
sltu	\$t3, \$t3, \$t2	# $2^{32} - 1 - t1 < t2$ ?
bne	\$t3, \$0, OVFL	# $t1 + t2 > 2^{32} - 1 \Rightarrow$ overflow

**Figure 3.4.** Example of overflow in Boolean arithmetic, adapted from [Maf01].

### 3.1.5. Logical Operations

Logical operations apply to fields of bits within a 32-bit word, such as bytes or bit fields (in C, as discussed in the next paragraph). These operations include shift-left and shift-right operations (sll and srl), as well as bitwise *and*, *or* (and, andi, or, ori). As we saw in Section 2, bitwise operations treat an operand as a vector of bits and operate on each bit position.

C bit fields are used, for example, in programming communications hardware, where manipulation of a bit stream is required. In Figure 3.5 is presented C code for an example communications routine, where a structure called *receiver* is formed from an 8-bit field called *receivedByte* and two one-bit fields called *ready* and *enable*. The C routine sets *receiver.ready* to 0 and *receiver.enable* to 1.

```

struct {
    unsigned int ready:      1;
    unsigned int enable:     1;
    unsigned int receivedByte: 8;
} receiver;
int data = receiver.receivedByte;
receiver.ready = 0;
receiver.enable = 1;

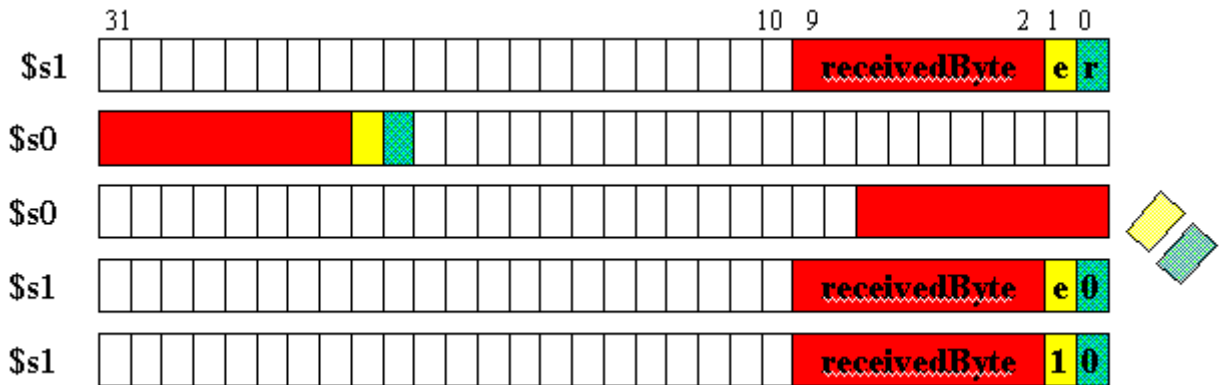
```

```

# $s0: data; $s1: receiver

sll    $s0, $s1, 22
srl    $s0, $s0, 24
andi   $s1, $s1, 0xfffe
ori    $s1, $s1, 0x0002

```



**Figure 3.5.** Example of C bit field use in MIPS, adapted from [Maf01].

Note how the MIPS code implements the functionality of the C code, where the state of the registers \$s0 and \$s1 is illustrated in the five lines of diagrammed register contents below the code. In particular, the initial register state is shown in the first two lines. The sll instruction loads the contents of \$s1 (the receiver) into \$s0 (the data register), and the result of this is shown on the second line of the register contents. Next, the srl instruction left-shifts \$s0 24 bits, thereby discarding the *enable* and *ready* field information, leaving just the received byte. To signal the receiver that the data transfer is completed, the andi and ori instructions are used to set the enable and ready bits in \$s1, which corresponds to the *receiver*. The data in \$s0 has already been received and put in a register, so there is no need for its further manipulation.

### 3.2. Arithmetic Logic Units and the MIPS ALU

#### Reading Assignments and Exercises

In this section, we discuss hardware building blocks, ALU design and implementation, as well as the design of a 1-bit ALU and a 32-bit ALU. We then overview the implementation of the MIPS ALU.

#### 3.2.1. Basic Concepts of ALU Design

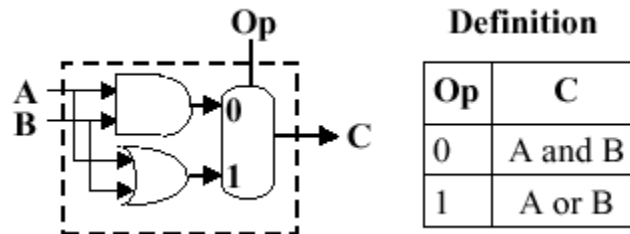
ALUs are implemented using lower-level components such as logic gates, including *and*, *or*, *not* gates and multiplexers. These building blocks work with individual bits,



but the actual ALU works with 32-bit registers to perform a variety of tasks such as arithmetic and shift operations.

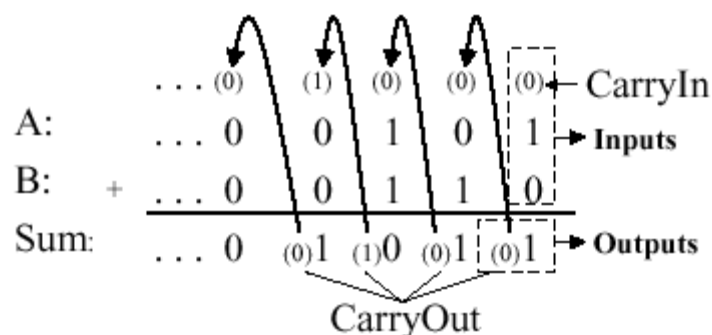
In principle, an ALU is built from 32 separate 1-bit ALUs. Typically, one constructs separate hardware blocks for each task (e.g., arithmetic and logical operations), where each operation is applied to the 32-bit registers in parallel, and the selection of an operation is controlled by a multiplexer. The advantage of this approach is that it is easy to add new operations to the instruction set, simply by associating an operation with a multiplexer control code. This can be done provided that the mux has sufficient capacity. Otherwise, new data lines must be added to the mux(es), and the CPU must be modified to accommodate these changes.

**3.2.2.1. And/Or Operations.** As shown in Figure 3.6, a simple (1-bit) ALU operates *in parallel*, producing all possible results that are then selected by the multiplexer (represented by an oval shape at the output of the *and* / *or* gates. The output *C* is thus selected by the multiplexer. (*Note*: If the multiplexer were to be applied at the input(s) rather than the output, twice the amount of hardware would be required, because there are two inputs versus one output.)



**Figure 3.6.** Example of a simple 1-bit ALU, where the oval represents a multiplexer with a control code denoted by *Op* and an output denoted by *C* - adapted from [Maf01].

**3.2.2.2. Full Adder.** Now let us consider the one-bit adder. Recalling the carry situation shown in Figure 3.1, we show in Figure 3.7 that there are two types of carries - *carry in* (occurs at the input) and *carry out* (at the output).



**Figure 3.7.** Carry-in and carry-out in Boolean addition, adapted from [Maf01].

Here, each bit of addition has three input bits ( $A_i$ ,  $B_i$ , and  $\text{CarryIn}_i$ ), as well as two output bits ( $\text{Sum}_i$ ,  $\text{CarryOut}_i$ ), where  $\text{CarryIn}_{i+1} = \text{CarryOut}_i$ . (Note: The "i" subscript denotes the i-th bit.) This relationship can be seen when considering the full adder's truth table, shown below:

Symbol

CarryIn

A

B

+

Sum

CarryOut

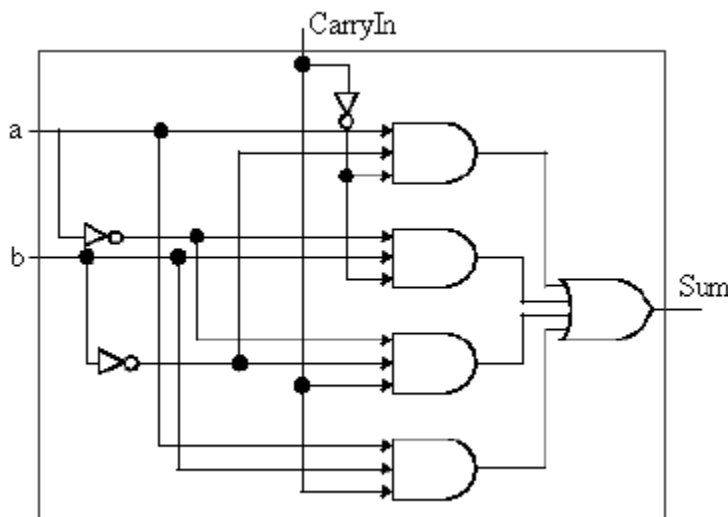
Definition

A	B	CarryIn	CarryOut	Sum
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

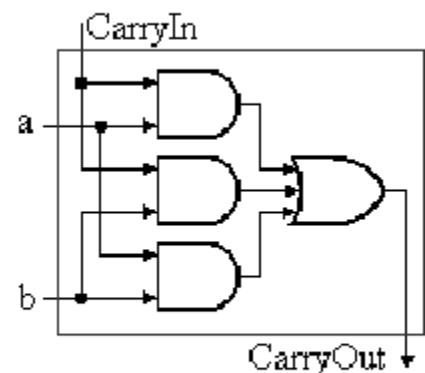
$$\begin{aligned}\text{CarryOut} &= (A*B*\text{CarryIn}) + (A*B*\text{CarryIn}) + (A*B*\text{CarryIn}) + (A*B*\text{CarryIn}) \\ &= (B*\text{CarryIn}) + (A*\text{CarryIn}) + (A*B)\end{aligned}$$

$$\text{Sum} = (A*B*\text{CarryIn}) + (A*B*\text{CarryIn}) + (A*B*\text{CarryIn}) + (A*B*\text{CarryIn})$$

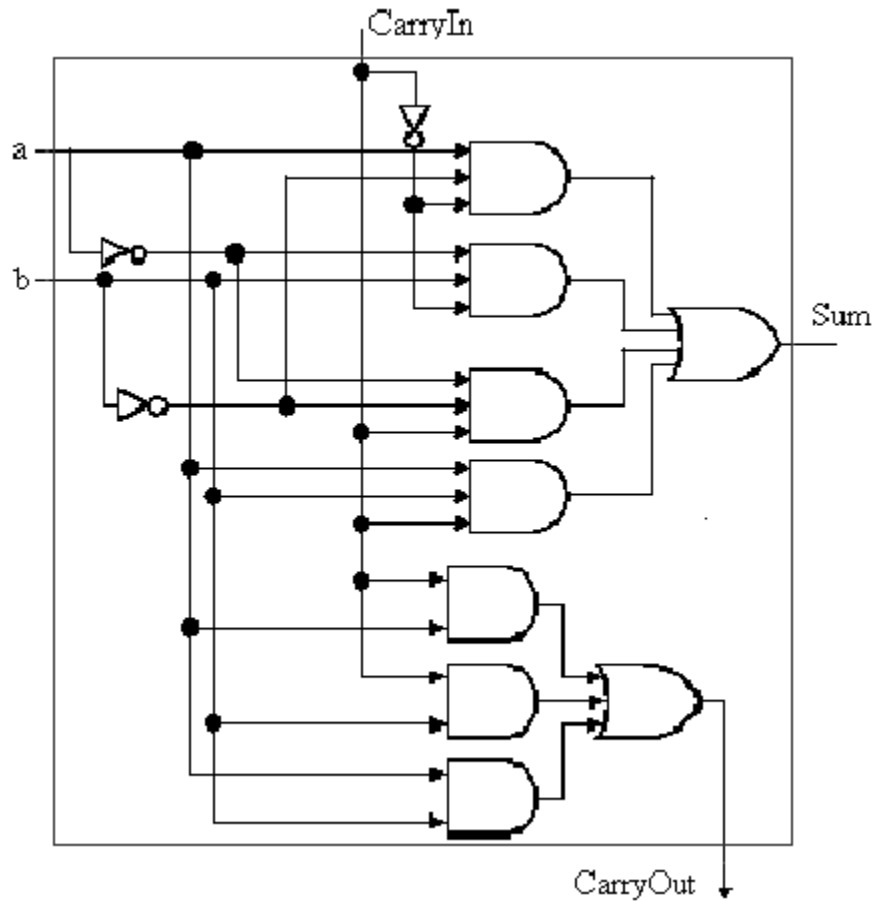
Given the four one-valued results in the truth table, we can use the sum-of-products method to construct a one-bit adder circuit from four three-input *and* gates and one four-input *or* gate, as shown in Figure 3.8a. The CarryOut calculation can be similarly implemented with three two-input *and* gates and one three-input *or* gate, as shown in Figure 3.8b. These two circuits can be combined to effect a one-bit full adder with carry, as shown in Figure 3.8c.



(a)



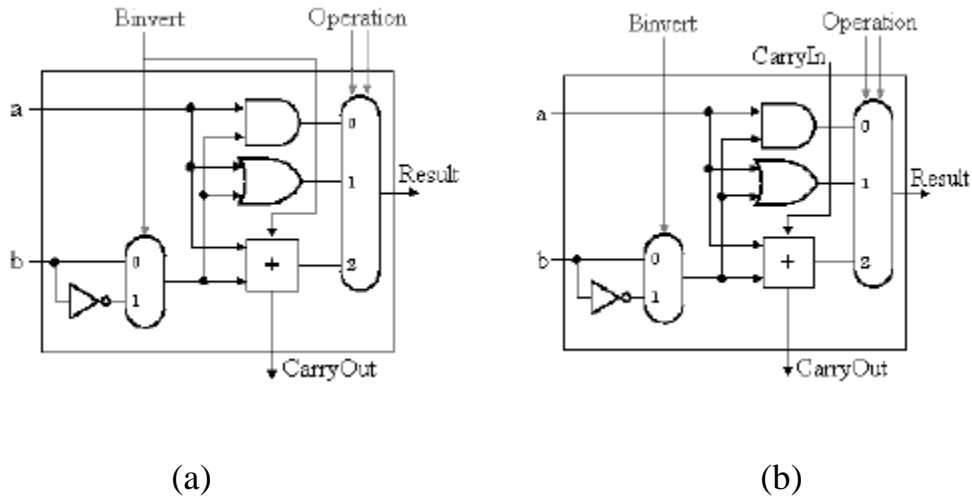
(b)



(c)

**Figure 3.7.** Full adder circuit (a) sum-of-products form from above-listed truth table, (b) *CarryOut* production, and (c) one-bit full adder with carry - adapted from [Maf01].

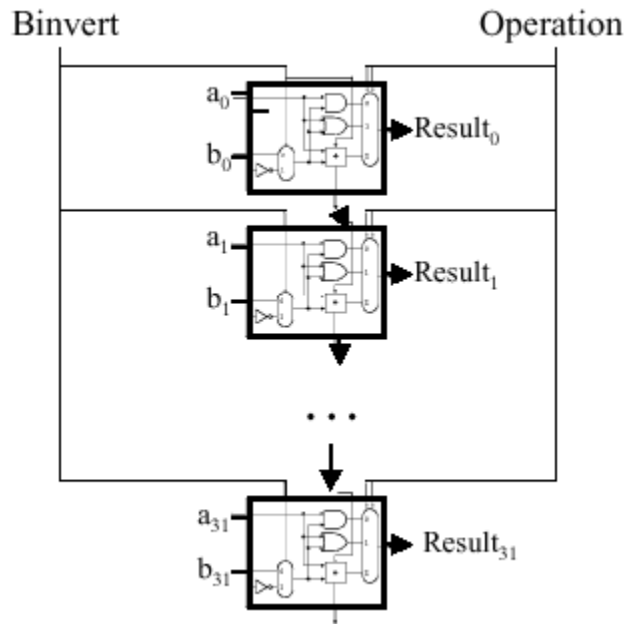
Recalling the symbol for the one-bit adder, we can add an addition operation to the one-bit ALU shown in Figure 3.6. This is done by putting two control lines on the output mux, and by having an additional control line that inverts the *b* input (shown as "Binvert") in Figure 3.9).



**Figure 3.9.** One-bit ALU with three operations: *and*, *or*, and addition: (a) Least significant bit, (b) Remaining bits - adapted from [Maf01].

### 3.2.3. 32-bit ALU Design

The final implementation of the preceding technique is in a 32-bit ALU that incorporates the *and*, *or*, and addition operations. The 32-bit ALU can be simply constructed from the one-bit ALU by chaining the carry bits, such that  $\text{CarryIn}_{i+1} = \text{CarryOut}_i$ , as shown in Figure 3.10.



**Figure 3.10.** 32-bit ALU with three operations: *and*, *or*, and addition - adapted from [Maf01].

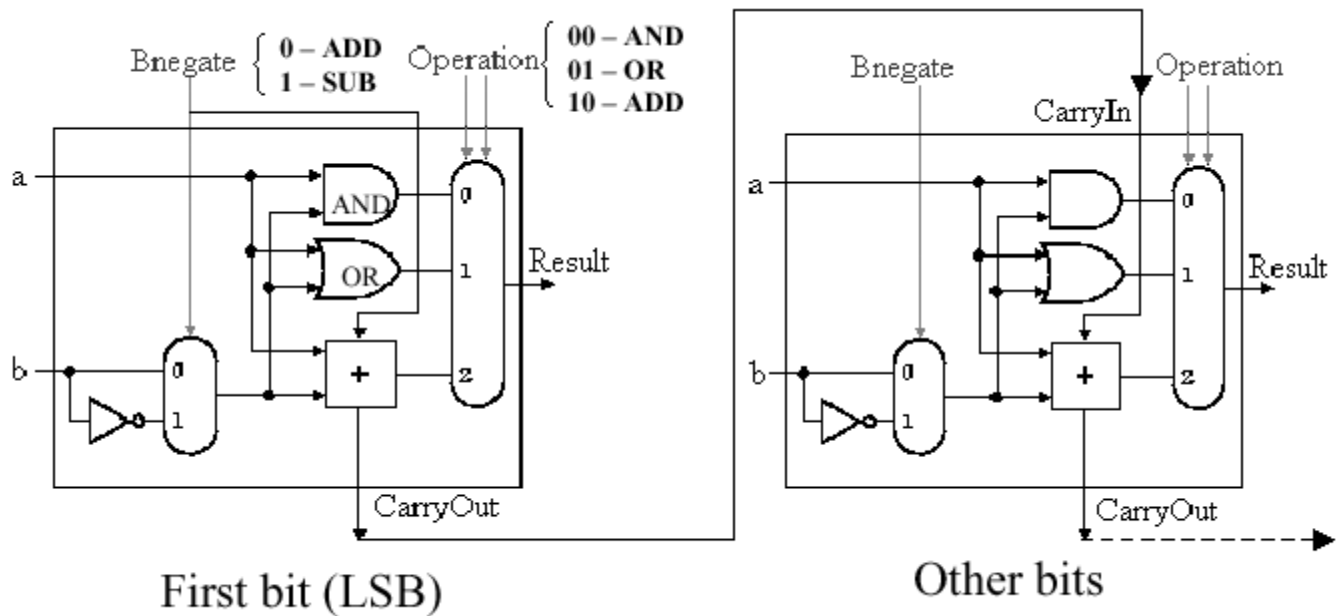
This yields a composite ALU with two 32-bit input vectors **a** and **b**, whose *i*-th bit is denoted by *a*<sub>*i*</sub> and *b*<sub>*i*</sub>, where *i* = 0..31. The result is also a 32-bit vector, and there are two control buses -

one for Binvert, and one for selecting the operation (using the mux shown in Figure 3.9). There is one CarryOut bit (at the bottom of Figure 3.10), and no CarryIn.

We next examine the MIPS ALU and how it supports operations such as shifting and branching.

### 3.2.4. MIPS ALU Design

We begin by assuming that we have the generic one-bit ALU designed in Sections 3.2.1-3.2.3, and shown below:



Here, the *Bnegate* input is the same as the *Binvert* input in Figure 3.9, and we assume that we have three control inputs to the mux whose control line configuration is associated with an operation, as follows:

Operations: AND, OR, ADD, SUB  
Control lines: 000 001 010 110

**3.2.4.1. Support for the slt Instruction.** The slt instruction (set on less-than) has the following format:

**slt rd, rs, rt**

where *rd* = 1 if *rs* < *rt*, and *rd* = 0 otherwise.

Observe that the inputs *rs* and *rt* can represent high-level language input variables *A* and *B*. Thus, we have the following implication:

$$A < B \Rightarrow A - B < 0,$$

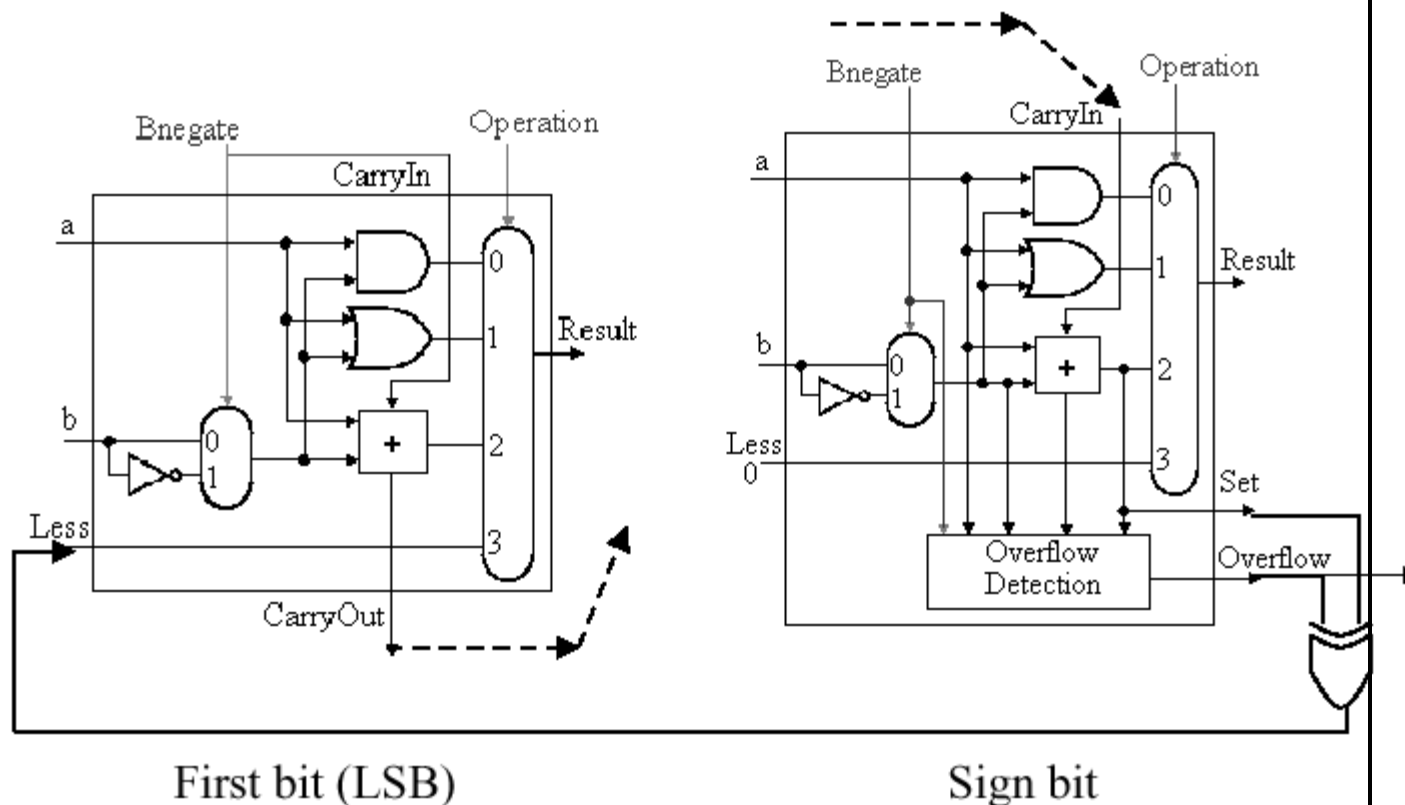
which is implemented as follows:

**Step 1.** Perform subtraction using negation and a full adder

**Step 2.** Check most significant bit (sign bit)

**Step 3.** Sign bit tells us whether or not  $A < B$

To implement *slt*, we need (a) new input line called *Less* that goes directly to the mux, and (b) a new control code (111) to select the *slt* operation. Unfortunately, the result for *slt* cannot be taken directly as the output from the adder. Instead, we need a new output line called *Set* that is used only for the *slt* instruction. Overflow detection logic is also associated with this bit. The additional logic that supports *slt* is shown in Figure 3.11.



**Figure 3.11.** One-bit ALU with additional logic for *slt* operation - adapted from [Maf01].

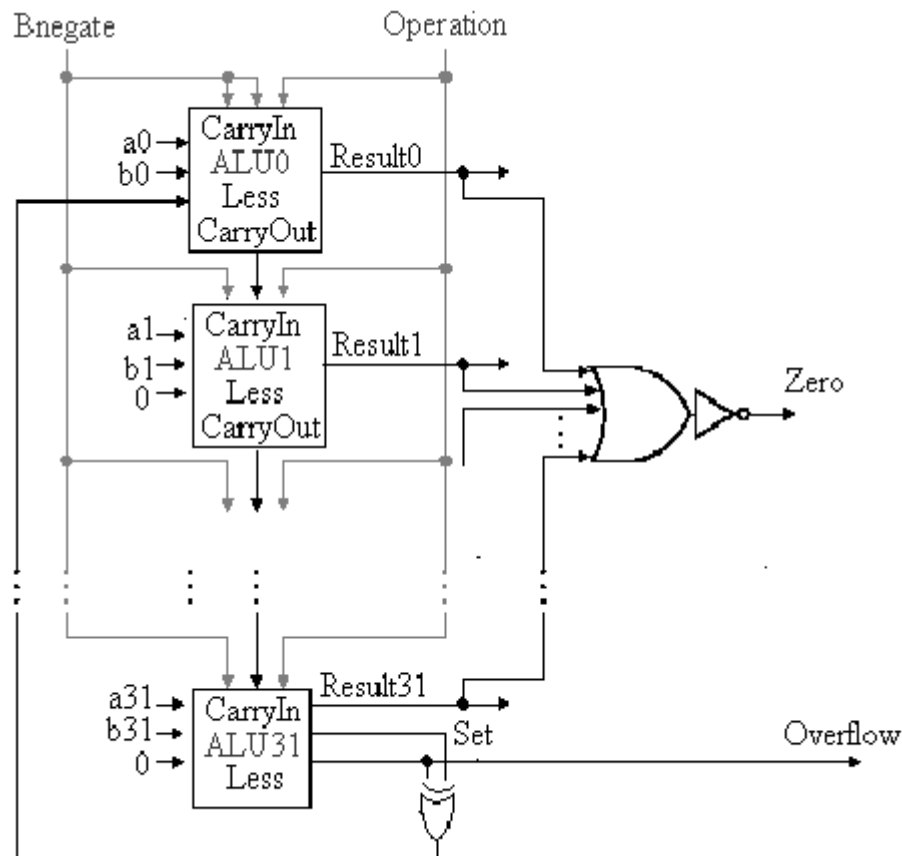
Thus, for a 32-bit ALU, the additional cost of the *slt* instruction is (a) augmentation of each of 32 muxes to have three control lines instead of two, (b) augmentation of each of 32 one-bit ALU's

control signal structure to have an additional (*Less*) input, and (c) the addition of overflow detection circuitry, a *Set* output, and an *xor* gate on the output of the sign bit.

**3.2.4.2. Support for the bne Instruction.** Recall the branch-on-not-equal instruction *bne* r1, r2, Label, where r1 and r2 denote registers and Label is a branch target label or address. To implement *bne*, we observe that the following implication holds:

$$A - B = 0 \Rightarrow A = B .$$

then add hardware to test if the comparison between A and B implemented as (A - B) is zero. Again, this can be done using negation and the full adder that we have already designed as part of the ALU. The additional step is to *or* all 32 results from each of the one-bit ALUs, then invert the output of the *or* operation. Thus, if all 32 bits from the one-bit full adders are zero, then the output of the *or* gate will be zero (inverted, it will be one). Otherwise, the output of the *or* gate will be one (inverted, it will be zero). We also need to consider A - B, to see if there is overflow when A = 0. A block diagram of the hardware modification is shown in Figure 3.12.

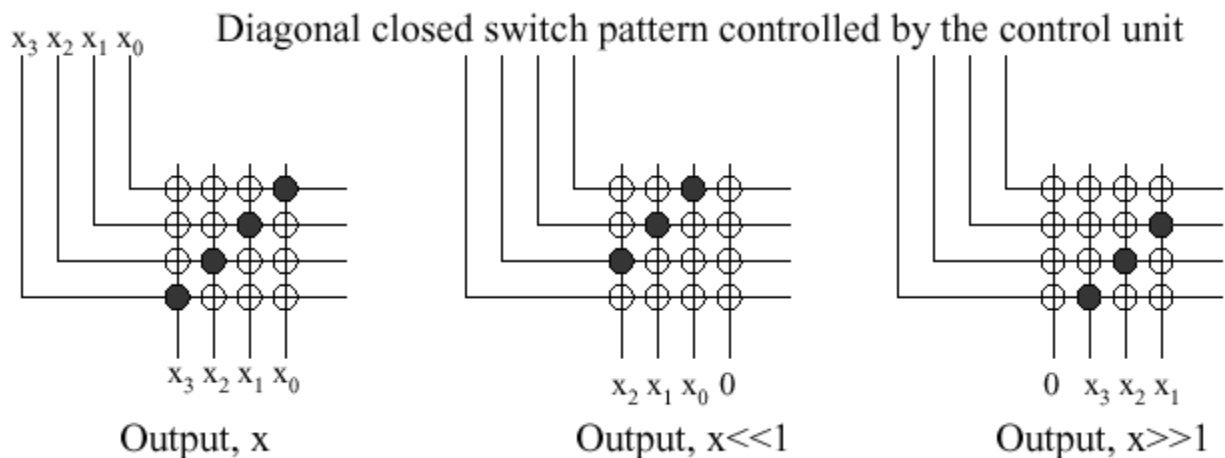


**Figure 3.12.** 32-bit ALU with additional logic to support *bne* and *slt* instructions - adapted from [Maf01].

Here, the additional hardware involves 32 separate output lines from the 342 one-bit adders, as well as a cascade of *or* gates to implement a 32-input *nor* gate (which doesn't exist in practice, due to excessive fan-in requirement).

**3.2.4.3. Support for Shift Instructions.** Considering the *sll*, *srl*, and *sra* instructions, these are supported in the ALU under design by adding a data line for the shifter (both left and right). However, the shifters are much more easily implemented at the transistor level (e.g., outside the ALU) rather than trying to fit more circuitry onto the ALU itself.

In order to implement a shifter external to the ALU, we consider the design of a *barrel shifter*, shown schematically in Figure 3.13. Here, the closed switch pattern, denoted by black filled circles, is controlled by the CPU through control lines to a mux or decoder. This allows data line  $x_i$  to be sent to output  $x_j$ , where  $i$  and  $j$  can be unequal.

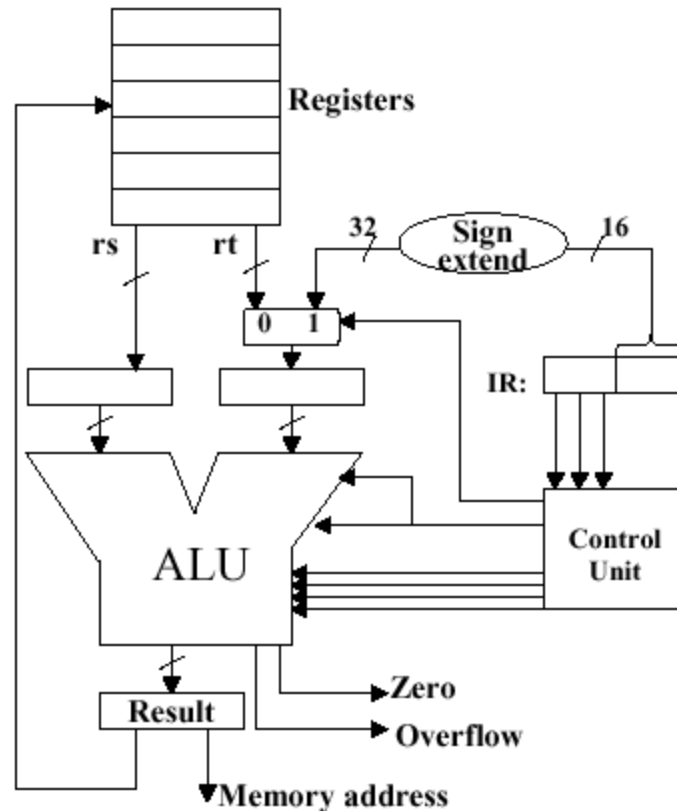


**Figure 3.13.** Four bit barrel shifter, where " $x \gg 1$ " denotes a shift amount greater than one - adapted from [Maf01].

This type of  $N$ -bit shifter is well understood and easy to construct, but has space complexity of  $O(N^2)$ .

**3.2.4.4. Support for Immediate Instructions.** In the MIPS immediate instruction formats, the first input to the ALU is the first register (we'll call it  $rs$ ) in the immediate command, while the second input is either data from a register  $rt$  or a zero or sign-extended constant (immediate). To support this type of instruction, we need to add a mux at the second input of the ALU, as shown in Figure 3.14. This allows us to select whether  $rt$  or the sign-extended immediate is input to the ALU.





**Figure 3.14.** Supporting immediate instructions on a MIPS ALU design, where IR denotes the instruction register, and  $(/^{16})$  denotes a 16-bit parallel bus - adapted from [Maf01].

### 3.2.5. ALU Performance Issues

When estimating or measuring ALU performance, one wonders if a 32-bit ALU is as fast as a 1-bit ALU - what is the degree of parallelism, and do all operations execute in parallel? In practice, some operations on  $N$ -bit operands (e.g., addition with sequential propagation of carries) take  $O(N)$  time. Other operations, such as bitwise logical operations, take  $O(1)$  time. Since addition can be implemented in a variety of ways, each with a certain level of parallelism, it is wise to consider the possibility of a full adder being a computational bottleneck in a simple ALU.

We previously discussed the ripple-carry adder (Figure 3.10) that propagates the carry bit from stage  $i$  to stage  $i+1$ . It is readily seen that, for an  $N$ -bit input,  $O(N)$  time is required to propagate the carry to the most significant bit. In contrast, the fastest  $N$ -bit adder uses  $O(\log_2 N)$  stages in a tree-structured configuration with  $N-1$  one-bit adders. Thus, the complexity of this technique is  $O(\log_2 N)$  work. In a sequential model of computation, this translates to  $O(\log_2 N)$  time. If one is adding smaller numbers (e.g., up to 10-bit integers with current memory technology), then a *lookup table* can be used that (1) forms a memory address  $A$  by concatenating binary representations of the two operands, and (2) produces a result stored in memory that is accessed using  $A$ . This takes  $O(1)$  time, that is dependent upon memory bandwidth.

An intermediate approach between these extremes is to use a *carry-lookahead adder* (CLA). Suppose we do not know the value of the carry-in bit (which is usually the case). We can express the generation (g) of a carry bit for the i-th position of two operands *a* and *b*, as follows:

$$g_i = a_i b_i ,$$

where the i-th bits of *a* and *b* are *and*-ed. Similarly, the propagated carry is expressed as:

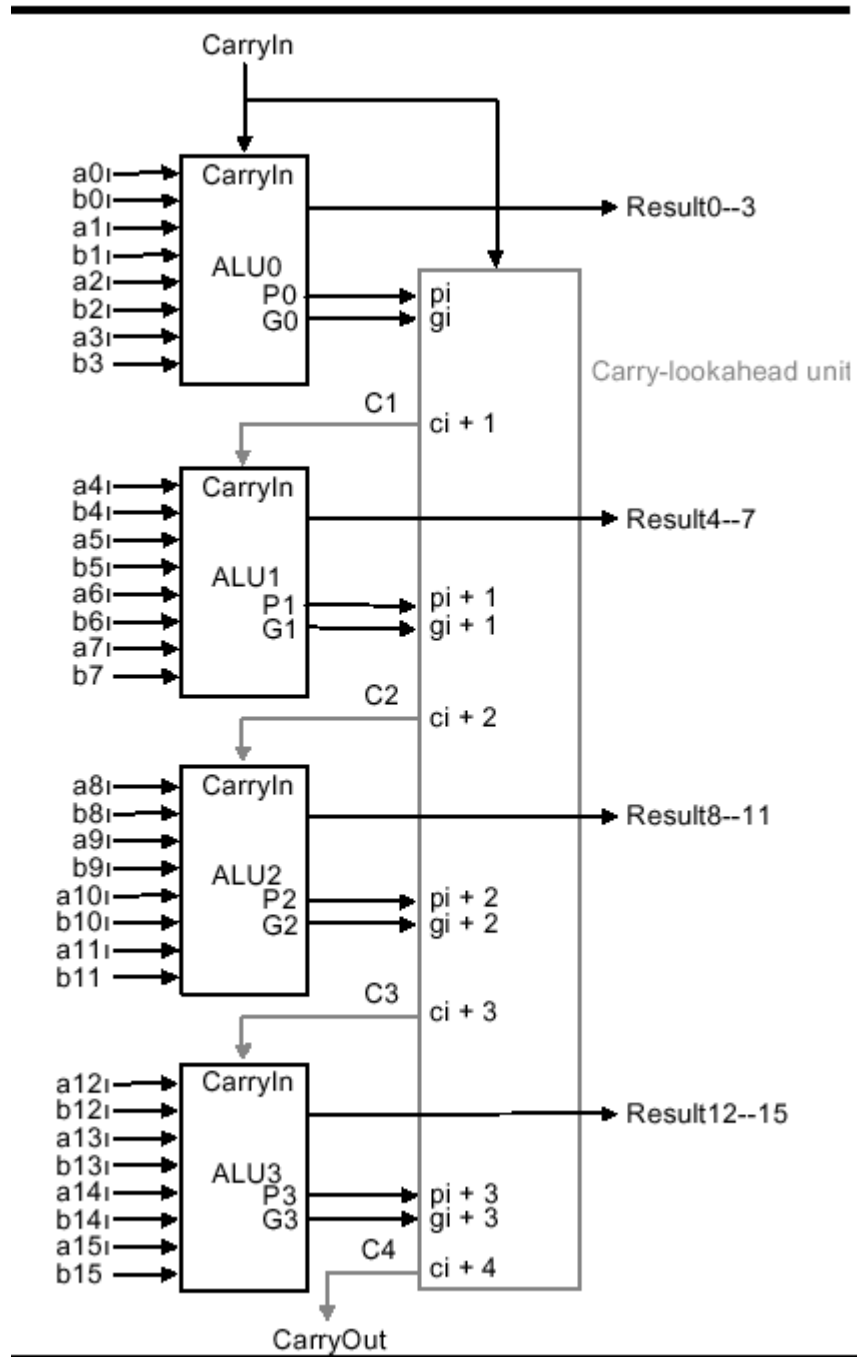
$$p_i = a_i + b_i ,$$

where the i-th bits of *a* and *b* are *or*-ed. This allows us to recursively express the carry bits in terms of the carry-in  $c_0$ , as follows:

$$\begin{array}{ll} c_1 = g_0 + p_0 c_0 & \\ c_2 = g_1 + p_1 c_1 & c_2 = g_1 + p_1 g_0 + p_1 p_0 c_0 \\ c_3 = g_2 + p_2 c_2 & c_3 = \\ c_4 = g_3 + p_3 c_3 & c_4 = \end{array}$$

Did we get rid of the ripple? (Well, sort of...) What we did was transform the work involved in carry propagation from the adder circuitry to a large equation for  $c_N$ . However, this equation must still be computed in hardware. (*Lesson:* In computing, you don't get much for free.)

Unfortunately, it is prohibitively costly to build a CLA circuit for operands as large as 16 bits. Instead, we can use the CLA principle to create a two-tiered circuit, for example, at the bottom level an array of four 4-bit full adders (economical to construct), connected at the top level by a CLA, as shown below:



Using a two-level CLA architecture, where lower- (upper-)case g and p denote the first (second) level generates and carries, we have the following equations:

$$P_0 = p_3 + p_2 + p_1 + p_0$$

$$P_1 = p_7 + p_6 + p_5 + p_4$$

$$P_2 = p_{11} + p_{10} + p_9 + p_8$$

$$P_3 = p_{15} + p_{14} + p_{13} + p_{12}$$

$$\begin{aligned}
G_0 &= g_3 + p_3g_2 + p_3p_2g_1 + p_3p_2p_1g_0 \\
G_1 &= g_7 + p_7g_6 + p_7p_6g_5 + p_7p_6p_5g_4 \\
G_2 &= g_{11} + p_{11}g_{10} + p_{11}p_{10}g_9 + p_{11}p_{10}p_9g_8 \\
G_3 &= g_{15} + p_{15}g_{14} + p_{15}p_{14}g_{13} + p_{15}p_{14}p_{13}g_{12}
\end{aligned}$$

Assuming that *and* as well as *or* gates have the same propagation delay, comparative analysis of the ripple carry vs. carry lookahead adders reveals that the total time to compute a CLA result is the summation of all gate delays along the longest path through the CLA. In the case of the 16-bit adder exemplified above, the CarryOut signals  $c_{16}$  and  $C_4$  define the longest path. For the ripple carry adder, this path has length  $2(16) = 32$ .

For the two-level CLA, we get two levels of logic in terms of the architecture (P and G versus p and g).  $P_i$  is specified in one level of logic using  $p_i$ .  $G_i$  is specified in one level of logic using  $p_i$  and  $g_i$ . Also,  $p_i$  and  $g_i$  each represent one level of logic computed in terms of inputs  $a_i$  and  $b_i$ . Thus, the CLA critical path length is  $2 + 2 + 1 = 5$ , which means that two-level 16-bit CLA is  $6.4 = 32/5$  times faster than a 16-bit ripple carry adder.

It is also useful to note that the logic equation for a one-bit adder can be expressed more simply with *xor* logic, for example:

$$A + B = A \text{ xor } B \text{ xor } \text{CarryIn} .$$

In some technologies, *xor* is more efficient than *and/or* gates. Also, processors are now designed in CMOS technology, which allows fewer muxes (this also applies to the barrel shifter). However, the design principles are similar.

### 3.2.6. Summary

We have shown that it is feasible to build an ALU to support the MIPS ISA. The key idea is to use a multiplexer to select the output from a collection of functional units operating in parallel. We can replicate a 1-bit ALU that uses this principle, with appropriate connections between replicates, to produce an N-bit ALU.

Important things to remember about ALUs are: (a) all of the gates are working in parallel, (b) the speed of a gate is affected by the number of inputs (degree of *fan-in*), and (c) the speed of a circuit depends on the number of gates in the longest computational path through the circuit (this can vary per operation). Finally, we have shown that changes in architectural organization can improve performance, similar to better algorithms in software.

### 3.3. Boolean Multiplication and Division

#### [Reading Assignments and Exercises](#)

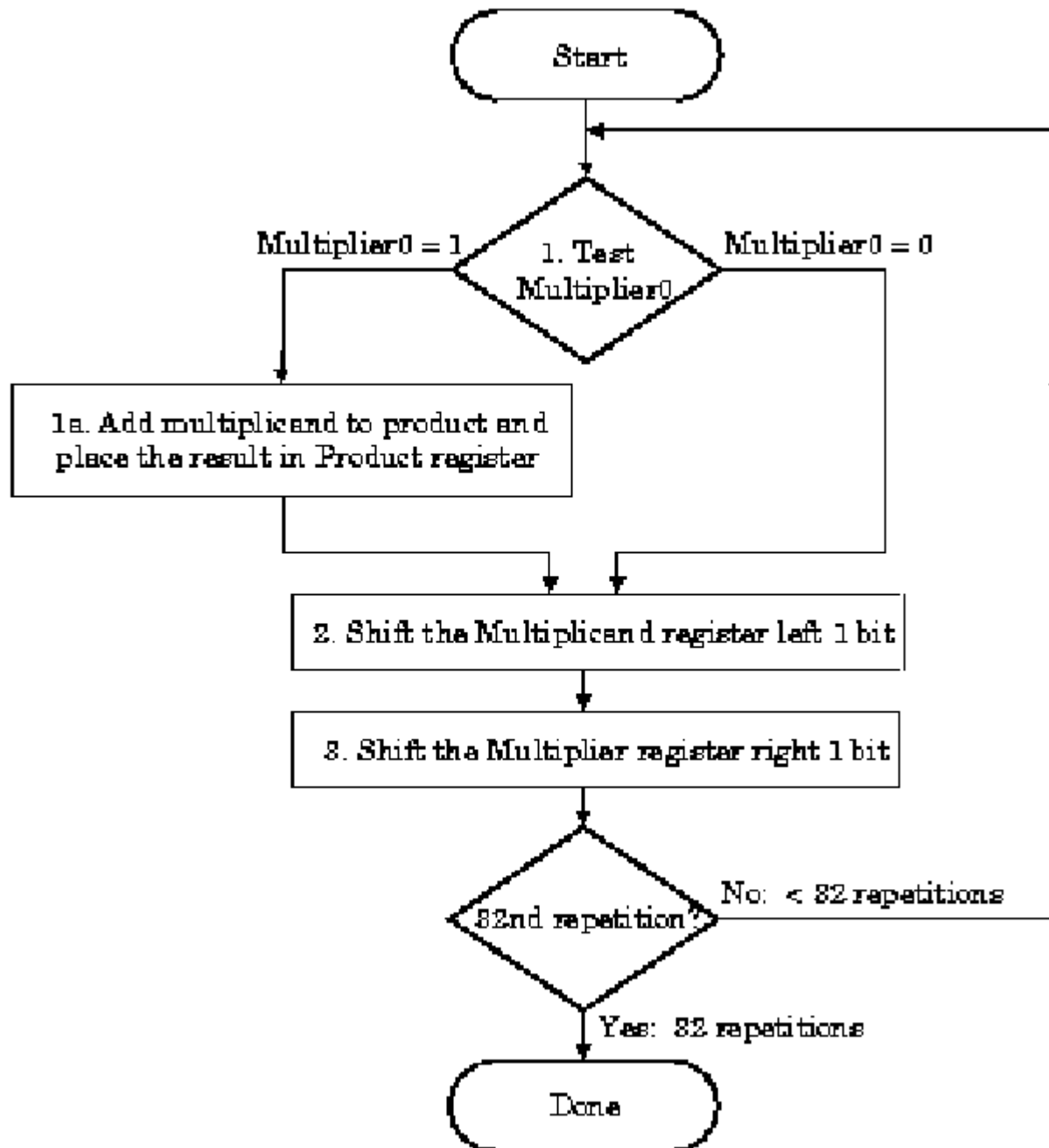
Multiplication is more complicated than addition, being implemented by shifting as well as addition. Because of the partial products involved in most multiplication algorithms, more time and more circuit area is required to compute, allocate, and sum the partial products to obtain the multiplication result.

### 3.3.1. Multiplier Design

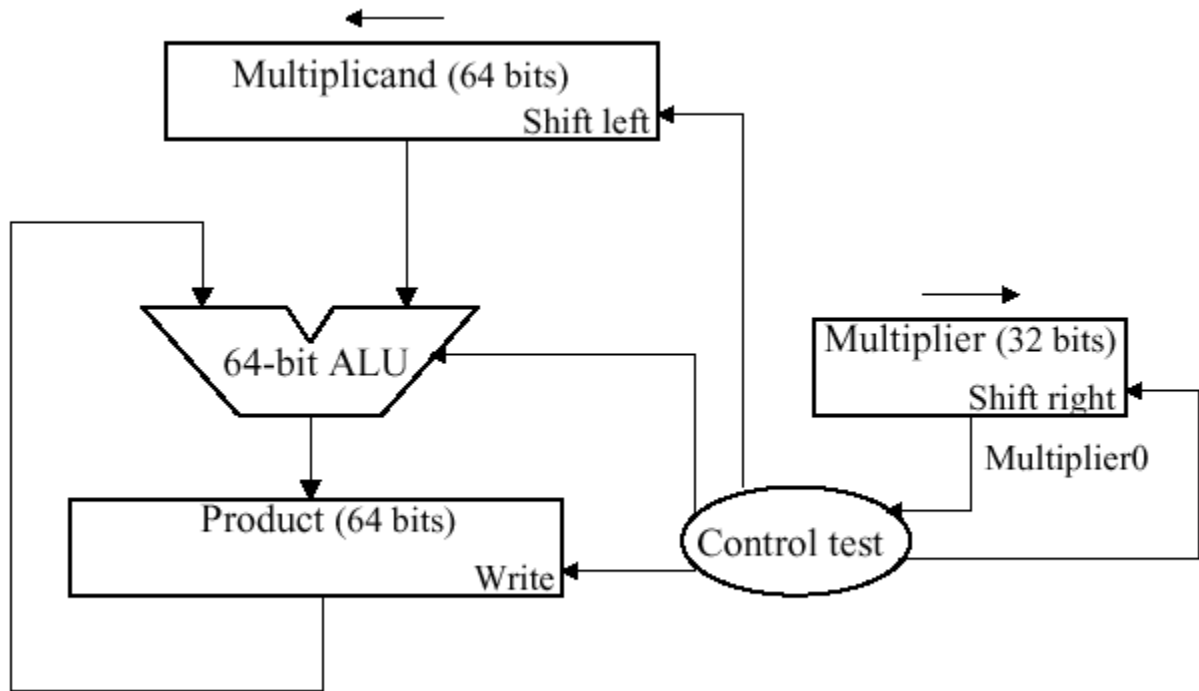
We herein discuss three versions of the multiplier design based on the *pencil-and-paper algorithm for multiplication* that we all learned in grade school, which operates on Boolean numbers, as follows:

```
Multiplicand: 0010 # Stored in register r1
Multiplier:  x 1101 # Stored in register r2
-----
      Partial Prod 0010 # No shift for LSB of Multiplier
"    " 0000 # 1-bit shift of zeroes (can omit)
"    " 0010 # 2-bit shift for bit 2 of Multiplier
"    " 0010 # 3-bit shift for bit 3 of Multiplier
----- # Zero-fill the partial products and add
PRODUCT 0011010 # Sum of all partial products -> r3
```

A flowchart of this algorithm, adapted for multiplication of 32-bit numbers, is shown in Figure 3.15, below, together with a schematic representation of a simple ALU circuit that implements this version of the algorithm. Here, the multiplier and the multiplicand are shifted relative to each other, which is more efficient than shifting the partial products alone.



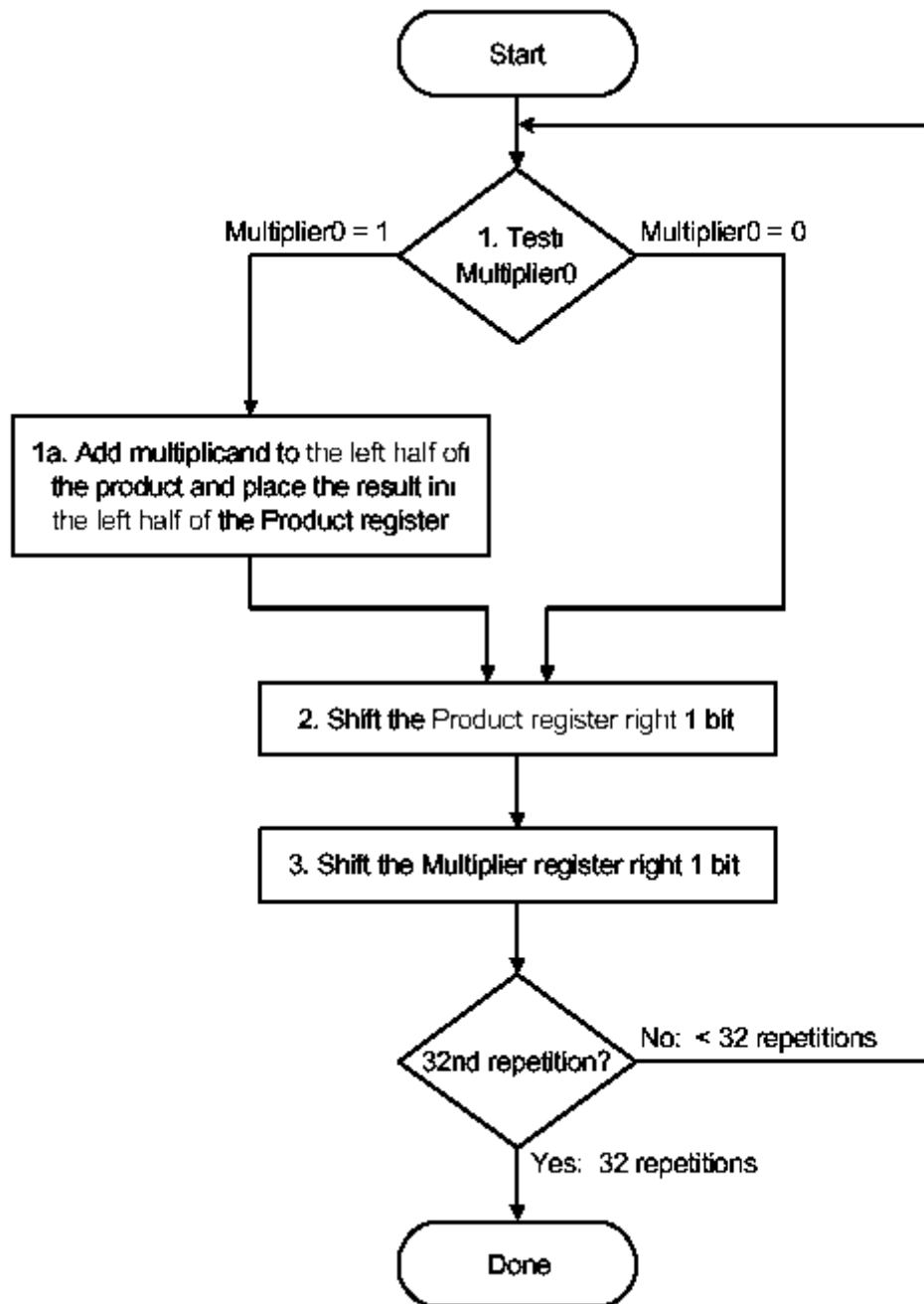
(a)



(b)

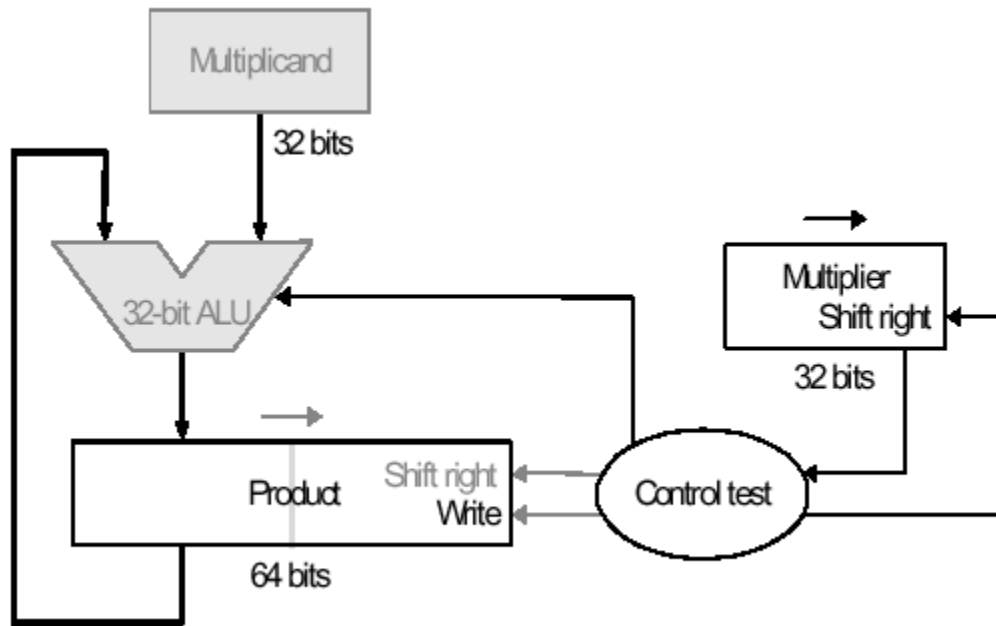
**Figure 3.15.** Pencil-and-paper multiplication of 32-bit Boolean number representations: (a) algorithm, and (b) simple ALU circuitry - adapted from [Maf01].

The second version of this algorithm is shown in Figure 3.16. Here, the product is shifted with respect to the multiplier, and the multiplicand is shifted after the product register has been shifted. A 64-bit register is used to store both the multiplicand and the product.



(a)

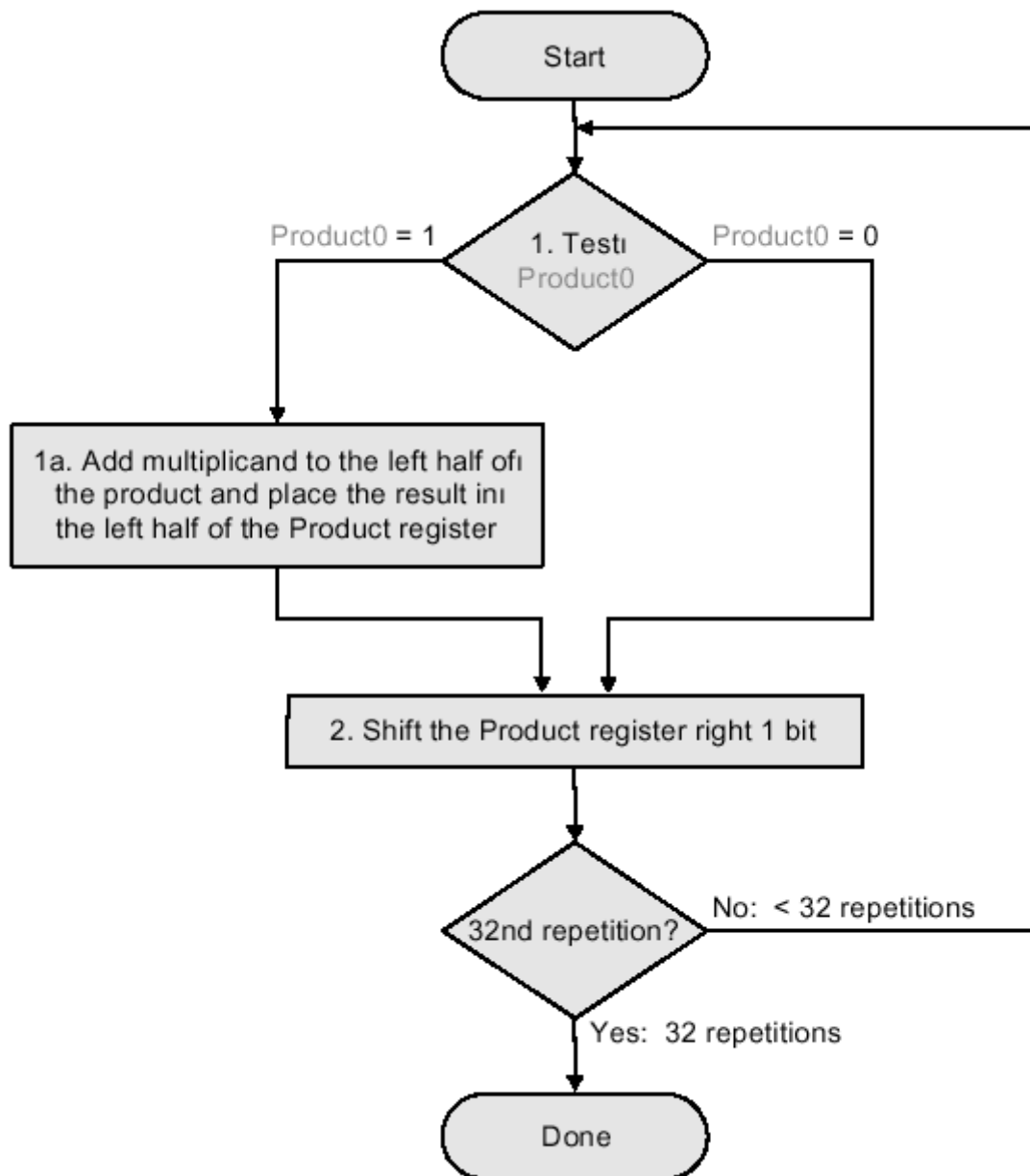




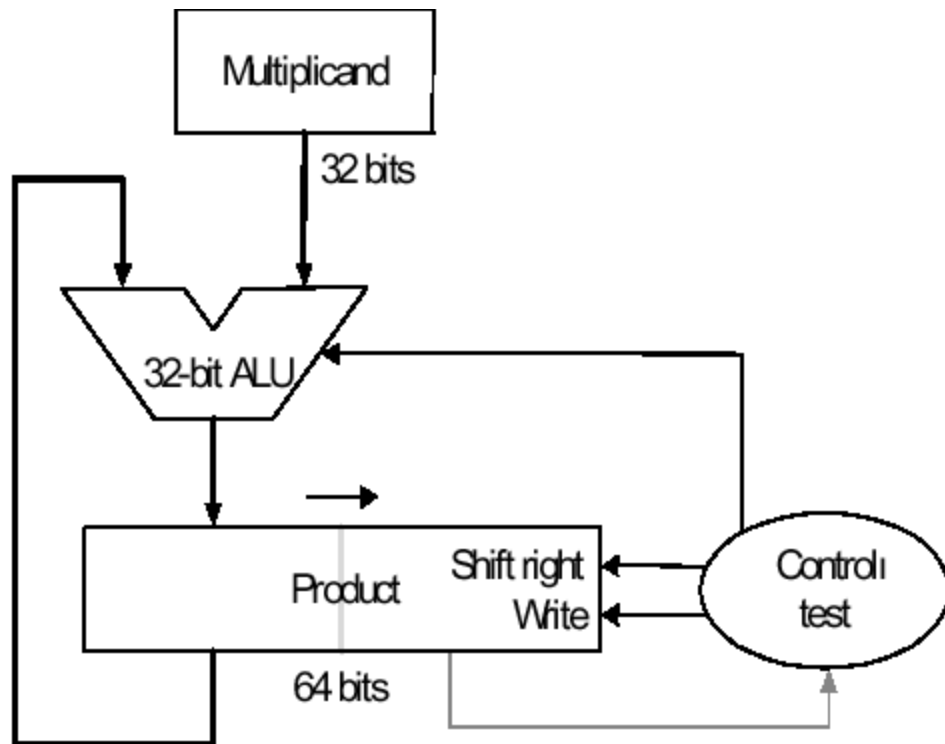
(b)

**Figure 3.16.** Second version of pencil-and-paper multiplication of 32-bit Boolean number representations: (a) algorithm, and (b) schematic diagram of ALU circuitry - adapted from [Maf01].

The final version puts results in the product register if and only if the least significant bit of the product produced on the previous iteration is one-valued. The product register only is shifted. This reduces by approximately 50 percent the amount of shifting that has to be done, which reduces time and hardware requirements. The algorithm and ALU schematic diagram is shown in Figure 3.17.



(a)



(b)

**Figure 3.17.** Third version of pencil-and-paper multiplication of 32-bit Boolean number representations: (a) algorithm, and (b) schematic diagram of ALU circuitry - adapted from [Maf01].

Thus, we have the following shift-and-add scheme for multiplication:

The preceding algorithms and circuitry does not hold for signed multiplication, since the bits of the multiplier no longer correspond to shifts of the multiplicand. The following example is illustrative:

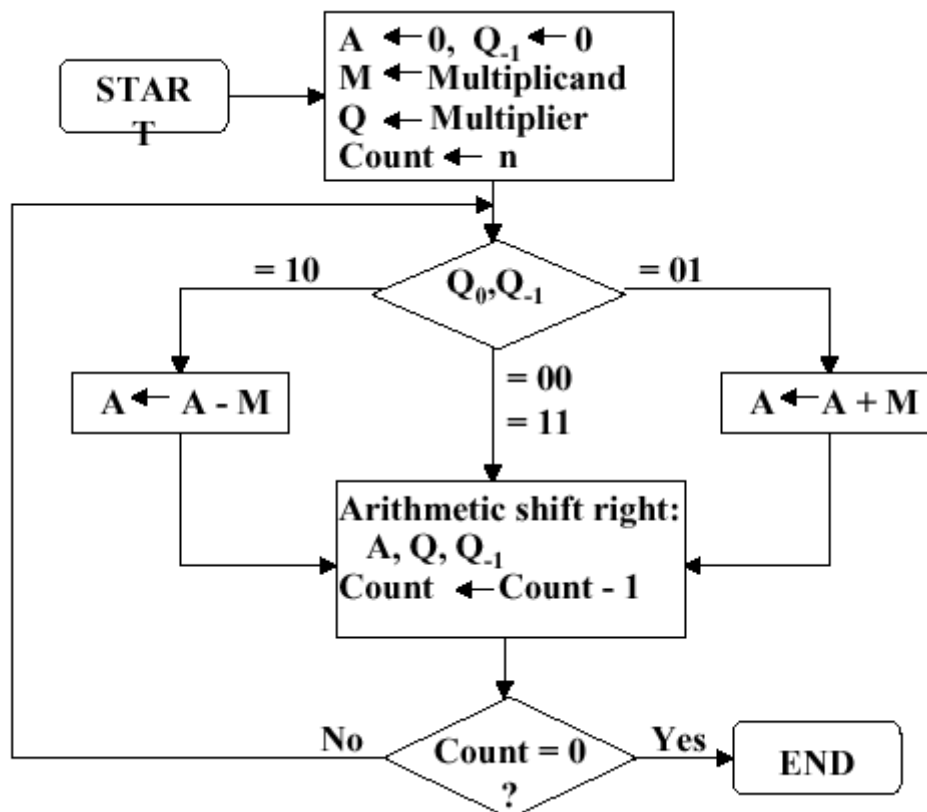
	Unsigned	Signed
1011	11	-5
x 1101	13	-3
<u>10001111</u>	143	<del>-143</del>

- Partial solution for negative multiplicands

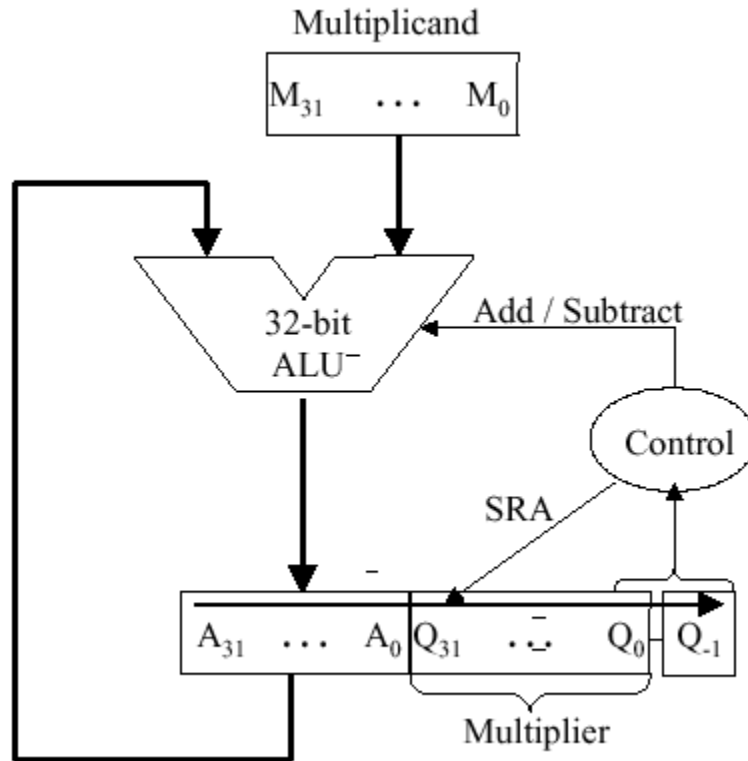
1001 (9)	1001 (-7)
x 0011 (3)	x 0011 (3)
<u>00001001</u> 1001 x 2 <sup>0</sup>	<u>11111001</u> (-7) x 2 <sup>0</sup> = (-7)
00010010 1001 x 2 <sup>1</sup>	11110010 (-7) x 2 <sup>1</sup> = (-14)
<u>00011011</u> (27)	<u>11101011</u> (-21)

- No straightforward solution if multiplier is negative

A solution to this problem is Booth's Algorithm, whose flowchart and corresponding schematic hardware diagram are shown in Figure 3.18. Here, the examination of the multiplier is performed with *lookahead* toward the next bit. Depending on the bit configuration, the multiplicand is positively or negatively signed, and the multiplier is shifted or unshifted.



(a)



(b)

**Figure 3.18.** Booth's procedure for multiplication of 32-bit Boolean number representations: (a) algorithm, and (b) schematic diagram of ALU circuitry - adapted from [Maf01].

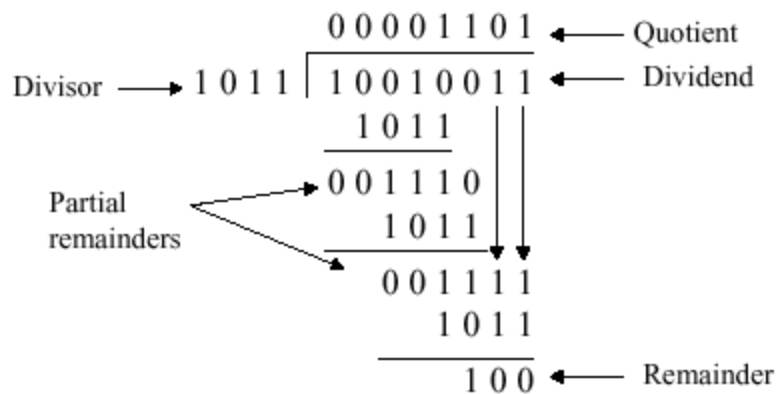
Observe that Booth's algorithm requires only the addition of a subtraction step and the comparison operations for the two-bit codes, versus the one-bit comparison in the preceding three algorithms. An example of Booth's algorithm follows:

	7	(0 1 1 1)			
	x 3	(0 0 1 1)			
	<u>A</u>	<u>Q</u>	<u>Q<sub>-1</sub></u>	<u>M</u>	
Initial values	0000	0011	0	0111	
	1001	0011	0	0111	A = A - M } 1
	1100	1001	1	0111	
	1110	0100	1	0111	Shift } 2
	0101	0100	1	0111	A = A + M } 3
	0010	1010	0	0111	
	0001	0101	0	0111	Shift } 4

Here  $N = 4$  iterations of the loop are required to produce a product from two  $N = 4$  digit operands. Four shifts and two subtractions are required. From the analysis of the algorithm shown in Figure 3.18a, it is easily seen that the maximum work for multiplying two  $N$ -bit numbers is given by  $O(N)$  shift and addition operations. From this, the worst-case computation time can be computed given CPI for the shift and addition instructions, as well as cycle time of the ALU.

### 3.3.2. Design of Arithmetic Division Hardware

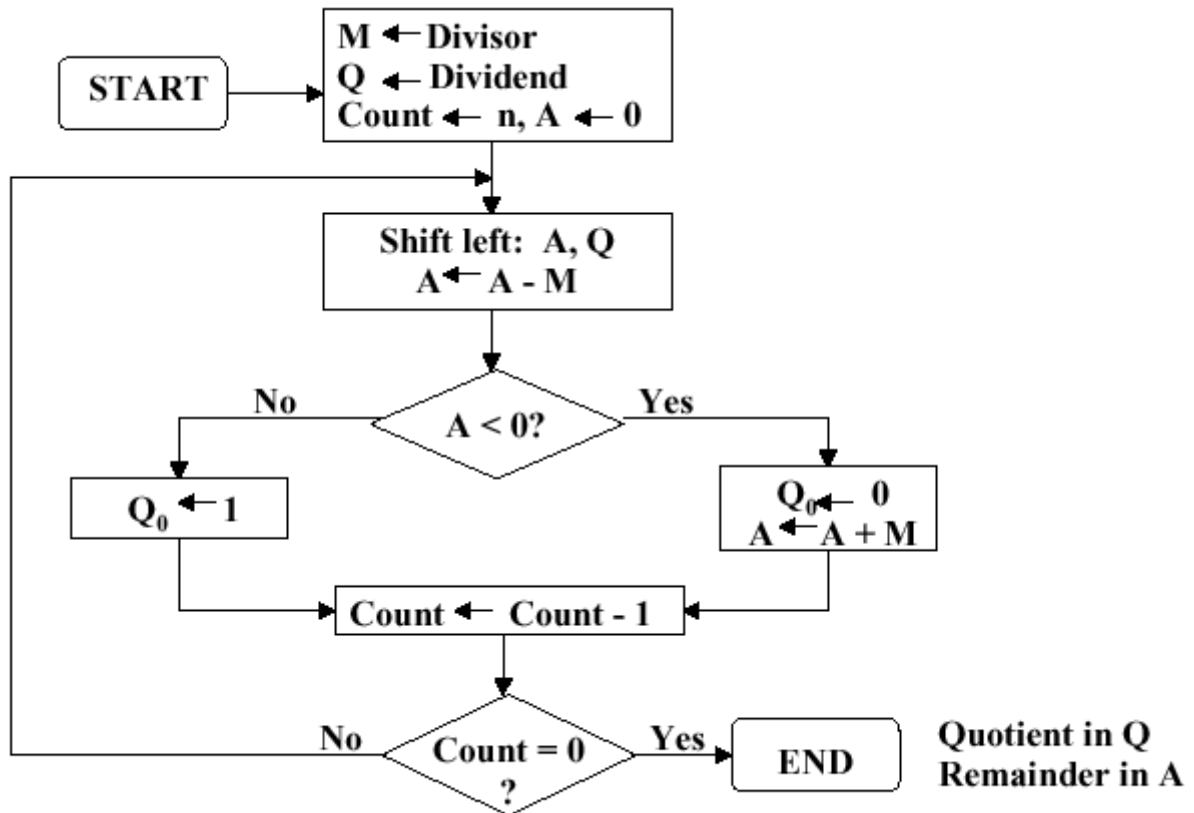
Division is a similar operation to multiplication, especially when implemented using a procedure similar to the algorithm shown in Figure 3.18a. For example, consider the pencil-and-paper method for dividing the byte 10010011 by the nybble 1011:



The governing equation is as follows:

$$\text{Dividend} = \text{Quotient} \cdot \text{Divisor} + \text{Remainder} .$$

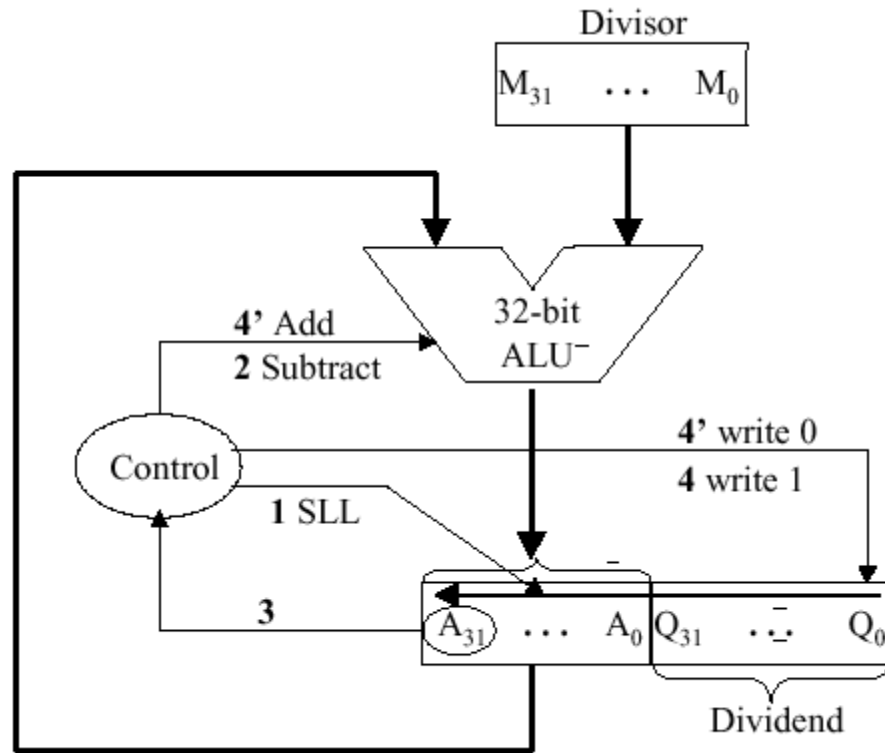
**3.3.2.1. Unsigned Division.** The *unsigned* division algorithm that is similar to Booth's algorithm is shown in Figure 3.19a, with an example shown in Figure 3.19b. The ALU schematic diagram is given in Figure 3.19c. The analysis of the algorithm and circuit is very similar to the preceding discussion of Booth's algorithm.



(a)

A	Q	M = 0011	
0000	0111	Initial values	
0000	1110	Shift	1
1101		A = A - M	
0000	1110	A = A + M	
0001	1100	Shift	2
1110		A = A - M	
0001	1100	A = A + M	
0011	1000	Shift	3
0000		A = A - M	
0000	1001	Q₀ = 1	
0001	0010	Shift	4
1110		A = A - M	
0001	0010	A = A + M	

(b)



(c)

**Figure 3.19.** Division of 32-bit Boolean number representations: (a) algorithm, (b) example using division of the unsigned integer 7 by the unsigned integer 3, and (c) schematic diagram of ALU circuitry - adapted from [Maf01].

**3.3.2.2. Signed Division.** With signed division, we negate the quotient if the signs of the divisor and dividend disagree. The remainder and the dividend must have the same signs. The governing equation is as follows:

$$\text{Remainder} = \text{Divident} - (\text{Quotient} \cdot \text{Divisor}) ,$$

and the following four cases apply:

$$(+7) / (+3): \quad Q = 2; \quad R = 1$$

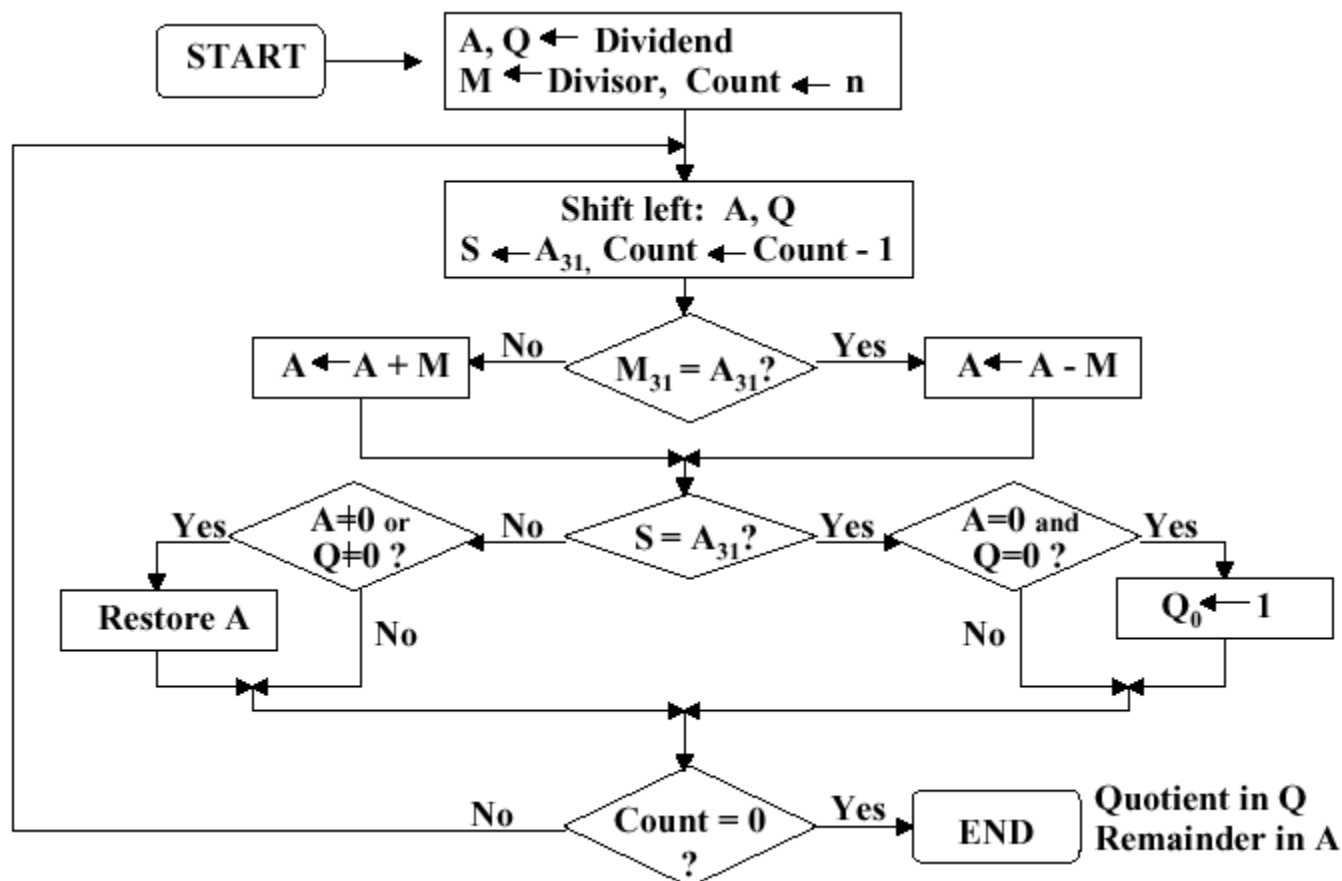
$$(-7) / (+3): \quad Q = -2; \quad R = -1$$

$$(+7) / (-3): \quad Q = -2; \quad R = 1$$

$$(-7) / (-3): \quad Q = 2; \quad R = -1$$

We present the preceding division algorithm, revised for signed numbers, as shown in Figure 3.20a. Four examples, corresponding to each of the four preceding sign permutations, are given in Figure 3.20b and 3.20c.





(a)

A	Q	M = 0011
0000	0111	Initial values
0000	1110	Shift
1101		Subtract
0000	1110	Restore
0001	1100	Shift
1110		Subtract
0001	1100	Restore
0011	1000	Shift
0000		Subtract
0000	1001	Q <sub>0</sub> = 1
0001	0010	Shift
1110		Subtract
0001	0010	Restore

(7) / (3)

A	Q	M = 1101
0000	0111	Initial values
0000	1110	Shift
1101		Add
0000	1110	Restore
0001	1100	Shift
1110		Add
0001	1100	Restore
0011	1000	Shift
0000		Add
0000	1001	Q <sub>0</sub> = 1
0001	0010	Shift
1110		Add
0001	0010	Restore

(7) / (-3)

(b)

A	Q	M = 0011		A	Q	M = 1101	
1111	1001	Initial values		1111	1001	Initial values	
1111	0010	Shift	} 1	1111	0010	Shift	} 1
0010		Add		0010		Subtract	
1111	0010	Restore		1111	0010	Restore	
1110	0100	Shift	} 2	1110	0100	Shift	} 2
0001		Add		0001		Subtract	
1110	0100	Restore		1110	0100	Restore	
1100	1000	Shift	} 3	1100	1000	Shift	} 3
1111		Add		1111		Subtract	
1111	1001	Q <sub>0</sub> = 1		1111	1001	Q <sub>0</sub> = 1	
1111	0010	Shift	} 4	1111	0010	Shift	} 4
0010		Add		0010		Subtract	
1111	0010	Restore		1111	0010	Restore	
(-7) / (3)				(-7) / (-3)			

(c)

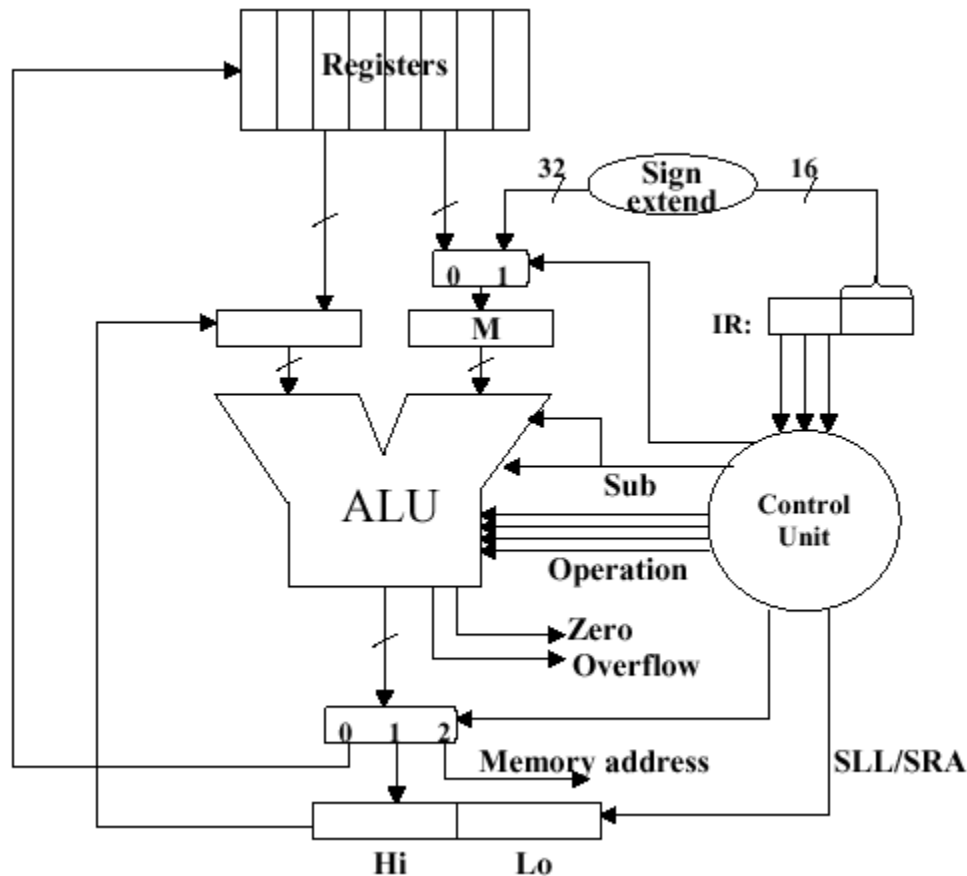
**Figure 3.20.** Division of 32-bit Boolean number representations: (a) algorithm, and (b,c) examples using division of +7 or -7 by the integer +3 or -3; adapted from [Maf01].

**Self-Exercise.** Be able to trace each example shown in Figure 3.20b,c through the algorithm whose flowchart is given in Figure 3.20a. Know how each part of the algorithm works, and why it behaves that way. *Hint: This exercise, or a part of it, is likely to be an exam question.*

**3.3.2.3. Division in MIPS.** MIPS supports multiplication and division using existing hardware, primarily the ALU and shifter. MIPS needs one extra hardware component - a 64-bit register able to support sll and sra instructions. The upper (high) 32 bits of the register contains the remainder resulting from division. This is moved into a register in the MIPS register stack (e.g., \$t0) by themfhi command. The lower 32 bits of the 64-bit register contains the quotient resulting from division. This is moved into a register in the MIPS register stack by the mflo command.

In MIPS assembly language code, signed division is supported by the div instruction and unsigned division, by the divu instruction. MIPS hardware does not check for division by zero. *Thus, divide-by-zero exception must be detected and handled in system software.* A similar comment holds for overflow or underflow resulting from division.

Figure 3.21 illustrates the MIPS ALU that supports integer arithmetic operations (+, -, x, /).



**Figure 3.21.** MIPS ALU supporting the integer arithmetic operations (+,-,x,/), adapted from [Maf01].

**Self-Exercise.** Show how the MIPS ALU in Figure 3.21 supports the integer arithmetic operations (+,-,x,/), using the algorithms and hardware diagrams given thus far. *Hint: This exercise, or a part of it, is likely to be an exam question.*

### 3.4. Floating Point Arithmetic

#### Reading Assignments and Exercises

Floating point (FP) representations of decimal numbers are essential to scientific computation using *scientific notation*. The standard for floating point representation is the IEEE 754 Standard. In a computer, there is a tradeoff between range and precision - given a fixed number of binary digits (bits), precision can vary inversely with range. In this section, we overview decimal to FP conversion, MIPS FP instructions, and how registers are used for FP computations.

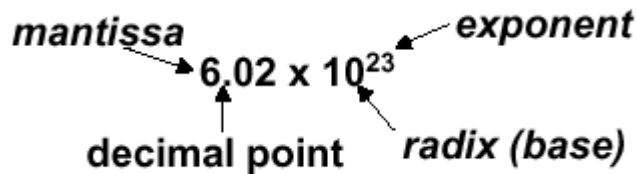
We have seen that an  $n$ -bit register can represent unsigned integers in the range  $0$  to  $2^n - 1$ , as well as signed integers in the range  $-2^{n-1}$  to  $-2^{n-1} - 1$ . However, there are very large numbers (e.g.,  $3.15576 \cdot 10^{25}$ ), very small numbers (e.g.,  $10^{-25}$ ), rational numbers with repeated digits (e.g.,  $2/3$

= 0.666666...), irrationals such as  $2^{1/2}$ , and transcendental numbers such as  $e = 2.718...$ , all of which need to be represented in computers for scientific computation to be supported.

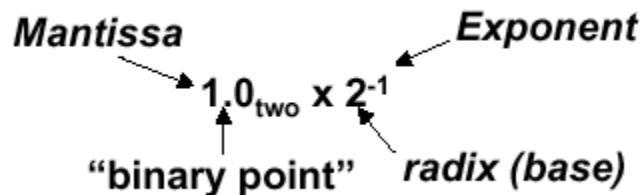
We call the manipulation of these types of numbers *floating point arithmetic* because the decimal point is not fixed (as for integers). In C, such variables are declared as the float datatype.

### 3.4.1. Scientific Notation and FP Representation

Scientific notation has the following configuration:



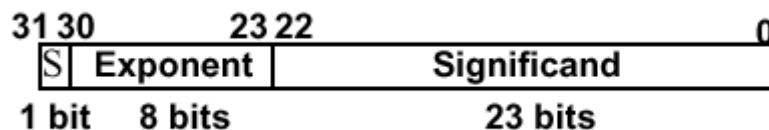
and can be in *normalized form* (mantissa has exactly one digit to the left of the decimal point, e.g.,  $2.3425 \cdot 10^{-19}$ ) or *non-normalized form*. Binary scientific notation has the following configuration, which corresponds to the decimal forms:



Assume that we have the following *normal format* for scientific notation in Boolean numbers:

$$+1.\text{xxxxxxx}_2 \cdot \text{w}^{\text{yyyy}}_2,$$

where "xxxxxxx" denotes the *significand* and "yyyy" denotes the *exponent* and we assume that the number has sign S. This implies the following 32-bit representation for FP numbers:

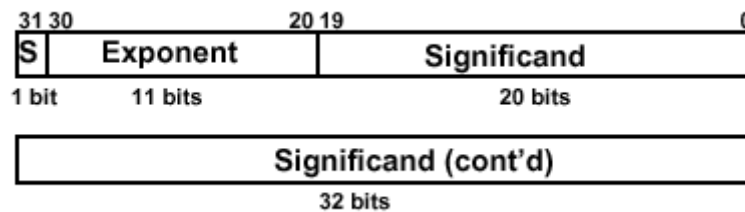


which can represent decimal numbers ranging from  $-2.0 \cdot 10^{-38}$  to  $2.0 \cdot 10^{38}$ .

### 3.4.2 Overflow and Underflow

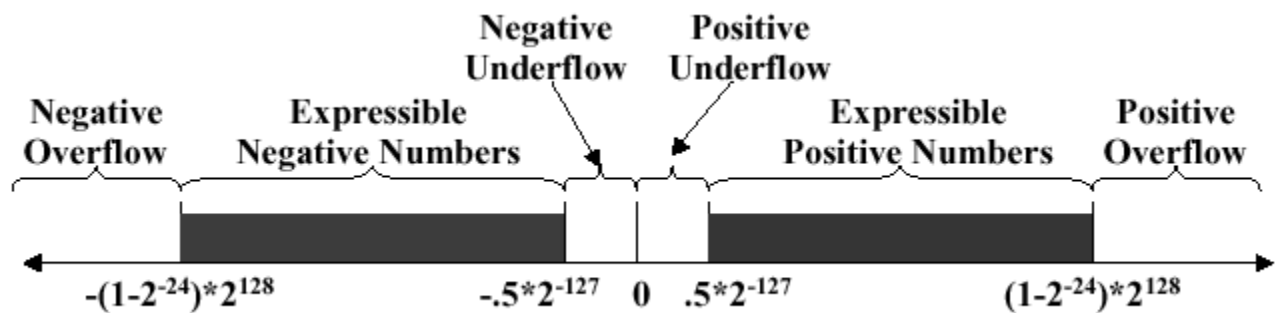
In FP, overflow and underflow are slightly different than in integer numbers. FP overflow (underflow) refers to the positive (negative) exponent being too large for the number of bits

allotted to it. This problem can be somewhat ameliorated by the use of *double precision*, whose format is shown as follows:



Here, two 32-bit words are combined to support an 11-bit signed exponent and a 52-bit significand. This representation is declared in C using the double datatype, and can support numbers with exponents ranging from  $-308_{10}$  to  $308_{10}$ . The primary advantage is greater precision in the mantissa.

The following chart illustrates specific types of overflow and underflow encountered in standard FP representation:



### 3.4.3. FP Arithmetic

Applying mathematical operations to real numbers implies that some error will occur due to the floating point representation. This is due to the fact that FP addition and subtraction are not associative, because the FP representation is only an approximation to a real number.

**Example 1.** Using decimal numbers for clarity, let  $x = -1.5 \cdot 10^{38}$ ,  $y = 1.5 \cdot 10^{38}$ , and  $z = 1.0$ . With floating point representation, we have:

$$x + (y + z) = -1.5 \cdot 10^{38} + (1.5 \cdot 10^{38} + 1.0) = 0.0$$

and

$$(x + y) + z = (-1.5 \cdot 10^{38} + 1.5 \cdot 10^{38}) + 1.0 = 1.0$$

The difference occurs because the value 1.0 cannot be distinguished in the significand of  $1.5 \cdot 10^{38}$  due to insufficient precision (number of digits) of the significand in the FP representation of these numbers (IEEE 754 assumed).

The preceding example leads to several implementational issues in FP arithmetic. Firstly, *rounding* occurs when performing math on real numbers, due to lack of sufficient precision. For example, when multiplying two N-bit numbers, a 2N-bit product results. Since only the upper N bits of the 2N bit product are retained, the lower N bits are *truncated*. This is also called *rounding toward zero*.

Another type of rounding is called *rounding to infinity*. Here, if rounding toward +infinity, then we always round up. For example, 2.001 is rounded up to 3, -2.001 is rounded up to 2. Conversely, if rounding toward -infinity, then we always round down. For example, 1.999 is rounded down to 1, -1.999 is rounded down to -2. There is a more familiar technique, for example, where 3.7 is rounded to 4, and 3.1 is rounded to 3. In this case, we resolve rounding from *n.5* to the nearest even number, e.g., 3.5 is rounded to 4, and -2.5 is rounded to 2.

A second implementational issue in FP arithmetic is addition and subtraction of numbers that have nonzero significands and exponents. Unlike integer addition, we can't just add the significands. Instead, one must:

1. Denormalize the operands and shift one of the operands to make the exponents of both numbers equal (we denote the exponent by E).
2. Add or subtract the significands to get the resulting significand.
3. Normalize the resulting significand and change E to reflect any shifts incurred by normalization.

We will review several approaches to floating point operations in MIPS in the following section.

### 3.5. Floating Point in MIPS

#### Reading Assignments and Exercises

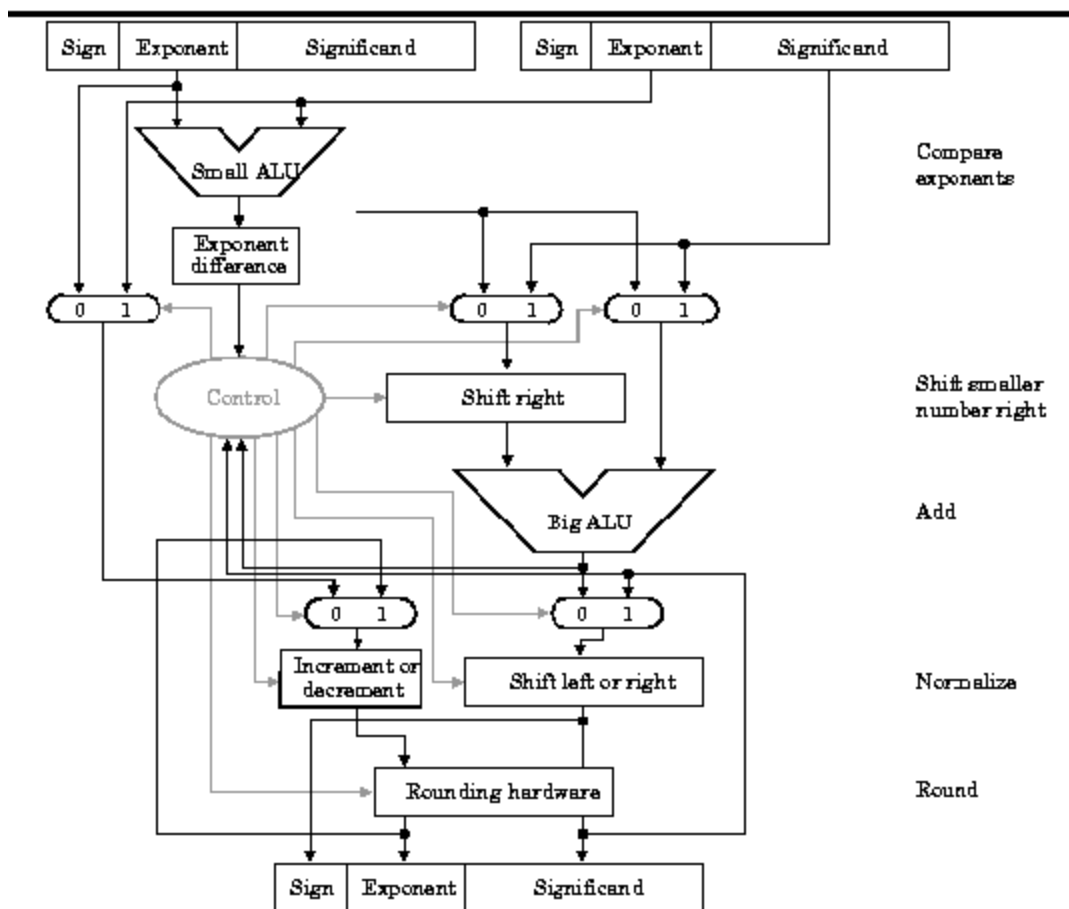
The MIPS FP architecture uses separate floating point instructions for IEEE 754 single and double precision. Single precision uses add.s, sub.s, mul.s, and div.s, whereas double precision instructions are add.d, sub.d, mul.d, and div.d. These instructions are much more complicated than their integer counterparts. Problems with implementing FP arithmetic include inefficiencies in having different instructions that take significantly different times to execute (e.g., division versus addition). Also, FP operations require much more hardware than integer operations.

Thus, in the spirit of RISC design philosophy, we note that (a) a particular datum is not likely to change its datatype within a program, and (b) some types of programs do not require FP computation. Thus, in 1990, the MIPS designers decided to separate the FP computations from the remainder of the ALU operations, and use a separate chip for FP (called the *coprocessor*). A MIPS coprocessor contains 32 32-bit registers designated as \$f0, \$f1, ..., etc. Most of these

registers are specified in the .s and .d instructions. Double precision operands are stored in *register pairs* (e.g., \$f0,\$f1 up to \$f30,\$f31).

The CPU thus handles all the regular computation, while the coprocessor handles the floating point operations. Special instructions are required to move data between the coprocessor(s) and CPU (e.g., mfc0, mtc0, mfc0, mtc0, etc.), where *cn* refers to coprocessor #*n*. Similarly, special I/O operations are required to load and store data between the coprocessor and memory (e.g., lwc0, swc0, lwc1, swc1, etc.)

FP coprocessors require very complex hardware, as shown in Figure 3.23, which portrays only the hardware required for addition.



**Figure 3.23.** MIPS ALU supporting floating point addition, adapted from [Maf01].

The use of floating point operations in MIPS assembly code is described in the following simple example, which implements a C program designed to convert Fahrenheit temperatures to Celsius.

```
Float f2c (float fahr) {  
    return ((5.0 / 9.0) * (fahr - 32.0));  
}
```



```
F2c:  
    lwc1 $f16, const5($gp)    # $f16 = 5.0  
    lwc1 $f18, const9($gp)    # $f18 = 9.0  
    div.s $f16, $f16, $f18    # $f16 = 5.0/9.0  
    lwc1 $f20, const32($gp)   # $f20 = 32.0  
    sub.s $f20, $f12, $f20    # $f20 = fahr - 32.0  
    mul.s $f0, $f16, $f20     # $f0 = (5/9)*(fahr-32)  
    jr    $ra                 # return
```

Here, we assume that there is a coprocessor c1 connected to the CPU. The values 5.0 and 9.0 are respectively loaded into registers \$f16 and \$f18 using the lwc1 instruction with the global pointer as base address and the variables const5 and const9 as offsets. The single precision division operation puts the quotient of 5.0/9.0 into \$f16, and the remainder of the computation is straightforward. As in all MIPS procedure calls, the jr instruction returns control to the address stored in the \$ra register.



## UNIT-IV

**Memory organization:** Memory hierarchy, main memory, auxiliary memory, associative memory, cache memory, virtual memory; **Input or output organization:** Input or output Interface, asynchronous data transfer, modes of transfer, priority interrupt, direct memory access.

### MEMORY ORGANIZATION

- RAM composed of a large number of ( $2^M$ ) of addressable locations, each of which stores a  $w$ -bit word.
- RAM operates as follows: first the address of the target location to be accessed is transferred via the address bus to the RAM's address buffer.
- The address is then processed by the address decoder, which selects the required location in the storage cell unit.
- If a read operation is requested, the contents of the addressed location are transferred from the storage cell unit to the data buffer and from there to the data bus.
- If a write operation is requested, the word to be stored is transferred from the data bus to the selected location in the stored unit. The storage unit is made up of many identical 1-bit memory cells and their Interconnections. In each line connected to the storage cell unit, we can expect to
- find a driver that acts as either an amplifier or a transducer of physical signals.

### Organization

- assume that each word is stored in a single track and that each access results in the transfer of a block of words.
- The address of the data to be accessed is applied to the address decoder, whose output determines the track to be used and the location of the desired block of information within the track.
- the track address determines the particular read-write head to be selected. The selected head is moved into position to transfer data to or from the target track. A track position indicator generates the address of the block that is currently passing the read-write head.
- The generated address is compared with the block address produced by the address decoder. The selected head is enabled and the data transfer between the storage track and the memory data buffer register begins.
- The read-write head is disabled when a complete block of information has been transferred.

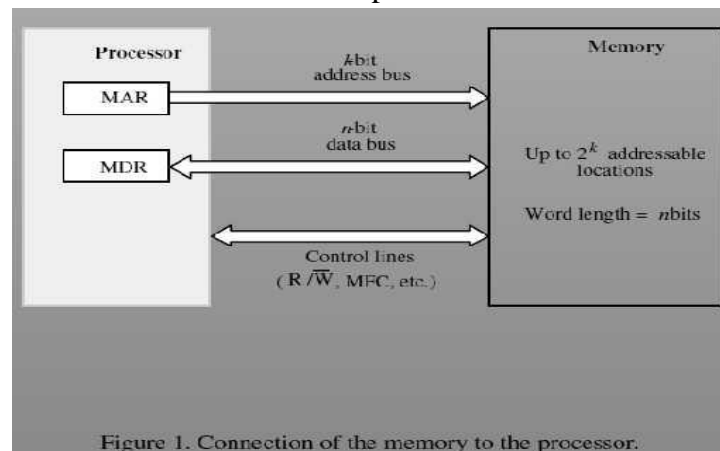
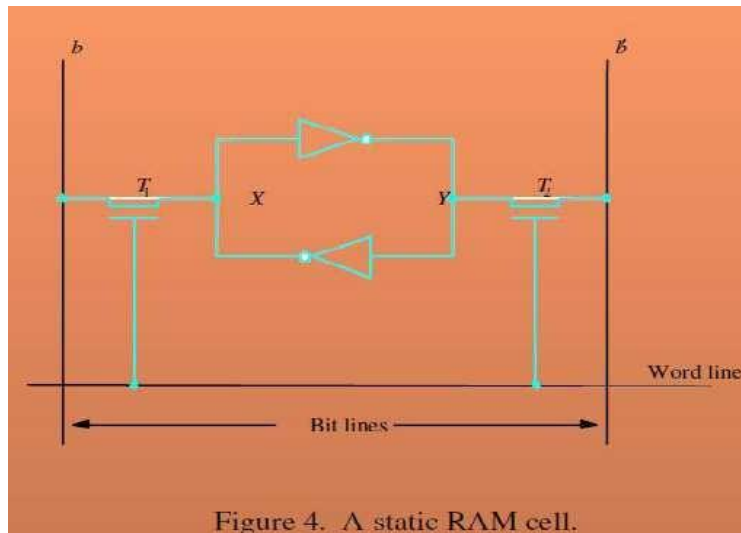


Figure 1. Connection of the memory to the processor.

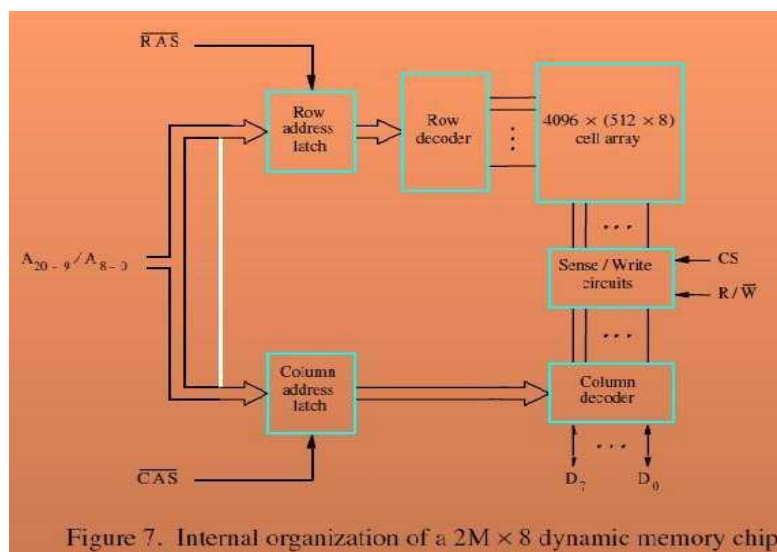


### Static memories (RAM)

- Circuits capable of retaining their state as long as power is applied
- *Static* RAM(SRAM)
- *volatile*

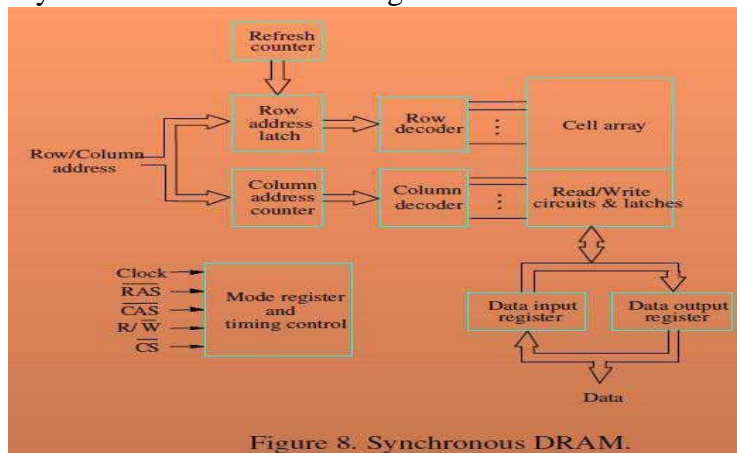
### DRAMS:

- Charge on a capacitor
- Needs —Refreshing



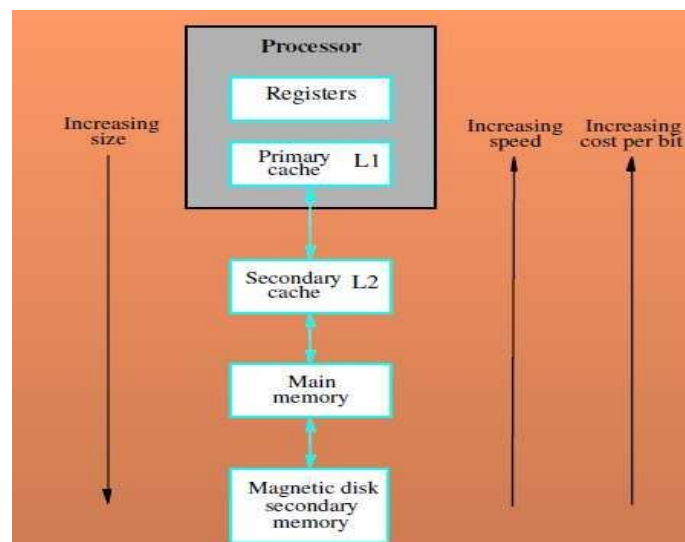
## Synchronous DRAMs

Synchronized with a clock signal



Memory system considerations

- Cost
- Speed
- Power dissipation
- Size of chip



### Principle of locality:

**Temporal locality** (locality in time): If an item is referenced, it will tend to be referenced again soon.

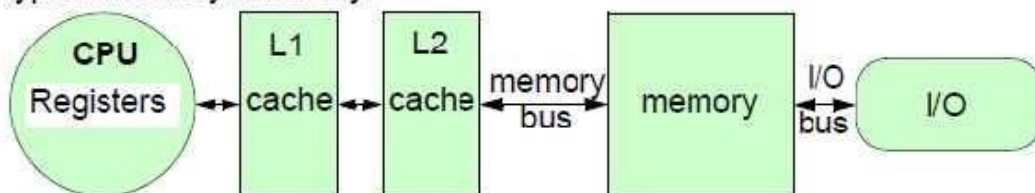
**Spatial locality** (locality in space): If an item is referenced, items whose addresses are close by will tend to be referenced soon.

**Sequentiality** (subset of spatial locality ).

The principle of locality can be exploited implementing the memory of computer as a *memory hierarchy*, taking advantage of all types of memories.

**Method:** The level closer to processor (the fastest) is a subset of any level further away, and all the data is stored at the lowest level (the slowest).

Typical memory hierarchy:



Level	1	2	3	4
Named as	Registers	Cache	memory	disk storage
Typical size	<1 KB	< 4 MB	<2 GB	>2GB
Access time (ns)	2 - 5	3 - 10	80 - 400	5'000'000
Dandwidth(MB/sec)	4000 - 32'000	800 - 5000	400 - 2000	4 - 32
Managed by	Compiler	Hardware	Operating system	Operating system / user

### Cache Memories

- Speed of the main memory is very low in comparison with the speed of processor
- For good performance, the processor cannot spend much time of its time waiting to access instructions and data in main memory.
- Important to device a scheme that reduces the time to ace the information
- An efficient solution is to use fast cache memory When a cache is full and a memory word

that is not in the cache is referenced, the cache control hardware must decide which block should be removed to create space for the new block that contain the referenced word.

### The basics of Caches

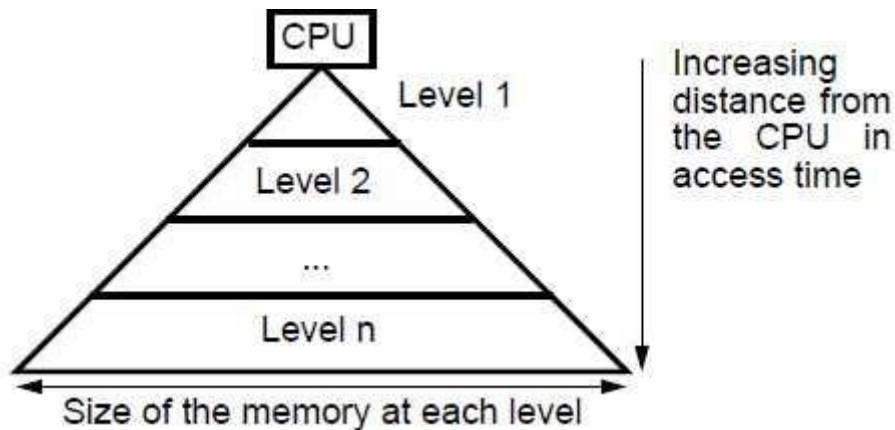
" The caches are organized on basis of *blocks*, the smallest amount of data which can be copied between two adjacent levels at a time.

" If data requested by the processor is present in some block in the upper level, it is called a *hit*.

" If data is not found in the upper level, the request is called a *miss* and the data is retrieved from the lower level in the hierarchy.

" The fraction of memory accesses found in the upper level is called a *hit ratio*.

" The storage, which takes advantage of locality of accesses is called a *cache*



Amdahl's Law about overall speedup:

$$\text{Speedup} = \frac{1}{(1 - \text{fraction of time cache can be used}) + \frac{\text{fraction of time cache can be used}}{\text{Speedup using cache}}}$$

Alternatively, CPU stalls can be considered<sup>1</sup>:

CPU execution time = (CPU clock cycles + Memory stall cycles) × Clock cycle

The number of memory stall cycles depends:

Memory stall cycles = IC × Memory references per instruction × Miss rate × Miss penalty

Size	Instruction cache	Data cache	
1 KB	3.06%	24.61%	13.34%
4 KB	1.76%	15.94%	7.24%
16 KB	0.64%	6.47%	2.87%
64 KB	0.15%	3.77%	1.35%

**Table: Direct mapped cache, 32-byte blocks, SPEC92, DECstation 5000.**

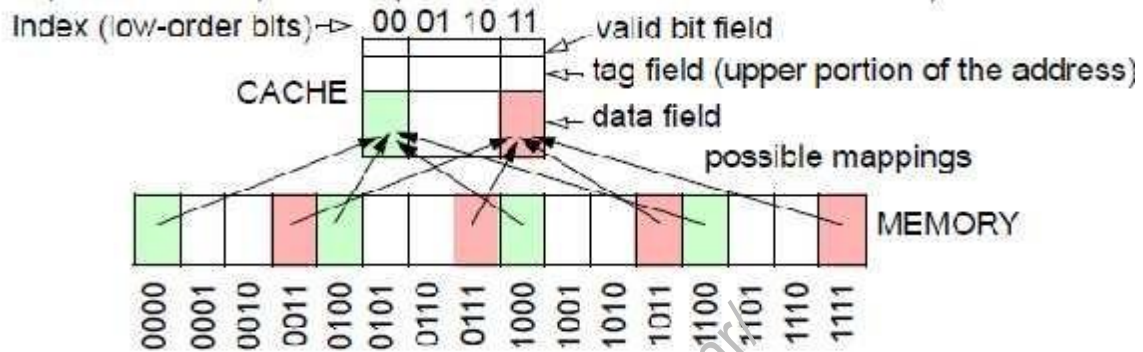
---

1. Here is assumed that CPU clock cycles include the time to handle a cache hit, and the CPU is stalled during a cache miss.

## ACCESSING A CACHE

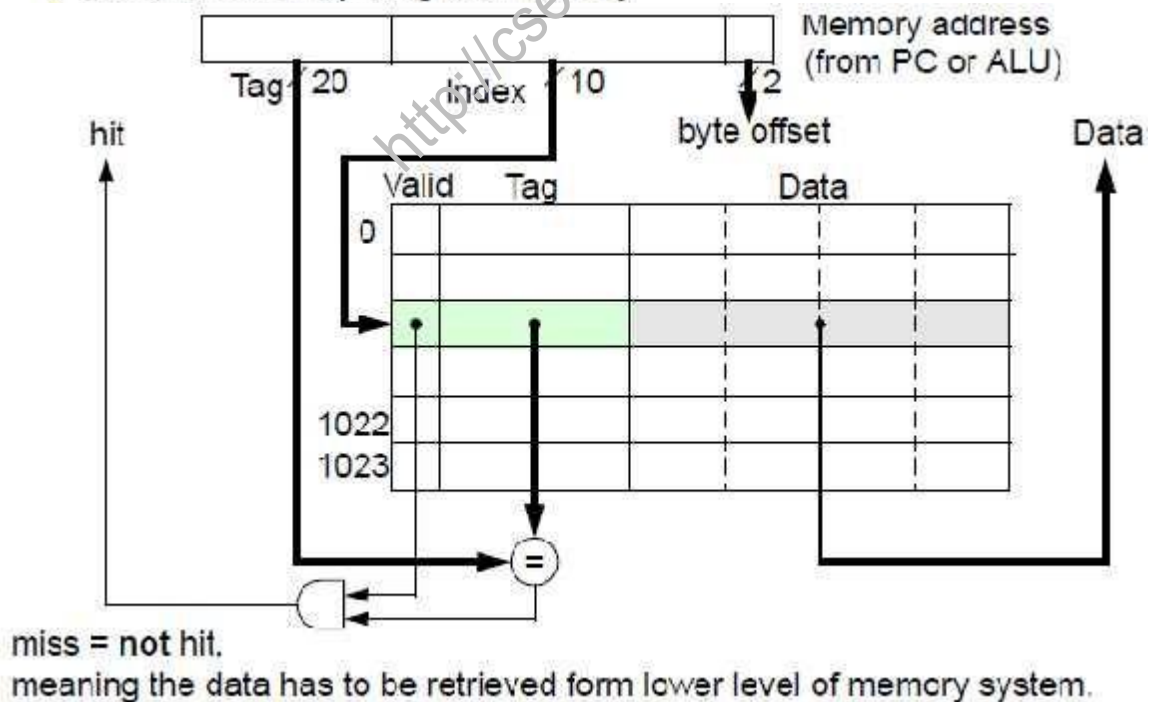
### ◆ Direct mapping:

(Block address) modulo (Number of cache blocks in the cache)



The *valid bit* indicates whether an entry contains a valid address. Initially, all valid bits are reset ("0" - not valid).

### ◆ Small fast memory + big slow memory



## Virtual memory

It is a computer system technique which gives an application program the impression that it has contiguous working memory (an address space), while in fact it may be physically fragmented and may even overflow on to disk storage.

Virtual memory provides two primary functions:

1. Each process has its own address space, thereby not required to be relocated nor required to use relative addressing mode.
2. Each process sees one contiguous block of free memory upon launch. Fragmentation is hidden.

## MEMORY MANAGEMENT REQUIREMENTS

### Partitioning Strategies – Fixed

Fixed Partitions – divide memory into equal sized pieces (except for OS)

- Degree of multiprogramming = number of partitions
- Simple policy to implement
  - All processes must fit into partition space
  - Find any free partition and load the process

### Partitioning Strategies – Variable

Idea: remove “wasted” memory that is not needed in each partition  
Memory is dynamically divided into partitions based on process needs  
Definition:

- *Hole*: a block of free or available memory
- Holes are scattered throughout physical memory
- *External fragmentation*
  - memory that is in holes too small to be usable by any process
  - Allocate part (or all) of memory to process and mark remainder as free
- *Compaction*
  - Moving things around so that holes can be consolidated
  -



## MEMORY MANAGEMENT POLICIES:

- *First Fit*: scan free list and allocate first hole that is large enough
- *Next Fit*: start search from end of last allocation
- *Best Fit*: find smallest hole that is adequate slower and lots of fragmentation
- *Worst fit*: find largest hole

## ASSOCIATIVE MEMORY

□ A content addressable processor is a content addressable memory with the added capability to write in parallel (multi-write) into all those words indicating agreement as the result of a search.

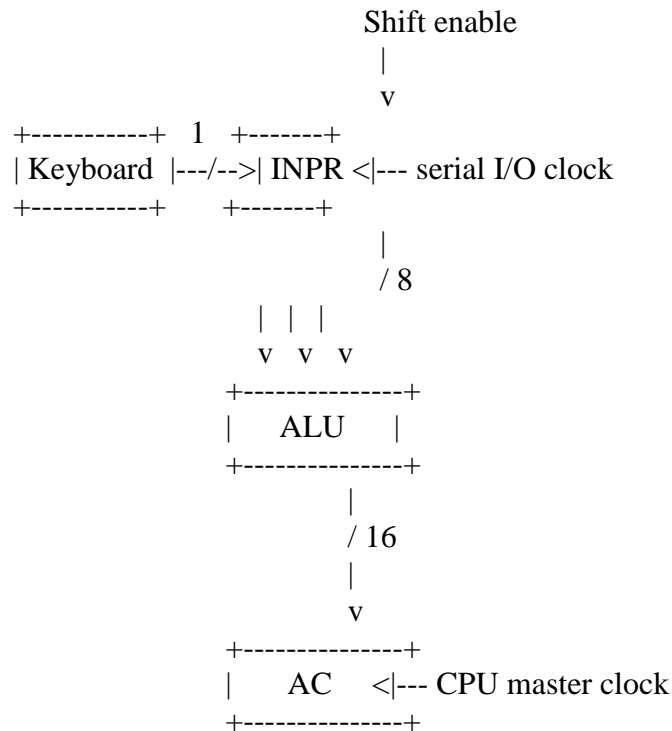
□□□□ A typical associative memory has the following components:

- Memory array
  - Comparand register
  - Mask register
  - Match/Mismatch (response) register
  - Multiple match resolver
  - Search logic
  - Input/Output register
  - Word select register
- 
- Mask Register is used to mask off portions of the data words which do not participate in the operations.
  - Word Select Register is used to mask off the memory words which do not participate in the operation.
  - Match/Mismatch Register indicates the success or failure of a search operation.
  - Input/Output Buffer acts as an interface between associative memory and the outside word.
  - Multiple Match Resolver narrows down the scope of the search to a specific location in the memory cell array in a cases where more than one memory word will satisfy the search condition(s).
  - Some/None bit shows the overall search result.

## Input-Output and Interrupt

The Basic Computer I/O consists of a simple terminal with a keyboard and a printer/monitor.

The keyboard is connected serially (1 data wire) to the INPR register. INPR is a shift register capable of shifting in external data from the keyboard one bit at a time. INPR outputs are connected in parallel to the ALU.



How many CPU clock cycles are needed to transfer a character from the keyboard to the INPR register? (tricky)

Are the clock pulses provided by the CPU master clock?

RS232, USB, Firewire are serial interfaces with their own clock independent of the CPU. ( USB speed is independent of processor speed. )

- RS232: 115,200 kbps (some faster)
- USB: 11 mbps
- USB2: 480 mbps
- FW400: 400 mbps
- FW800: 800 mbps
- USB3: 4.8 gbps

OUTR inputs are connected to the bus in parallel, and the output is connected serially to the terminal. OUTR is another shift register, and the printer/monitor receives an end-bit during each clock pulse.

## I/O Operations

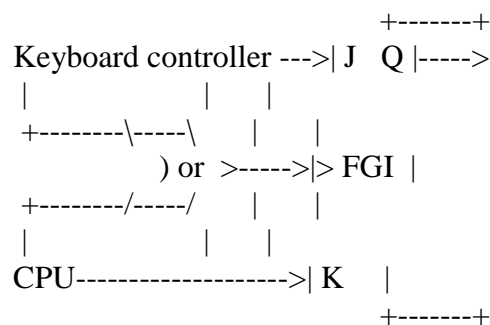
Since input and output devices are not under the full control of the CPU (I/O events are asynchronous), the CPU must somehow be told when an input device has new input ready to send, and an output device is ready to receive more output.

The FGI flip-flop is set to 1 after a new character is shifted into INPR. This is done by the I/O interface, not by the control unit. This is an example of an asynchronous input event (not synchronized with or controlled by the CPU).

The FGI flip-flop must be cleared after transferring the INPR to AC. This must be done as a microoperation controlled by the CU, so we must include it in the CU design.

The FGO flip-flop is set to 1 by the I/O interface after the terminal has finished displaying the last character sent. It must be cleared by the CPU after transferring a character into OUTR.

Since the keyboard controller only sets FGI and the CPU only clears it, a JK flip-flop is convenient:



How do we control the CK input on the FGI flip-flop? (Assume leading-edge triggering.)

There are two common methods for detecting when I/O devices are ready, namely *software polling* and *interrupts*. These two methods are discussed in the following sections.

Table 5-5 outlines the Basic Computer input-output instructions.

## Interrupts

To alleviate the problems of software polling, a hardware solution is needed.

Analogies to software polling in daily life tend to look rather silly. For example, imagine a teacher is analogous to a CPU, and the students are I/O devices. The students are working asynchronously, as the teacher walks around the room constantly asking each individual student "are you done yet?".

What would be a better approach?

With interrupts, the running program is not responsible for checking the status of I/O devices. Instead, it simply does its own work, and assumes that I/O will take care of itself!

When a device becomes ready, the CPU *hardware* initiates a branch to an I/O subprogram called an *interrupt service routine (ISR)*, which handles the I/O transaction with the device.

An interrupt can occur during *any* instruction cycle as long as interrupts are enabled. When the current instruction completes, the CPU interrupts the flow of the program, executes the ISR, and then resumes the program. The program itself is not involved and is in fact unaware that it has been interrupted.

Figure 5-13 outlines the Basic Computer interrupt process.

Interrupts can be globally enabled or disabled via the IEN flag (flip-flop).

Some architectures have a separate ISR for each device. The Basic Computer has a single ISR that services both the input and output devices.

If interrupts are enabled, then when either FGI or FGO gets set, the R flag also gets set. ( $R = FGI \vee FGO$ ) This allows the system to easily check whether *any* I/O device needs service. Determining which one needs service can be done by the ISR.

If  $R = 0$ , the CPU goes through a normal instruction cycle. If  $R = 1$ , the CPU branches to the ISR to process an I/O transaction.

How much time does checking for interrupts add to the instruction cycle?

Interrupts are usually disabled while the ISR is running, since it is difficult to make an ISR *reentrant*. (Callable while it is already in progress, such as a recursive function.) Hence, IEN and R are cleared as part of the interrupt cycle. IEN should be re-enabled by the ISR when it is finished. ( In many architectures this is done by a special return instruction to ensure that interrupts are not enabled before the return is actually executed. )

The Basic Computer interrupt cycle is shown in figure 5-13 (above).

The Basic Computer interrupt cycle in detail:

$T_0 T_1 T_2 (IEN)(FGI \vee FGO): R \leftarrow 1$

RT<sub>0</sub>: AR  $\leftarrow$  0, TR  $\leftarrow$  PC

RT<sub>1</sub>: M[AR]  $\leftarrow$  TR, PC  $\leftarrow$  0

RT<sub>2</sub>: PC  $\leftarrow$  PC + 1, IEN  $\leftarrow$  0, R  $\leftarrow$  0, SC  $\leftarrow$  0

To enable the use of interrupts requires several steps:

1. Write an ISR
2. Install the ISR in memory at some arbitrary address X
3. Install the instruction "BUN X" at address 1
4. Enable interrupts with the ION instruction

The sequence of events utilizing an interrupt to process keyboard input is as follows:

1. A character is typed
2. FGI  $\leftarrow$  1 (same as with polling)
3. R  $\leftarrow$  1, IEN  $\leftarrow$  0
4. M[0]  $\leftarrow$  PC (store return address)
5. PC  $\leftarrow$  1 (branch to interrupt vector)
6. BUN X (branch to ISR)
7. ISR checks FGI (found to be 1)
8. INP (AC  $\leftarrow$  INPR)
9. Character in AC is placed in a queue
10. ISR checks FGO (found to be 0)
11. ION
12. BUN 0 I

Programs then read their input from a queue rather than directly from the input device. The ISR adds input to the queue as soon as it is typed, regardless of what code is running, and then returns to the running program.

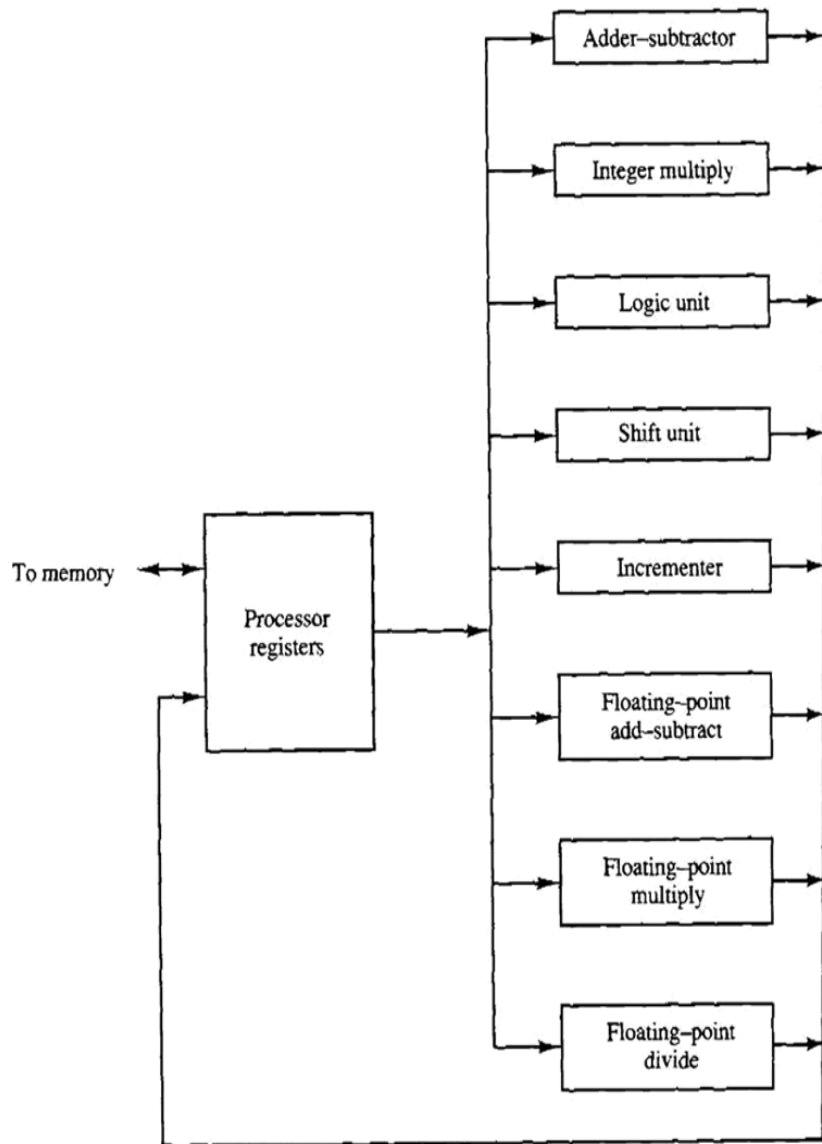
## UNIT-V

Pipeline: Parallel processing, pipelining-arithmetic pipeline, instruction pipeline;  
Multiprocessors: Characteristics of multiprocessors, inter connection structures, inter processor arbitration, and inter processor communication and synchronization

### **Parallel Processing**

- A parallel processing system is able to perform concurrent data processing to achieve faster execution time
- The system may have two or more ALUs and be able to execute two or more instructions at the same time
- Also, the system may have two or more processors operating concurrently
- Goal is to increase the *throughput* – the amount of processing that can be accomplished during a given interval of time
- Parallel processing increases the amount of hardware required
- Example: the ALU can be separated into three units and the operands diverted to each unit under the supervision of a control unit
- All units are independent of each other
- A multifunctional organization is usually associated with a complex control unit to coordinate all the activities among the various components

Figure 9-1 Processor with multiple functional units.



- Parallel processing can be classified from:
  - The internal organization of the processors
  - The interconnection structure between processors
  - The flow of information through the system
  - The number of instructions and data items that are manipulated simultaneously
    - The sequence of instructions read from memory is the *instruction stream*
    - The operations performed on the data in the processor is the *data stream*
    - Parallel processing may occur in the instruction stream, the data stream, or both

### **Computer classification:**

- Single instruction stream, single data stream – SISD
- Single instruction stream, multiple data stream – SIMD
- Multiple instruction stream, single data stream – MISD
- Multiple instruction stream, multiple data stream – MIMD
- SISD – Instructions are executed sequentially. Parallel processing may be achieved by means of multiple functional units or by pipeline processing
- SIMD – Includes multiple processing units with a single control unit. All processors receive the same instruction, but operate on different data.
- MIMD – A computer system capable of processing several programs at the same time.
- We will consider parallel processing under the following main topics:

### **PIPELINING**

- Pipelining is a technique of decomposing a sequential process into sub operations, with each sub process being executed in a special dedicated segment that operates concurrently with all other segments
- Each segment performs partial processing dictated by the way the task is partitioned
- The result obtained from the computation in each segment is transferred to the next segment in the pipeline
- The final result is obtained after the data have passed through all segments
- Can imagine that each segment consists of an input register followed by an combinational circuit
- A clock is applied to all registers after enough time has elapsed to perform all segment activity
- The information flows through the pipeline one step at a time
  - Example:  $A_i * B_i + C_i$  for  $i = 1, 2, 3, \dots, 7$



- The suboperations performed in each segment are:

$$R1 \leftarrow A_i, R2 \leftarrow B_i$$

$$R3 \leftarrow R1 * R2, R4 \leftarrow C_i$$

$$R5 \leftarrow R3 + R4$$

Figure 9-2 Example of pipeline processing.

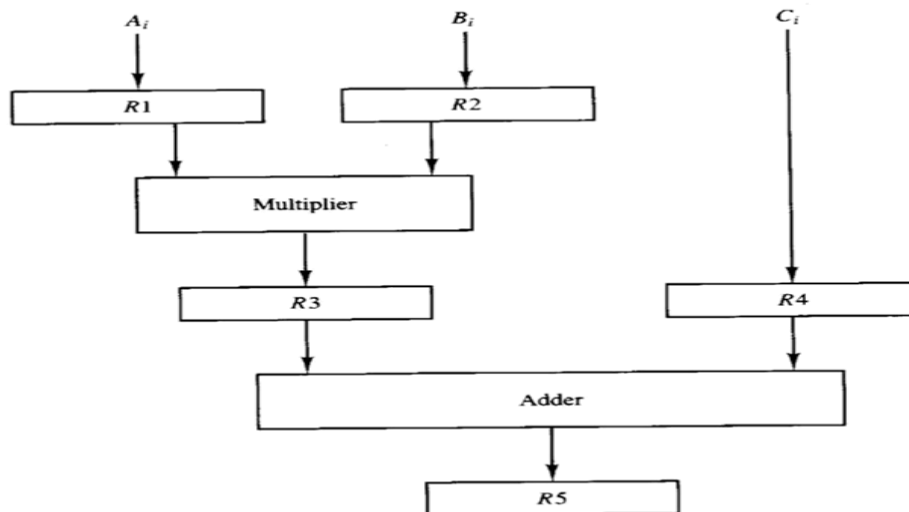


TABLE 9-1 Content of Registers in Pipeline Example

Clock Pulse Number	Segment 1		Segment 2		Segment 3
	R1	R2	R3	R4	R5
1	$A_1$	$B_1$	—	—	—
2	$A_2$	$B_2$	$A_1 * B_1$	$C_1$	—
3	$A_3$	$B_3$	$A_2 * B_2$	$C_2$	$A_1 * B_1 + C_1$
4	$A_4$	$B_4$	$A_3 * B_3$	$C_3$	$A_2 * B_2 + C_2$
5	$A_5$	$B_5$	$A_4 * B_4$	$C_4$	$A_3 * B_3 + C_3$
6	$A_6$	$B_6$	$A_5 * B_5$	$C_5$	$A_4 * B_4 + C_4$
7	$A_7$	$B_7$	$A_6 * B_6$	$C_6$	$A_5 * B_5 + C_5$
8	—	—	$A_7 * B_7$	$C_7$	$A_6 * B_6 + C_6$
9	—	—	—	—	$A_7 * B_7 + C_7$

- Any operation that can be decomposed into a sequence of suboperations of about the same complexity can be implemented by a pipeline processor
- The technique is efficient for those applications that need to repeat the same task many time with different sets of data
- A task is the total operation performed going through all segments of a pipeline
- The behavior of a pipeline can be illustrated with a *space-time* diagram
- This shows the segment utilization as a function of time
- Once the pipeline is full, it takes only one clock period to obtain an output

Figure 9-4 Space-time diagram for pipeline.

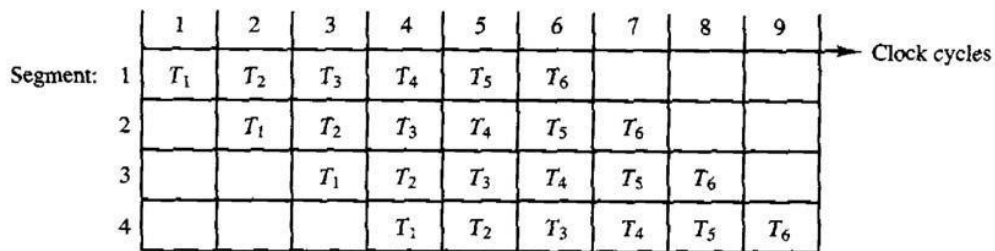


Figure 9-2 Example of pipeline processing.

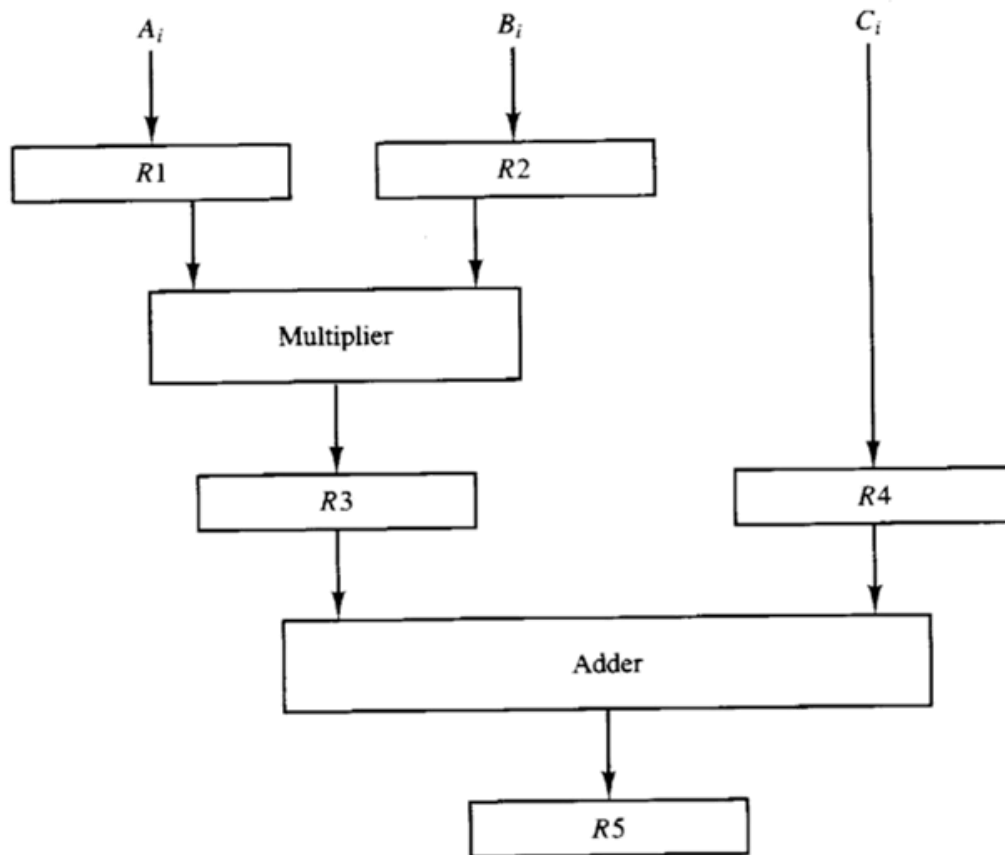
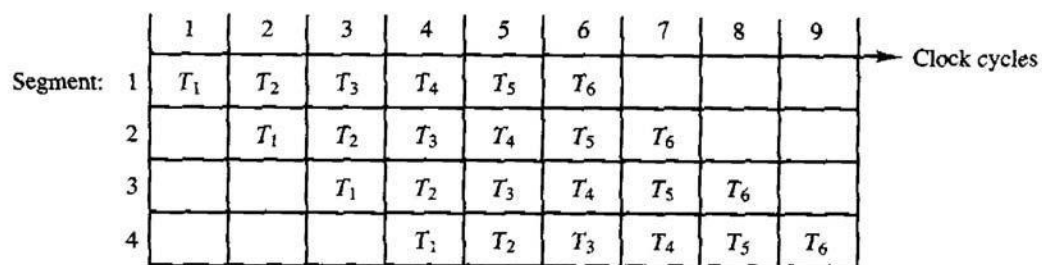


TABLE 9-1 Content of Registers in Pipeline Example

Clock Pulse Number	Segment 1		Segment 2		Segment 3
	R1	R2	R3	R4	R5
1	$A_1$	$B_1$	—	—	—
2	$A_2$	$B_2$	$A_1 * B_1$	$C_1$	—
3	$A_3$	$B_3$	$A_2 * B_2$	$C_2$	$A_1 * B_1 + C_1$
4	$A_4$	$B_4$	$A_3 * B_3$	$C_3$	$A_2 * B_2 + C_2$
5	$A_5$	$B_5$	$A_4 * B_4$	$C_4$	$A_3 * B_3 + C_3$
6	$A_6$	$B_6$	$A_5 * B_5$	$C_5$	$A_4 * B_4 + C_4$
7	$A_7$	$B_7$	$A_6 * B_6$	$C_6$	$A_5 * B_5 + C_5$
8	—	—	$A_7 * B_7$	$C_7$	$A_6 * B_6 + C_6$
9	—	—	—	—	$A_7 * B_7 + C_7$

- Any operation that can be decomposed into a sequence of suboperations of about the same complexity can be implemented by a pipeline processor
- The technique is efficient for those applications that need to repeat the same task many time with different sets of data
- A task is the total operation performed going through all segments of a pipeline
- The behavior of a pipeline can be illustrated with a *space-time* diagram
- This shows the segment utilization as a function of time
- Once the pipeline is full, it takes only one clock period to obtain an output

Figure 9-4 Space-time diagram for pipeline.



- Consider a  $k$ -segment pipeline with a clock cycle time  $t_p$  to execute  $n$  tasks
- The first task  $T_1$  requires time  $kt_p$  to complete
- The remaining  $n - 1$  tasks finish at the rate of one task per clock cycle and will be completed after time  $(n - 1)t_p$
- The total time to complete the  $n$  tasks is  $[k + n - 1]t_p$
- The example of Figure 9-4 requires  $[4 + 6 - 1]$  clock cycles to finish
- Consider a nonpipeline unit that performs the same operation and takes  $t_n$  time to complete each task
- The total time to complete  $n$  tasks would be  $nt_n$

- The *speedup* of a pipeline processing over an equivalent nonpipeline processing is defined by the ratio

$$S = \frac{nt_n}{(k + n - 1)t_p}$$

- As the number of tasks increase, the speedup becomes  $S = \frac{t_n}{t_p}$

- If we assume that the time to process a task is the same in both circuits,  $t_n = k t_p$   $S = \frac{k t_n}{t_p} = k$

- Therefore, the theoretical maximum speed up that a pipeline can provide is  $k$

- Example:

- Cycle time =  $t_p = 20$  ns ○ # of segments =  $k = 4$
- # of tasks =  $n = 100$

The pipeline system will take  $(k + n - 1)t_p = (4 + 100 - 1)20\text{ns} = 2060$  ns

Assuming that  $t_n = k t_p = 4 * 20 = 80$  ns,

A nonpipeline system requires  $n k t_p = 100 * 80 = 8000$  ns  
The speedup ratio =  $8000/2060 = 3.88$

- The pipeline cannot operate at its maximum theoretical rate
- One reason is that the clock cycle must be chosen to equal the time delay of the segment with the maximum propagation time
- Pipeline organization is applicable for arithmetic operations and fetching instructions

- As the number of tasks increase, the speedup becomes  $S = \frac{t_n}{t_p}$

$$t_p$$

- Therefore, the theoretical maximum speed up that a pipeline can provide is  $k$

- Example:

Cycle time =  $t_p = 20$  ns    # of segments =  $k = 4$   
 # of tasks =  $n = 100$

The pipeline system will take  $(k + n - 1)t_p = (4 + 100 - 1)20\text{ns} = 2060$  ns

Assuming that  $t_n = kt_p = 4 * 20 = 80$  ns,

A nonpipeline system requires  $nt_p = 100 * 80 = 8000$  ns  
 The speedup ratio =  $8000/2060 = 3.88$

- The pipeline cannot operate at its maximum theoretical rate
- One reason is that the clock cycle must be chosen to equal the time delay of the segment with the maximum propagation time
- Pipeline organization is applicable for arithmetic operations and fetching instructions

### Arithmetic Pipeline

- Pipeline arithmetic units are usually found in very high speed computers
- They are used to implement floating-point operations, multiplication of fixed-point numbers, and similar computations encountered in scientific problems
- Example for floating-point addition and subtraction
  - Inputs are two normalized floating-point binary numbers
 
$$X = A \times 2^a$$

$$Y = B \times 2^b$$
- A and B are two fractions that represent the mantissas
- a and b are the exponents

- Four segments are used to perform the following:
  - Compare the exponents    ○ Align the mantissas
  - Add or subtract the mantissas
  - Normalize the result

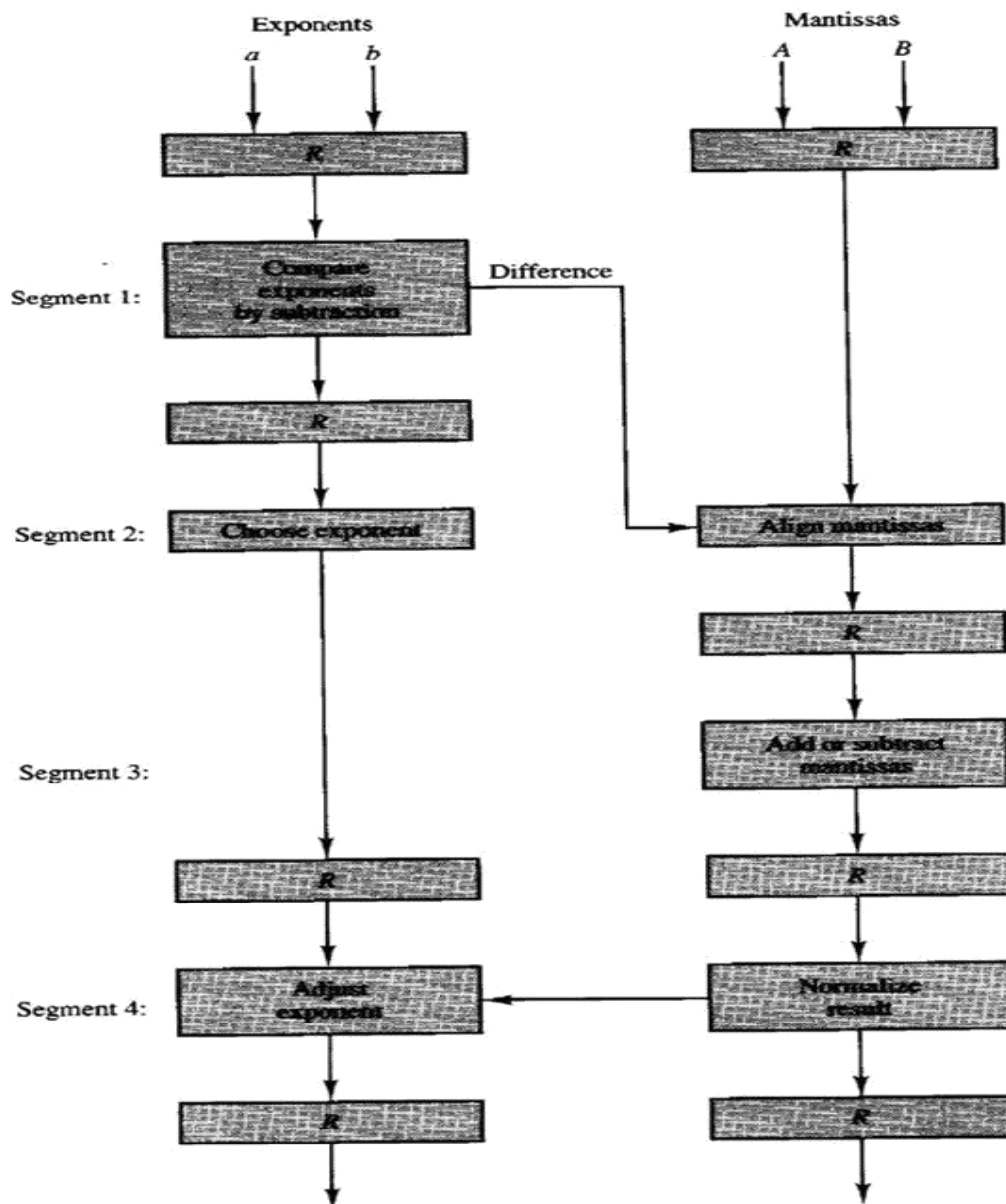


Figure 9-6 Pipeline for floating-point addition and subtraction.

- $X = 0.9504 \times 10^3$  and  $Y = 0.8200 \times 10^2$
- The two exponents are subtracted in the first segment to obtain  $3-2=1$
- The larger exponent 3 is chosen as the exponent of the result
- Segment 2 shifts the mantissa of Y to the right to obtain  $Y = 0.0820 \times 10^3$
- The mantissas are now aligned
- Segment 3 produces the sum  $Z = 1.0324 \times 10^3$
- Segment 4 normalizes the result by shifting the mantissa once to the right and incrementing the exponent by one to obtain  $Z = 0.10324 \times 10^4$

### Instruction Pipeline

- An instruction pipeline reads consecutive instructions from memory while previous instructions are being executed in other segments
- This causes the instruction fetch and execute phases to overlap and perform simultaneous operations
- If a branch out of sequence occurs, the pipeline must be emptied and all the instructions that have been read from memory after the branch instruction must be discarded
- Consider a computer with an instruction fetch unit and an instruction execution unit forming a two segment pipeline
- A FIFO buffer can be used for the fetch segment
- Thus, an instruction stream can be placed in a queue, waiting for decoding and processing by the execution segment
- This reduces the average access time to memory for reading instructions
- Whenever there is space in the buffer, the control unit initiates the next instruction fetch phase
- The following steps are needed to process each instruction:
  - Fetch the instruction from memory
  - Decode the instruction
  - Calculate the effective address
  - Fetch the operands from memory
  - Execute the instruction
  - Store the result in the proper place
- The pipeline may not perform at its maximum rate due to:
  - Different segments taking different times to operate
  - Some segment being skipped for certain operations
  - Memory access conflicts



- Example: Four-segment instruction pipeline
- Assume that the decoding can be combined with calculating the EA in one segment
- Assume that most of the instructions store the result in a register so that the execution and storing of the result can be combined in one segment

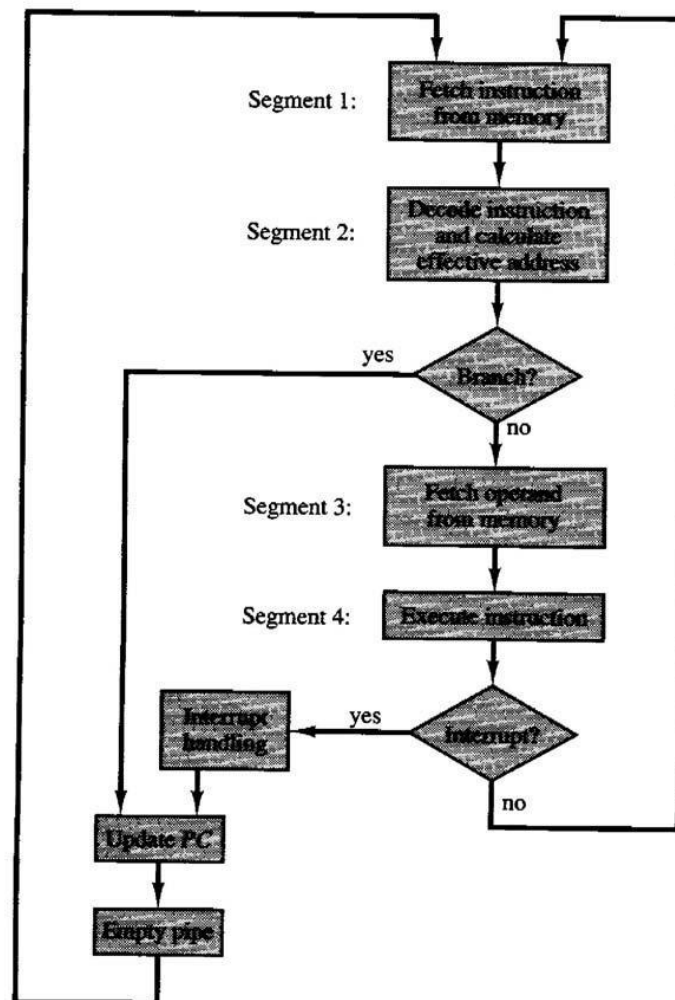


Figure 9-7 Four-segment CPU pipeline.

- Up to four suboperations in the instruction cycle can overlap and up to four different instructions can be in progress of being processed at the same time
- It is assumed that the processor has separate instruction and data memories
  
- Reasons for the pipeline to deviate from its normal operation are:
  - *Resource conflicts* caused by access to memory by two segments at the same time.
  - *Data dependency* conflicts arise when an instruction depends on the result of a previous instruction, but his result is not yet available

- Assume that most of the instructions store the result in a register so that the execution and storing of the result can be combined in one segment

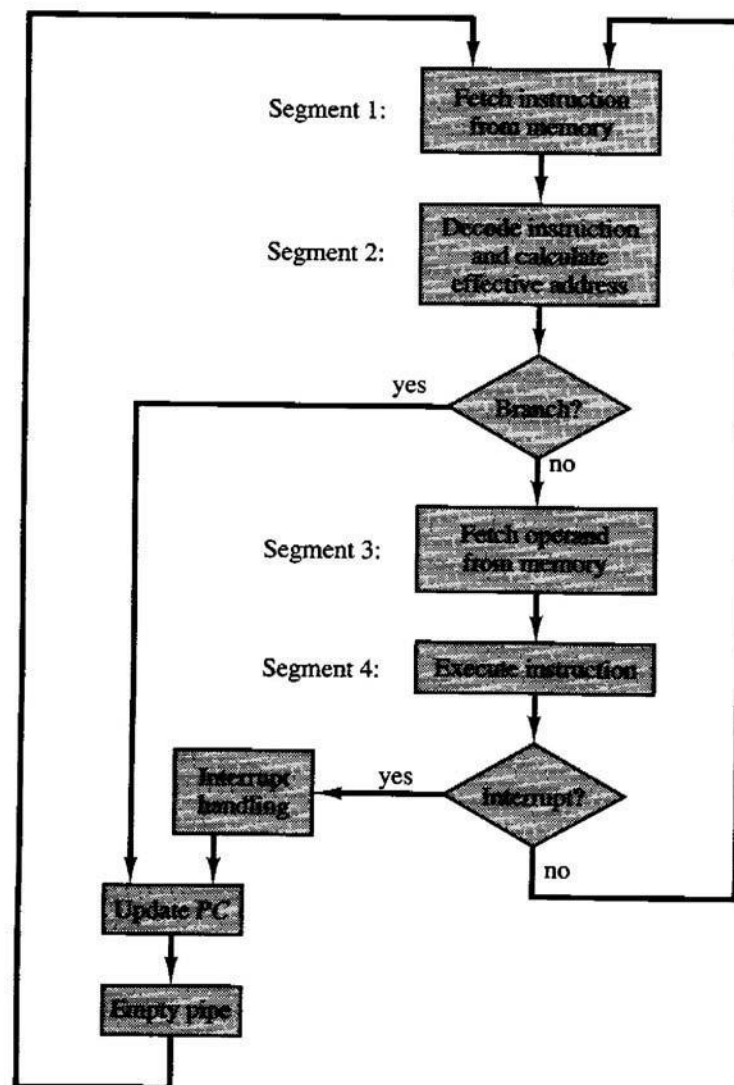


Figure 9-7 Four-segment CPU pipeline.

- Up to four suboperations in the instruction cycle can overlap and up to four different instructions can be in progress of being processed at the same time
- It is assumed that the processor has separate instruction and data memories
- Reasons for the pipeline to deviate from its normal operation are:

Resource conflicts caused by access to memory by two segments at the same time.

Data dependency conflicts arise when an instruction depends on the result of a previous instruction, but his result is not yet available

Branch difficulties arise from program control instructions that may change the value of PC

- Methods to handle data dependency:
  - Hardware interlocks are circuits that detect instructions whose source operands are destinations of prior instructions. Detection causes the hardware to insert the required delays without altering the program sequence.
  - Operand forwarding uses special hardware to detect a conflict and then avoid it by routing the data through special paths between pipeline segments. This requires additional hardware paths through multiplexers as well as the circuit to detect the conflict.
  - Delayed load is a procedure that gives the responsibility for solving data conflicts to the compiler. The compiler is designed to detect a data conflict and reorder the instructions as necessary to delay the loading of the conflicting data by inserting no-operation instructions.
- Methods to handle branch instructions:
  - *Prefetching the target instruction* in addition to the next instruction allows either instruction to be available.
  - *A branch target buffer* is an associative memory included in the fetch segment of the branch instruction that stores the target instruction for a previously executed branch. It also stores the next few instructions after the branch target instruction. This way, the branch instructions that have occurred previously are readily available in the pipeline without interruption.
  - *The loop buffer* is a variation of the BTB. It is a small very high speed register file maintained by the instruction fetch segment of the pipeline. Stores all branches within a loop segment.

- *Branch prediction* uses some additional logic to guess the outcome of a conditional branch instruction before it is executed. The pipeline then begins prefetching instructions from the predicted path.